
Supplementary Materials: Artificial Neural Networks to Predict the Apparent Degree of Supersaturation in Supersaturated Lipid-Based Formulations: A Pilot Study.

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Table S1. Equilibrium solubility values ($\mu\text{g}/\text{mL}$) and aDS for the dataset of 21 drugs using Capmul MCM and Maisine CC. AT refers to Ambient Temperature. Data in brackets refer to standard deviation (SD) of solubility value or standard error (SE) of aDS ratios. * denotes data obtained from a previous publication (1).

Drug Compound	AT Solubility Capmul MCM	AT Solubility Maisine CC	Solubility 60°C $sLBFC_{Capmul}^{MC}$	Solubility 60°C $sLBFC_{Maisine}^{LC}$	aDS $sLBFC_{Capmul}^{MC}$	aDS $sLBFC_{Maisine}^{LC}$
Carvedilol	45.07 (2.94)	10.28 (0.70)	127.90 (2.77)	28.91 (1.79)	2.84 (0.11)	2.81 (0.15)
Celecoxib	49.78 (5.61)*	13.30 (1.11)*	88.10 (6.67)	36.16 (2.83)	1.77 (0.14)	2.72 (0.18)
Cinnarizine	35.97 (1.03)*	29.27 (1.01)*	81.67 (3.98)	86.64 (6.54)	2.27 (0.07)	2.96 (0.14)
Clotrimazole	192.06 (5.91)	91.05 (3.73)	311.16 (13.89)	170.82 (5.27)	1.62 (0.05)	1.88 (0.06)
Danazol	16.32 (4.52)	11.19 (0.64)	42.91 (1.85)	22.41 (0.95)	2.63 (0.43)	2.00 (0.08)
Dipyridamole	10.17 (0.98)	1.38 (0.17)	32.22 (3.12)	4.71 (0.61)	3.17 (0.25)	3.42 (0.36)
Felodipine	74.41 (4.63)	36.79 (1.04)	125.73 (12.40)	49.71 (6.19)	1.69 (0.11)	1.35 (0.10)
Fenofibrate	76.95 (6.66)	50.11 (1.38)	136.98 (11.10)	144.38 (8.82)	1.78 (0.12)	2.88 (0.11)
Fenofibric acid	11.81 (4.77)	7.80 (0.26)	36.28 (1.55)	18.45 (0.56)	3.07 (0.72)	2.37 (0.06)
Griseofulvin	4.70 (0.51)	1.92 (0.01)	12.55 (0.52)	3.68 (0.26)	2.67 (0.18)	1.91 (0.08)
Haloperidol	31.37 (1.34)	7.63 (0.94)	46.03 (1.43)	14.22 (0.45)	1.47 (0.04)	1.86 (0.14)
Ibuprofen	237.34 (14.85)	128.67 (4.05)	616.10 (103.62)	436.41 (46.36)	2.60 (0.27)	3.39 (0.22)
Indometacine	21.31 (0.70)	7.84 (0.30)	35.53 (1.55)	14.45 (0.25)	1.67 (0.05)	1.84 (0.04)
Itraconazole	1.99 (0.02)	0.53 (0.01)	5.12 (0.49)	1.16 (0.03)	2.57 (0.14)	2.18 (0.03)
JNJ-2a	283.07 (15.58)*	47.50 (1.24)	293.35 (27.73)	76.48 (2.92)	1.04 (0.07)	1.61 (0.04)
Ketoconazole	104.92 (3.32)	29.62 (0.25)	221.22 (2.98)	66.14 (5.06)	2.11 (0.04)	2.23 (0.10)
Naproxen	39.21 (4.83)	17.27 (1.98)	50.73 (6.04)	25.90 (0.45)	1.29 (0.13)	1.50 (0.10)
Niclosamide	8.73 (0.55)	3.21 (0.25)	14.96 (0.96)	5.44 (0.22)	1.71 (0.09)	1.70 (0.09)
Progesterone	97.92 (9.08)	49.49 (0.84)	163.96 (19.86)	112.75 (6.06)	1.67 (0.15)	2.28 (0.07)
Sulfalazine	3.79 (0.08)	0.20 (0.03)	4.89 (0.13)	0.32 (0.03)	1.29 (0.03)	1.62 (0.17)
Venetoclax	2.45 (0.41)	2.44 (0.16)	6.43 (0.28)	3.62 (0.84)	2.62 (0.12)	1.48 (0.21)

Table S2. RP-HPLC/UV Methods utilised in this study. ACN refers to Acetonitrile, MeOH refers to Methanol, TFA refers to Trifluoroacetic Acid, H₂O refers to Water and NaAC refers to Sodium Acetate. * denotes the fact that the mobile phase was adjusted to pH 2.5 with 5 %v/v Orthophosphoric acid.

Drug	Column	A	B	Ratio	Temp (°C)	Flow Rate (ml/min)	Inj. (μL)	Vol	λ (nm)
Danazol	Symmetry C18 5 μm, 4,6 x 150 mm	ACN	H ₂ O	55:45	25	1	50	286	
Ketoconazole	Symmetry C18 5 μm, 4,6 x 150 mm	Phosphate buffer 10 mM, pH 8.5	ACN	40:60	25	0.8	50	297	
Venetoclax	Zorbax Eclipse Plus-C18 column (5 μm, 4.6 mm x 150 mm) including Zorbax 156 Eclipse Plus-C18 guard column (5 μm, 4.6 mm x 12.5 mm)	ACN + 0.5 % TFA	H ₂ O + 0.5 % TFA	53:47	40	1	50	316	
Carvedilol	Symmetry C18 5 μm, 4,6 x 150 mm	ACN	NaAc 25 mM, pH 5.0	60:40	25	1	50	280	
Clotrimazole	Symmetry C18 5 μm, 4,6 x 150 mm	MeOH	ACN	95:5	25	1	50	255	
Griseofulvin	Symmetry C18 5 μm, 4,6 x 150 mm	ACN	H ₂ O	55:45	25	1	50	292	
Dipyridamole	Gemini 5μ C18 4,6 x 250 mm	ACN	H ₂ O	60:40	40	1	20	282	
Felodipine	Gemini 5μ C18 4,6 x 250 mm	ACN	H ₂ O	70:30	25	1	20	360	
Haloperidol	Symmetry C18 5 μm, 4,6 x 150 mm	ACN:MeOH	NaAc 25 mM, pH 5.0	65:35	25	0.8	50	247	
Naproxen	Symmetry C18 5 μm, 4,6 x 150 mm	ACN + 0.1% TFA	H ₂ O + 0.1% TFA	60:40	25	1	50	254	
Niclosamide	Symmetry C18 5 μm, 4,6 x 150 mm	95:5:0.1 ACN:H ₂ O:TFA	5:95:0.1 ACN:H ₂ O:TFA	75:25	25	1	50	332	
Progesterone	Symmetry C18 5 μm, 4,6 x 150 mm	ACN	NaAc 25 mM, pH 5.5	85:15	25	1	50	254	
Sulfalazine	Symmetry C18 5 μm, 4,6 x 150 mm	ACN:H ₂ O:TFA	H ₂ O:ACN:TFA	60:40	25	1	50	357	
Fenofibric Acid	Symmetry C18 5 μm, 4,6 x 150 mm	ACN*	H ₂ O*	70:30	25	1	20	286	

Table S3. Equilibrium solubility and aDS_{2h} in sLBF_{Capmul^{MC}} and sLBF_{Maisine^{LC}} and the aDS ratio difference from average aDS and average aDS_{2h} used to investigate the short term stability of the sLBF after cooling at AT.

	Solubility 60°C (+2h) Capmul MCM	Solubility 60°C (+2h) Maisine CC	aDS _{2h} sLBF _{Capmul^{MC}}	aDS _{2h} sLBF _{Maisine^{LC}}	aDS Ratio Unit Change	aDS Ratio Unit Change
Carvedilol	116.44 (6.57)	27.75 (1.02)	2.58 (0.13)	2.70 (0.12)	0.25	0.11
Celecoxib	101.8 (0.0)	39.6 (0.0)	2.04 (0.13)	2.97 (0.14)	0.27	0.25
Cinnarizine	100.1 (0.0)	97.5 (0.0)	2.78 (0.05)	3.33 (0.07)	0.51	0.34
Clotrimazole	308.30 (1.28)	172.73 (0.90)	1.61 (0.03)	1.74 (0.04)	0.01	0.13
Danazol	39.99 (3.54)	22.57 (1.88)	2.45 (0.41)	2.02 (0.12)	0.18	0.01
Dipyridamole	29.55 (4.25)	4.53 (0.49)	2.91 (0.29)	3.29 (0.31)	0.26	0.13
Felodipine	125.19 (5.94)	45.89 (9.05)	1.68 (0.08)	1.25 (0.14)	0.01	0.10
Fenofibric Acid	32.74 (3.17)	17.86 (0.93)	2.77 (0.66)	2.29 (0.08)	0.30	0.08
Griseofulvin	12.21 (0.15)	3.70 (0.24)	2.59 (0.16)	1.92 (0.07)	0.07	0.01
Haloperidol	45.37 (0.24)	13.47 (0.79)	1.45 (0.04)	1.76 (0.14)	0.02	0.10
JNJ-2A	259.5 (0.0)	65.8 (0.0)	0.92 (0.03)	1.38 (0.02)	0.12	0.23
Ketoconazole	224.87 (11.29)	63.82 (3.81)	2.14 (0.07)	2.15 (0.08)	0.03	0.08
Naproxen	45.42 (7.01)	20.39 (2.82)	1.16 (0.13)	1.18 (0.12)	0.14	0.32
Niclosamide	14.06 (1.02)	5.13 (0.23)	1.61 (0.09)	1.60 (0.08)	0.10	0.10
Progesterone	133.30 (16.12)	99.09 (7.27)	1.36 (0.12)	2.00 (0.09)	0.31	0.28
Sulfalazine	4.69 (0.23)	0.30 (0.03)	1.24 (0.04)	1.49 (0.16)	0.05	0.13
Venetoclax	7.13 (1.29)	2.89 (0.52)	2.91 (0.32)	1.18 (0.13)	0.29	0.30

Figure S1. Unabridged Abbreviations of Independent Input Variables used in the final PLS and ANN models. Extra information about the descriptors used can be found at this reference (9).

Variables in PLS model predicting aDS sLBF_{Capmul^{MC}}:

- **VMcGowan:** Mc Gowan's characteristic volume (2) .
- **N_Hydrogn:** Number of hydrogens.
- **SHCH_321:** Atom-type hydrogen E-state index for -CH3, -CH2- and >CH- groups (saturated aliphatic carbon) (3).
- **EEM_Afc:** Sum of absolute values of scaled sigma Fukui indices on C (4, 5).
- **EEM_AFnp:** Sum of absolute values of scaled sigma Fukui indices on nonpolar atoms.
- **EEM_NFc:** Minimum scaled sigma Fukui index on C.
- **SHaaCH:** Atom-type hydrogen E-state index for aCHa groups (aromatic carbons).
- **Pi_FMi4:** Fourth component of the autocorrelation vector of scaled pi Fukui- indices (electrophilic).

Variables in PLS model predicting aDS sLBF_{Maisine^{LC}}:

- **EEM_NFc:** Minimum scaled sigma Fukui index on C.
- **EEM_NFnp:** Minimum scaled sigma Fukui index on nonpolar atoms.
- **HIVI-TC:** pIC50 in log(mol/L) for inhibition of the HIV-1 Integrase 3'-processing.
- **N_FrRotB:** Number of freely rotatable bonds.
- **NPA_Q2:** Second component of the autocorrelation vector of NPA partial atomic charges.
- **Pi_AQo:** Sum of absolute values of pi partial atomic charges on O.
- **Pi_AQc:** Sum of absolute values of pi partial atomic charges on C.
- **Pi_FPI3:** Third component of the autocorrelation vector of scaled pi Fukui+ indices (nucleophilic)
- **Pi_FMi6:** Sixth component of the autocorrelation vector of scaled pi Fukui- indices (electrophilic).

Variables in MLP-ANN Predicting aDS sLBF_{Capmul^{MC}}:

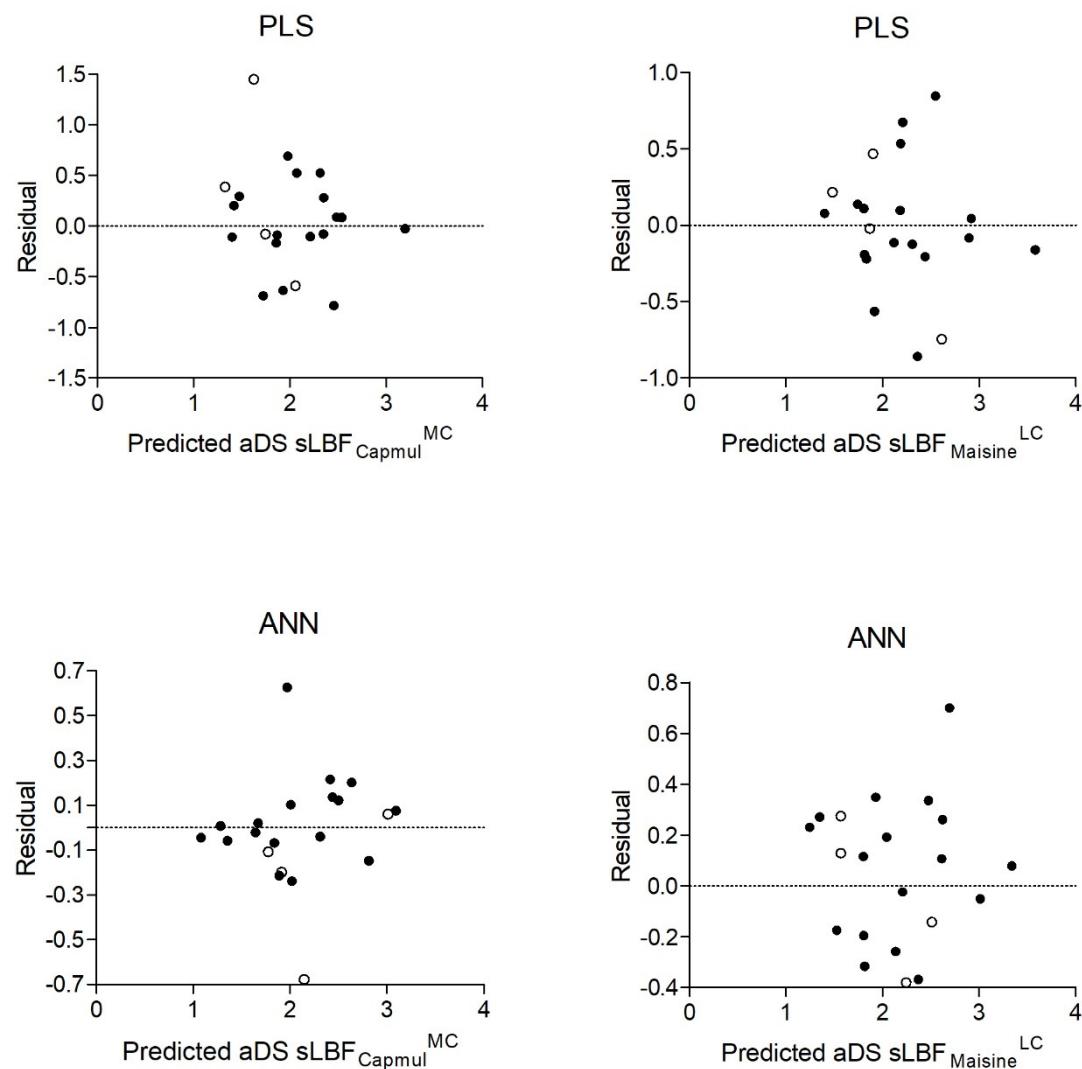
- **Pi_FPI5:** Fifth component of the autocorrelation vector of pi Fukui(+) indices.
- **SolFactor:** Universal salt solubility factor based on S+Sw model.
- **N_CYPAtoms:** Number of potential atoms that can be oxidized by CYP P450 enzymes.
- **EEM_F4:** Fourth component of the autocorrelation vector of sigma Fukui indices.
- **Pi_FPI3:** Third component of the autocorrelation vector of pi Fukui(+) indices.

- **NPA_Q6:** Sixth component of the autocorrelation vector of estimated NPA partial atomic charges (6, 7).
- **MlogP:** Moriguchi estimation of log P (8).
- **MolVol:** Liquid molar volume (cm^3/mol) at the normal boiling point is based on Schroeder's method.
- **NPA_Q1:** First component of the autocorrelation vector of estimated NPA partial atomic charges.
- **S+S_Intrinsic:** Intrinsic water solubility (mg/mL) based on S+Sw and S+pH_Satd models.
- **EqualEta:** Equalized molecular hardness.
- **ΔH_{fus} :** Enthalpy of fusion in kJ/mol obtained from literature.
- **M_CX:** Summation of numbers of carbon and halogen atoms weighted by C:1.0, F:0.5, Cl:1.0, Br:1.5, and I:2.0.
- **Pi_MinQ:** Minimum Hückel pi atomic charge.
- **N_Electr:** Total number of electrons in a molecule.

Variables in MLP-ANN Predicting aDS sLBF_{Maisine^{LC}}

- **N_Bonds:** Number of bonds.
- **Pi_FPl1:** First component of the autocorrelation vector of pi Fukui(+) indices.
- **T_Rads:** topological equivalent of Rads_3D.
- **MaxQ:** Maximal PEOE Partial Atomic Charge.
- **N_Atoms:** Number of atoms.
- **Pi_FMl1:** First component of the autocorrelation vector of pi Fukui(-) indices.
- **HBDch:** Sum of Estimated NPA Partial Atomic Charges on HB Donor Hydrogens.
- **F_AromB:** Aromatic bonds as fraction of total bonds.
- **NPA_Q2:** Second component of the autocorrelation vector of estimated NPA partial atomic charges.
- **SssCH:** Atom-type E-state index for >CH- groups.
- **NPA_Q5:** Fifth component of the autocorrelation vector of estimated NPA partial atomic charges.

Figure S2. Predicted by Residual plots for sLBF_{Capmul^{MC}} and sLBF_{Maisine^{LC}} using PLS and ANN modelling.



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