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Determining finite strain: how far have we progressed?

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Abstract

One of the main aims in the field of structural geology is the identification and quantification of deformation or strain. This pursuit has occupied geologists since the 1800's, but has evolved dramatically since those early studies. The quantification of strain in sedimentary lithologies was initially restricted to lithologies of known initial shape, such as fossils or reduction spots. In 1967, Ramsay presented a series of methods and calculations, which allowed populations of clasts to be used as strain markers. These methods acted as a foundation for modern strain analysis, and have influenced thousands of studies. This review highlights the significance of Ramsay's contribution to modern strain analysis. We outline the advances in the field over the 50 years since publication of the 'Folding and Fracturing of Rocks', review the existing limitations of strain analysis methods and look to future developments.

'The analysis of the variation in amount of finite strain in a deformed zone is of the utmost importance in helping to understand the structural geometry and hence the structural history of the rocks.'

John Ramsay, 1967

The field of structural geology is primarily concerned with understanding the deformation of crustal rocks. This deformation or strain is caused when external forces or stresses act on a rock mass, causing a change in its shape or size (Ramsay, 1967). The concept of quantifying strain in rocks has been prevalent since the 1800's, and has evolved dramatically since those early studies. Various methods have been used to identify and quantify strain, the earliest of which relied on objects of a known initial

shape. This approach was first taken by Phillips (1843) and Sharpe (1847) who used deformed fossils, with Sharpe (1847) noting that the most deformed fossils were present in the areas with the most intense cleavage. This led to Sorby's seminal interpretations of cleavage development (Sorby, 1849) and correlation of cleavage to areas with high strain (Sorby, 1856). Haughton (1856) provided the first mathematical description of length changes in fossils due to strain in naturally deformed rocks, furthermore, he applied the concept of the strain ellipsoid to rock deformation, which established a framework for strain to be quantified and compared.

It was not until the quantitative studies on distorted ooids by Cloos (1947) that truly numerical and methodological strategies were fully applied to strain analysis. By the early 1960's, strain analysis methods were still largely dependent on the presence of strain markers of known initial shape, such as fossils, ooids or reduction spots (Breddin, 1954, 1957; DeSitter, 1964). In 1967, John Ramsay presented a suite of precise and mathematical procedures that allowed for the accurate determination of finite strain in deformed rocks. These methods, though significantly modified, have stood the test of time and are regularly employed. Of the many publications citing Ramsay's *Folding and Fracturing*, a significant number, >1000, have focussed on strain analysis (Lisle, this issue). It is clear that these techniques are still applied to both field studies and mathematical models of rock deformation.

This review starts by highlighting the importance of Ramsay's initial contribution, then we outline the significant advances in the techniques of strain analysis made over the last 50 years. This is followed with a brief discussion on applications of strain analysis and how these techniques have advanced our understanding of natural rock deformation. There is clearly a huge body of research involving strain analysis and it is not possible to reference every application here, but we have highlighted some key developments. We then follow this by providing a discussion of some of the key unresolved problems in the field. We conclude with some ideas for future directions and hope that this will act as a springboard for those investigating strain in rocks for the first time.

Strain Analysis Techniques proposed by Ramsay

The significance of Ramsay's contribution was that he set out in a systematic and mathematical manner techniques for determining strain from objects of known initial shape, and he established methods which allowed populations of objects, such as sedimentary clasts, of non-spherical and fluctuating initial shape, to be used as strain markers. These methods depend on clast orientation, repacking and intraclast deformation of clasts due to deformation. This was a key development in strain analysis, as it allowed estimates to be made from lithologies that did not have obvious or established strain markers (Fig. 1). The methods developed by Ramsay (1967) are briefly outlined below:

Method 1

The first method that Ramsay outlined built on existing techniques at the time, and involved direct measurement of the principal axes of elliptical strain markers and the orientation of their long axes (Ramsay, 1967, p 193). These axes are then plotted against each other (Fig. 2a) and the slope of the best-fit line that also passes through the origin provides an estimate of the strain ratio (Fig. 2b). Ramsay noted it was difficult to accurately identify ellipse lengths in high deformation regimes, and that it was difficult to identify the maximum stretching direction in low strain regimes.

Method 2

The second method (Ramsay, 1967, p 193-194), does not rely on direct measurement of ellipse axes, and accounts for difficulties in methods of identifying the length of maximum ellipse axes. The centre of each ellipse is identified and the lengths of chords from the centre to the edge of each ellipse along three arbitrarily directions are measured. The sum of the chord lengths for the three defined directions for a population of objects is calculated (Fig. 2c). If the objects were initially circular, the ratios of elongation can be calculated for each direction.

Method 3

This method, commonly referred to as the nearest-neighbour or centre-to-centre method, (Ramsay, 1967, p 195-196) was developed to tackle cases where pressure solution was suspected to have occurred, and is applicable to rocks with particles equally or unequally distributed throughout the rock mass. In cases where pressure solution is a significant deformation mechanism, the elliptical shape or preferred orientation of markers is not reliable. This method is particularly useful for identifying cases where non-passive deformation is thought to have occurred (i.e. that the clasts are not deforming homogeneously with the matrix). The basic premise involves measuring the distance between object centres, and assuming that in the unstrained state these distances should be isotropic (Fig. 3a). During deformation the distance between centres should become shorter parallel to the maximum compression axis (Fig. 3b & c).

Method 4

The fourth method (Ramsay, 1967, p 197-199) utilised the measurements of distorted angles of radial and tangential lines in elliptical sections, such as those in spherulites. Whilst an elegant method of calculating strain, this method has had limited use due to the specific nature of the strain markers required.

R_f/\emptyset Method

In addition to the four methods above, Ramsay (1967, p 204-211) also outlined a method for specifically dealing with markers of initial elliptical, the R_f/\emptyset method (Fig. 4), where R_f is the deformed axial ratio of the marker ellipsoid, while \emptyset is the orientation of the long axis. This is slightly more complex than using initially circular objects, in that when an ellipse is deformed under homogeneous conditions, the resulting shape is another ellipse. The axial ratio (R_f) and orientation of the deformed ellipse is a result of the combination of the initial aspect ratio (R_i) and orientation (θ), and the strain

ellipse, all of which are unknowns. When a population of deformed ellipses are considered, variations in their \emptyset values can be related to eccentricity in their orientations prior to deformation.

Measuring strain after Ramsay

Essentially Ramsay (1967) developed methods whereby strain estimates could be made using parameters derived from the following: strain marker orientation, strain marker shape, position of strain marker centres, distance between centres and the angle between centres. The two main types of methods that prevailed were the R_f/\emptyset method and the centre-to-centre. The R_f/\emptyset method (Fig. 4) determines finite strain from randomly oriented populations of deformed elliptical objects, while the centre-to-centre method (Fig. 3) uses the distance between centres of adjacent objects, and assumes the objects were uniformly distributed prior to deformation.

Subsequent to the initial R_f/\emptyset method, alternative methods based on marker shape and orientation were developed (Dunnet, 1969; Elliott, 1970; Dunnet and Siddans, 1971; Matthews et al., 1974; Borradaile, 1976; Shimamoto and Ikeda, 1976; Lisle, 1977a, 1977b, 1985; Robin, 1977; Peach and Lisle, 1979; Siddans, 1980; Yu and Zheng, 1984; Mulchrone and Meere, 2001; Mulchrone et al., 2003). Dunnet (1969) developed an R_f/\emptyset diagram method, while Elliott (1970) applied a similar graphical approach, the shape factor grid. Dunnet and Siddans (1971) took non-random initial orientations into consideration for the R_f/\emptyset diagram method. A significant drawback of these methods is that they are subjective.

An algebraic method that accommodated statistical analysis of any errors produced was introduced by Matthews et al. (1974). The drawback of this method was that the orientation of the principal strain axis needed to be calculated independently prior to using the method. Similarly, Robin (1977) derived a method that allowed analysis of strain markers of any shape but required prior independent knowledge of the principal strain axes. Advances in the R_f/\emptyset method are discussed in further detail by Lisle (1994). In order to address the issues outlined above with calculating strain from distributions of elliptical objects, Shimamoto and Ikeda (1976) developed an objective non-graphical, reproducible

approach to strain analysis. This approach averaged the parameters of all of the marker ellipses to generate one marker ellipse, or if the initial distribution was isotropic, a marker circle. The Mean Radial Length (MRL) method of Mulchrone et al. (2003) took a similar approach, whereby the average shape of a population of isotropic ellipses or non-deformed sedimentary clasts equates to a circle. As this population becomes deformed by either shape change or rotation, this circle becomes an ellipse and can be directly related to the strain ellipse in the same manner that any circular marker can after deformation.

The centre-to-centre family of techniques are based on using object-to-object separation and assume that the distribution of marker objects are isotropic and that after deformation the distance between any marker centre and all other clast centres has been modified. The relative change in clast centres distances can be related to the direction and magnitude of the finite strain ellipse (Ramsay, 1967). Compared to the R_f/ϕ method, the centre-to-centre method involved relatively complicated calculations and was particularly labour intensive. As a result, it initially received significantly less attention than the R_f/ϕ method. This changed when a relatively simple graphical approach was developed by Fry (1979; Hanna and Fry, 1979), which used all object-object separations. This was subsequently further improved as the Normalised Fry Method (Erslev, 1988) and the enhanced Normalised Fry Method (Erslev and Ge, 1990). McNaught (1994) further extended these methods by facilitating the use of non-elliptical markers by determining best-fit ellipses for these irregular shaped objects. One of the drawbacks of the centre-to-centre techniques is that they do not account for volume loss, which can be considerable when pressure solution is a dominant deformation mechanism (Onasch, 1986; Dunne et al., 1990). Furthermore, if pressure solution is significant, there are difficulties in identifying the pre-strain centres of clasts and if significant heterogeneous deformation is present at the clast scale than this can lead to further underestimates of strain.

The Fry methods have been regularly incorporated into automated analysis tools (Ailleres et al., 1995; Launeau and Robin, 1996; Launeau et al., 2010). Despite popularity and ease of use, these methods

are subjective, with interpreter bias being introduced at both the identification of clast centres, and the definition of the central ellipse on the Fry plot. Mulchrone (2003) used Delaunay triangulation to characterise nearest neighbour separations, and defined object centres using the centroid of the best-fit ellipse. This resulted in a more objective and automated process for identifying object centres and creating the tie-lines between nearest neighbours.

Calculating the strain ellipsoid

Most strain analysis techniques focus on quantifying strain in a 2D plane. In order to quantify strain in 3D, a strain ellipsoid needs to be defined. Typically, the strain ellipsoid is defined from strain ellipses on several planar surfaces with differing orientations. Similar to calculating the strain ellipse, calculating the strain ellipsoid is not a trivial process, and numerous attempts have been made at determining the most accurate best-fit ellipsoid. Ramsay (1967; p. 142-147) derived a series of equations to solve for the best-fit ellipsoid from three mutually perpendicular planes. Numerical algorithms were subsequently developed for three orthogonal sections (Shimamoto and Ikeda, 1976; Oertel, 1978). This was followed by methods, which allowed for non-orthogonal sections (Milton, 1980; Gendzwill and Stauffer, 1981; Shao and Wang, 1984; De Paor, 1990). Owens (1984) in particular described an iterative method for the calculation of the best-fit strain ellipsoid from any number of non-perpendicular sections using a least squares approach, as well as applying a scale factor. Robin introduced an approach utilising a series of linear equations (Robin, 2002; Launeau and Robin, 2005). Shan (2008) built on the Robin method, and included added flexibility, whereby stretching lineation data could be included. The important distinction of the Robin and Shan methods from the previous methods was that they were non-iterative but separated the parameters to be calculated from the initial data. Vollmer (2017) has provided a more detailed comparison of the Robin and Shan methods, as well as applying bootstrap statistics to the results. Mookerjee and Nickleach (2011) presented a suite of methods in Mathematica, which attempts to minimise the errors between the best-fit ellipsoid and any of the measured planes used as input data.

The geometries of strain ellipsoids can be represented in 2D space using a Flinn Plot (Flinn, 1956, 1962, 1965). This type of plot was first used to compare the elliptical properties of clast populations in conglomerates (Zingg, 1935). The ratio of the maximum to intermediate ellipsoid axes (R_X/Y) is plotted as ordinate and the ratio of the minimum to intermediate axes (R_Y/Z) is plotted as abscissa on these graphs. The Flinn Plot was subsequently modified by Ramsay (1967) to include a logarithmic scale (Fig. 5; discussed further in Hobbs et al., 1976; Ramsay and Huber, 1983). The benefit of the logarithmic Flinn Plot is that it provides a more even distribution of points with increase in deformation (Ramsay and Huber, 1983), whilst in the original Flinn Plot low strains are clustered near the origin, making it difficult to interpret data.

The symmetry of the strain ellipsoid can be described by the ratio $K ((X/Y)/(Y/Z))$. If $K > 1$ then the ellipsoid is considered to have a prolate or axial symmetric constriction and has one long axis and two shorter axes. If $K < 1$ the ellipsoid is considered to be oblate or axially symmetrically flattened and has two long axes and one shorter axis. Between these two fields of flattening and constriction is the field of plane strain ($K=1$) and which only occurs when strain is acting in the XZ plane. K represents the slope of a line from the data point to the origin at (1,1), so that $K=a-1/b-1$ with $a=x/y$ and $b=y/z$. K on the diagram can define a series of domains, so that when $K=0$ the finite strain ellipsoid is uniaxial oblate and has been flattened perpendicular to Z . As K tends towards 1 the ellipsoid moves away from being purely uniaxial, but remains in the oblate and flattened domain. For K values greater than 1 the ellipsoid lies in the prolate or constrictive domain, and for $K=\infty$ the ellipsoid is purely uniaxial prolate and stretched along the X axis (Park, 1997). The degree of how far removed the ellipsoid is from spherical (ellipsoid eccentricity) is calculated as $\sqrt{((X/Y)^2 + (Y/Z)^2)}$.

A less-popular alternative to the Flinn Plot, the Nadai-Hsu Plot (Fig. 5; Nadai, 1950; Hsu, 1966) was first applied to geological strain analysis by Hossack (1968). This type of plot presents strain in a polar area, and is argued to provide a less distorted representation of the deviatoric strains (Hobbs et al.,

1976; Brandon, 1995; Mookerjee and Peek, 2014). Another advantage of this type of polar plot is that ellipsoids with low strain ratios plot closer together regardless of the ellipsoid shape. Ramsay and Huber (1983) criticised the Nadai-Hsu plots, irrotational strain is assumed, while most natural deformation involves progressive non-coaxial rotational strains.

The fundamental difference is that the Nadai-Hsu Plots use the *amount of strain* (ϵ_s) and Lode's Ratio (v), to define the ellipsoid shape (Lode, 1926). The *amount of strain*, is related to the octahedral shear, Y_o , and is defined by: $\epsilon_s = (\sqrt{3} / 2) Y_o$, where $Y_o = (2/3) [(\epsilon_1 - \epsilon_2)^2 + (\epsilon_2 - \epsilon_3)^2 + (\epsilon_3 - \epsilon_1)^2]^{1/2}$ and ϵ_1 , ϵ_2 and ϵ_3 represent the strain axes. The Lode Ratio is defined as $v = (2\epsilon_2 - \epsilon_1 - \epsilon_3) / (\epsilon_1 - \epsilon_3)$ and ranges from -1 to 1. Lode ratios of -1 define a prolate ellipsoid, while 1 and 0, define an oblate and plane strain ellipsoid respectively. Whereas the Flinn Plot solely relies on the aspect ratios of the strain ellipsoid (as discussed above). For a more in depth discussion of the merits of each method readers are referred to Mookerjee and Peek (2014) and Vollmer (2017).

Automation

Possibly one of the biggest drawbacks to most strain analysis studies is the high labour intensity required for both the identification of object boundaries, and the accurate identification of their centres for enough objects to create a statistically robust sample set. Since the late seventies, many attempts have been made at automating strain or fabric analysis to address this (e.g., Peach and Lisle, 1979). Initially, the limiting steps in the automation of these strain analysis techniques was the recognition and fitting of best-fit ellipses to geological strain markers, such as sedimentary clasts (Fig. 6a & b).

The efficient and accurate automatic segmentation of thin section images is still a developing field and has received a lot of recent attention with numerous attempts at automated extraction using image processing or GIS-based techniques (e.g., Goodchild and Fueten, 1998; Heilbronner, 2000; van den Berg et al., 2002; Perring et al., 2004; Barraud, 2006; Choudhury et al., 2006; Li et al., 2008; Tarquini and Favalli, 2010; DeVasto et al., 2012; Gorsevski et al., 2012; Heilbronner and Barrett 2013;

Mingireanov Filho et al., 2013; Jungmann et al., 2014; Asmussen et al., 2015). Although these methods produce rapid grain boundary maps, they are typically inaccurate or achieve different results depending on the nature of the image. This is highlighted by the regular use of quartz clasts as strain markers, whereby the automatic identification of their boundaries is complicated by undulose extinction, deformation bands, diffuse boundaries and colour similarities between neighbouring grains. Despite these advances, most methods follow the approach of Mukul (1998), whereby grains used as strain markers are manually traced, and then analysed using image analysis software.

A number of methods for automated image analysis have been successfully utilised in the past for geological strain analysis (Ailleres et al., 1995; Erslev and Ge, 1990; Masuda et al., 1991; McNaught, 1994; Heilbronner and Barrett, 2013). Panozzo (1984) utilised digitised sets of points representing linear or elliptical objects in her projection method. Mulchrone et al. (2005) developed a parameter extraction program (SAPE) that rapidly extracts the required data by using a simple region-growing algorithm to identify regions of interest. Vollmer developed a similar method, Ellipsefit (Vollmer, 2010, 2011, 2017). Many of these techniques are discussed in Heilbronner and Barrett (2013), who have provided a superb overview of image analysis techniques for geological material and it is recommended as a starting point for readers interested in this field.

Once grain boundaries have been identified and ellipses are fitted to clasts, the parameters required for a range of strain analysis techniques such as the aspect ratio, orientation, and the centroid of the object can now be easily extracted. For the R_f/ϕ method the difficulties in calculating a strain estimate cease once ellipses have been fitted to strain markers; for the centre-to-centre methods the difficulties continue.

The accuracy of centre-to-centre strain estimates can be further hampered by the ability to clearly define the vacancy field or central void of the Fry Plot (Fig. 6c), which in a strained sample should represent the strain ellipse (Crespi, 1986; Waldron and Wallace, 2007). A variety of techniques have been applied in order to accurately and objectively define this void (Erslev and Ge, 1990; McNaught,

1994; Waldron and Wallace, 2007; Lisle, 2010; Shan and Xiao, 2011; Reddy and Srivastava, 2012; Mulchrone, 2013). Similar problems exist for defining the curve of the polar plot (Mulchrone, 2013).

In order to reduce the time and labour intensity required, Mulchrone et al. (2013) integrated image analysis, ellipse fitting and parameter extraction, and strain analysis routines for MRL and DTNNM in one workflow. They also included a method for bootstrapping the results in order to produce uncertainty estimates (Fig. 6 e&f). Kumar et al. (2014) carried out a detailed comparison analyses on these methods, and found that the Delaunay Triangulation Method of Mulchrone (2013) and the Continuous Function Method of Waldron and Wallace (2007) were the most accurate. Additionally they concluded that the Delaunay Triangulation Method and the image analysis technique of Reddy and Srivastava (2012) were the most time efficient.

The other method that has stood out is the SURFOR method, first presented by Panozzo (1984, 1987), and discussed in detail in Heilbronner and Barrett (2013). The SURFOR method takes a slightly different approach to fabric or strain analysis compared to the Ramsay family of methods. Rather than focussing on the object orientation or the spatial relationship between objects, the SURFOR method quantifies the fabric based on the shape, size and orientation of 'surfaces' (Heilbronner and Barrett, 2013). The 'surfaces' can be any linear element, such as fractures or grain boundaries. One particular advantage of the SURFOR method over the original Ramsay R_f/ϕ method is that it accounts for marker size, with smaller objects having less of an impact on the final strain/anisotropy estimate. A similar approach is taken by Launeau et al. (1990, 1996, 2010), whereby linear filters are used to count intercepts along any arbitrary direction of a digital image. The intercepts technique has shown to be comparable to the MRL and the DTNNM methods in moderate strain regimes, although in low strain regimes there appears to be a discrepancy between the methods (McCarthy et al., 2015). These discrepancies are due to uncertainties in strain estimates in low strain regimes.

Application of strain analysis and advances in strain theory

This contribution has focussed on the significant advances made in geological strain analysis, as outlined above, which have provided a number of valuable insights into geological deformation. Unfortunately, natural deformation is rarely simple or restricted to 2D planes, yet this approach have aided with understanding of complex deformations.

Strain analysis and resulting knowledge of the finite strain state of a point in a rock mass has played a fundamental part in the understanding of the development of tectonic fabrics and foliations (Ramsay and Wood, 1973, Tullis and Wood, 1975). However, nature tends to reveal more by capturing change in strain through time and space, (e.g. porphyroclasts and related structures, layers which are shortened and then stretched, and regions of intense shear where the continuum from low to high strain can be spatially traced). Often the spatial changes can be interpreted as reflecting the temporal deformation history. Ramsay (1967) applied the concept of infinitesimal strain together with that of finite strain to understand deformation history, with the difference between what happens in a short time step compared to that over long time periods helped develop the ideas of progressive strain. This infinitesimal approach was followed by the seminal work of Means et al. (1980) who considered the velocity gradient tensor to conceptualise progressive deformation, and used vorticity to quantify rotational deformation. A detailed discussion of vorticity is beyond the scope of this contribution, and interested readers should consult the work of Fossen and Tikoff (Fossen and Tikoff, 1993; Tikoff and Fossen, 1993; Tikoff and Fossen, 1995; Tikoff and Fossen, 1999; Passchier and Trouw, 2005).

Many of the 2D finite strain methods discussed in previous sections have a natural extension to 3D, but there is still a dearth of 3D strain studies. Methods based on shape (e.g. Shimamoto and Ikeda, 1976; Mulchrone et al., 2003) and inter-object relationships (e.g. Fry, 1979; Mulchrone, 2013) can be readily developed into 3D methods. However, in many cases the primary difficulty rests with acquiring suitable data in 3D in order to apply the methods. Recent technological advances have seen the application of tomography to the acquisition of high quality images of 3D markers in rocks (Louis et al,

2006; Adam et al, 2013; Robin and Charles, 2015). This is certain to be an area of future development and will inform finite strain studies and their interpretation in the context of 3D deformation history (Tikoff and Fossen, 1999).

Important comparisons have been made between clast-based strain analyses and other methods of quantifying deformation. A number of studies in the seventies and eighties highlighted a close relationship between finite strain estimates and quartz crystallographic fabrics (Marjoribanks, 1976; Miller and Christie, 1981; Lisle, 1985; Law, 1986). Rapid developments in techniques such as Electron Back Scatter Diffraction (EBSD) have largely confirmed this relationship, but also provided insights into deformation at subgrain scales one of the most prominent methods for the determination of preferred orientation of minerals in thin sections (Passchier and Trouw, 2005; Prior et al., 2009).

Similar advances in rock deformation studies have been made in the field of Anisotropy of Magnetic Susceptibility (AMS), with Graham (1954) first suggesting that magnetic fabrics could be a valuable tool in petrofabric analysis and establishing a link between layer parallel shortening and AMS. Since this pioneering study there has been a huge volume of work confirming the ability of AMS to determine the orientation-distribution of all minerals and all subfabrics in a specimen, with comprehensive reviews provided by Borradaile and Henry (1997) and Borradaile and Jackson (2010). In direct comparisons of AMS to strain analysis techniques, AMS has been shown to be a highly sensitive and rapid method for quantifying tectonic fabrics (Burmeister et al., 2009; Weil and Yonkee, 2009; McCarthy et al., 2015).

Other significant contributions of strain analysis includes providing accurate information for structural restorations. Compaction and stratigraphic thickening due to deformation can be estimated and incorporated in the construction of balanced cross sections (Woodward et al., 1986; Protzman and Mitra, 1990; Mitra, 1994). Despite Layer Parallel Shortening (LPS) or internal deformation (compaction, collapse of pore space, dissolution or cleavage formation) being shown to accommodate significant shortening in balanced cross sections from carbonate duplexes (27%; Cooper et al., 1983),

gravity driven thrust systems (18-25%; Butler and Paton, 2010), and analogue models (15-30%; Koyi et al., 2004; Burberry, 2015; Lathrop and Burberry, 2017), strain analysis techniques are rarely applied to balancing cross sections.

Unresolved issues in strain analysis

Hobbs and Talbot (1966) highlighted a few of the limitations of strain analysis a year before Ramsay published his seminal text, and the majority of these seem to prevail today: the initial shapes of many strain markers cannot be measured accurately enough to yield highly accurate estimates; and homogeneous strain is typically assumed. Although these assumptions still prevail, they have largely been accepted to be unresolved. In addition to this, a number of factors add further uncertainty to any strain estimate including: strength and influence of the primary or pre-strain fabric; effects of non-passive strain; and the effects of volume-change, these are discussed below.

Primary fabrics

The largest problem for strain analysis methods is the uncertainty regarding the strength and orientation of an initial primary fabric. Most strain analysis methods, particularly the R_f/ϕ family of techniques, rely on the assumption that the strain markers have a random initial orientation. Certainly in the case of sedimentary rocks this is rarely true, as most sediments develop a preferred orientation either due to depositional processes or diagenesis (Elliott, 1970; Dunnet and Siddans, 1971; Boulter, 1976; Seymour and Boulter, 1979; De Paor, 1980; Holst, 1982; Paterson and Yu, 1994; Maffione and Morris, 2017).

In a study of undeformed lithologies Holst (1982) found that sections not parallel with bedding had a preferred orientation of clasts along the trace of the bedding plane, while sections parallel to bedding typically had no preferred orientation of clasts. Even if an isotropic or random depositional fabric existed, a preferred orientation typically develops during diagenesis and compaction through active or partly rigid body rotation (Borradaile, 1987). Several efforts have been made to remove the effects

of primary fabrics on strain estimates (Elliott, 1970; Dunnet and Siddans, 1971; Matthews et al., 1974; Shimamoto and Ikeda, 1976; Lisle, 1977a; Seymour and Boulter, 1979; Holst, 1982; Wheeler, 1986; DePaor, 1988). Unfortunately, most of these methods utilise one or more of the above assumptions and/or assume the existence of independent information concerning the strain ellipsoid. Some of these assumptions regarding the primary fabrics of sedimentary rocks were highlighted by Patterson and Yu (1994) and include the following: individual grains are spherical prior to straining; orientations and shapes of grain populations define spherical, pre-strain fabric ellipsoids (i.e. grains have an initial uniform distribution); pre-strain fabric ellipsoids are symmetric around bedding; and initial fabrics are recognisable even after straining.

Failing to account for any of these factors can lead to considerable errors in strain estimates, particularly in domains with relatively low strains ($R < 1.5$). To account for these errors Patterson and Yu (1994) suggested that a correction should be applied by multiplying the estimated strain ellipsoid by an average pre-strain ellipsoid. Unfortunately, information regarding the magnitude and orientation of the pre-strain ellipsoid is rarely available. Paterson and Yu (1994) compiled XYZ averages for a range of rock types, but this is a limited data set and should be expanded. Regarding the orientation, the estimated strain ellipsoid can be multiplied by the reciprocal pre-strain ellipsoid multiple times in numerous orientations to create an error bracket. Ramsay (1967) showed that all possible combinations of two ellipsoids result in an approximate triangular region on a Flinn plot. Following the methodology of Paterson and Yu (1994), this triangular region is then representative of the error bars of the strain estimate.

Non-passive deformation

A key assumption of most current strain analysis techniques is that strain is homogenous and that markers behave in a wholly passive manner in relation to their host material. This breaks down in most natural materials especially when sedimentary clasts are used for strain analysis.

371 Clearly, the most ideal strain markers are those that were originally spherical, which were then
372 deformed passively with no competency contrast between the marker and the host rock. If this holds
373 true then the final shape of the marker will reflect that of the finite strain ellipsoid (Ramsay, 1967).
374 The fundamental assumption of most strain analysis methods is that there is no competency or
375 ductility contrast between the markers and their matrix/host rock, so that the marker and surrounding
376 rock matrix responded to deformation identically. Unfortunately, clasts and their surrounding matrix
377 rarely deform in a passive manner, due to competency or ductility contrasts between the marker and
378 the host rock. This competency contrast is inherently linked to the viscosity contrast between different
379 clast types and the matrix (Ramsay, 1967; Gay, 1968a,b, 1969; Lisle, 1985b; Freeman, 1987; Freeman
380 and Lisle, 1987; Treagus, 2002; Mulchrone and Walsh, 2006; Czeck et al., 2009). Gay (1968a) pointed
381 out that clasts with a low viscosity deform faster than the bulk rock strain ellipse, while clasts with
382 high viscosities resisted deformation and deformed slower than the bulk rock strain ellipse. Gay
383 (1968a) also noted that the viscosity ratio between a clast and the matrix is dependent on the relative
384 proportion of clasts and matrix. Freeman and Lisle (1987) confirmed that the errors in strain estimates
385 are higher when the clasts represent a small fraction of the bulk rock. This is driven by the high ductility
386 contrast, whereby the majority of strain is accommodated by the weaker matrix. As the clast-to-matrix
387 ratio increases the ductility contrast reduces, potentially caused by the reduced ability of the matrix
388 to flow due to the increase in clast on clast interaction. This separation of strain behaviour between
389 the matrix and clasts is typically termed strain partitioning. This type of behaviour is largely controlled
390 by object concentration and the degree of packing and clast interaction, due to the effect these have
391 on the viscosity contrasts (Gay, 1968a; Lisle et al., 1983; Mandal et al., 2003; Vitale and Mazzoli, 2005).
392 Generally, lithologies with higher object concentrations display reduced effects of strain partitioning,
393 leading to more accurate strain estimates (Mandal et al., 2003; Vitale and Mazzoli, 2005).

394 While reviewing problems arising from these competency contrasts, Treagus and Treagus (2002)
395 concluded that conglomerates as a whole deformed at an approximately constant viscosity in a
396 linearly viscous manner, but also found that R_f/ϕ style methods characterised clast strain whereas the

centre-to-centre methods were more effective at characterising bulk rock strain. This is in part due to two factors: clasts typically only represent 50-70% of the bulk rock (Leeder, 1982); and the R_f/ϕ methods only consider clast shape and orientation, while centre-to-centre techniques account for distances between the clasts.

This non-passive deformation can be accounted for by utilising centre-to-centre methods, which include spatial information in the estimates of strain, and provide bulk-rock strain estimates that are closer to true strain values. This has been illustrated in a range of natural settings (Meere et al., 2008, Soares and Dias, 2015). Meere et al. (2008) attributed non-passive deformation to the presence of a relatively incompetent clay-rich matrix, which effectively cushioned clasts from internal deformation. This type of behaviour allows for high degrees of competent clast long-axis alignment achieved by a combination of rigid body rotation, layer boundary slip and particle–particle interactions, with minimal evidence of penetrative deformation, despite evidence from traditional strain markers such as reduction spots and deformed burrows (Meere et al., 2008). In these situations, using the R_f/ϕ methods leads to a significant underestimate of strain. More recently, Meere et al. (2016) highlighted the importance of identifying passive clast behaviour and the potential for deformation prior to lithification in understanding the deformation history of a region.

415 Most studies applying the strain analysis techniques discussed, do not account for any potential
416 volume change of the markers. Although Ramsay (1967) had already presented a modified Flinn
417 diagram, which was capable of including some aspect of volume loss, this aspect of strain analysis is
418 typically ignored. Clearly natural deformation rarely occurs in a closed system, and many attempts
419 have been made at estimating volume reduction during deformation, as opposed to diagenetic
420 volume loss. For example, there has been considerable debate regarding the amount of volume loss
421 in slate belts. Sorby (1856) initially suggested that a 50% volume reduction could occur in slates, but
422 settled on ~11% (1908). Wright and Platt (1982) suggested a volume loss of 50% in the Martinsburg
423 Shale of West Virginia. Similar volume reductions were suggested in the Taconic Slate Belt (Goldstein
424 et al., 1995, 1998). Onasch (1994) suggested a range of volume loss of 14-35% in deformed quartz
425 arenites. Similarly, Markley and Wojtal (1996) suggested 10-15% volume loss in an Appalachian mixed
426 siliciclastic sequence. Mosher (1987) analysed the variation in sizes of cobbles in the Purgatory
427 Conglomerate, Rhode Island, and suggested that there could be a volume loss of 23-55% of the original
428 cobble volumes in the areas of most intense deformation.

429 Despite these reports of significant volume reduction, these large volumes are rarely confirmed by
430 geochemical analyses (Wintsch et al., 1991; Erslev and Ward, 1994; Tan et al., 1995). Similarly, Ramsay
431 and Wood (1973) considered that a 10-20% volume reduction could occur based on density
432 differences between lithified mudstones and slates, and argued that greater volume losses were likely
433 to only occur in the deformation of incompletely consolidated sediments. As discussed earlier
434 shortening values of this magnitude have been identified by in a range of settings (e.g., Cooper et al.,
435 1983; Butler and Paton, 2010; Lathrop & Burberry, 2017).

436 While volume change has been mathematically incorporated into strain analysis (Gratier, 1983;
437 Onasch and Davis, 1988; Baird and Hudleston, 2007), most rocks lack the necessary strain markers for
438 this type of analysis. Some success has been made using isocon diagrams (Grant, 1986), but these are

typically restricted to discrete shear zones (Srivastava et al., 1995; Bhattacharyya and Hudleston, 2001; Baird and Hudleston, 2007). Other successes in identifying volume loss has come from gravity driven fold and thrust belts, where the amount of extension high on the slope can be compared to the amount of compression towards the toe of the slope (Butler and Paton, 2010).

Conclusions

Determining finite strain has seen significant developments since the seminal contribution of John Ramsay. Through advances in imaging and software, it is easier than ever before to collect large data sets and apply multiple strain analysis techniques rapidly, and there are a number of methods which can incorporate statistical handling of the results. Strain analysis is regularly incorporated into structural studies employing anisotropy of magnetic susceptibility, electron backscatter diffraction, x-ray tomography, microstructural analysis etc., which have not only led to advances in our knowledge of rock deformation processes, but also regional scale understanding. It should be obvious that detailed strain analysis studies are required to understand the spatial variations of strain in deformed terranes, but also the significance of those variations.

Of the many advances outlined here, most of them have been driven by developments in computing, automation and statistical methods, whilst the basis for these strain analysis techniques have by in large remained the same, which is a testament to the initial contribution of Ramsay. We anticipate that the next significant advances in this field will again be largely technologically driven. In particular, 3D imaging of strain markers and 3D strain analysis should become more widespread, and perhaps developed into 4D. Although, there have been advances in applying micro-tomography to geological materials, these techniques are yet to be applied to strain analysis. There is also scope for advances to be made in the extraction of high quality data from images with minimum human intervention e.g., grain boundary identification, and machine learning techniques could be applied to this. The natural optical heterogeneity of geological materials, even in single mineral phases such as quartz due to impurities, inclusions and microstructural features, will always makes the automation of grain

464 identification challenging. Increasingly the use of non-destructive chemical mapping techniques, for
465 example using electron microscope energy-dispersive X-Ray spectroscopy (QEMSCAN) or Raman
466 spectroscopy, produces outputs that allow the user to filter this heterogeneity thereby making the
467 process of grain boundary identification more manageable. This, coupled with new machine learning
468 techniques, will likely develop into a fully automated process for data acquisition, with strain analysis
469 studies becoming fully automated and significantly more efficient.

470 Regardless of any future developments, it should be clear that the strain analysis techniques of
471 Ramsay and their modernised equivalents should have a place in every structural geologist's toolbox.

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825 **Figure Captions**

826 Fig. 1 Identifying strain in rocks. A. A highly idealised rock outcrop with three exposed mutually
827 perpendicular surfaces, with appropriate strain markers on each surface. The strain ellipsoid illustrates
828 the relationship between the tectonic stretching axes XYZ and sigma 1, 2 & 3. B. A real outcrop from
829 the Dingle Peninsula, which presents a more challenging problem for identifying and quantifying
830 strain.

831 Fig. 2 A. Measuring the long (M) and short (m) axes of elliptical strain markers. B. Plot of the long and
832 short axes from A. The slope of a best-fit line that passes through the points and the origin provides
833 an estimate of the strain ratio. C. Measuring chords along three defined directions for a population of
834 ellipses.

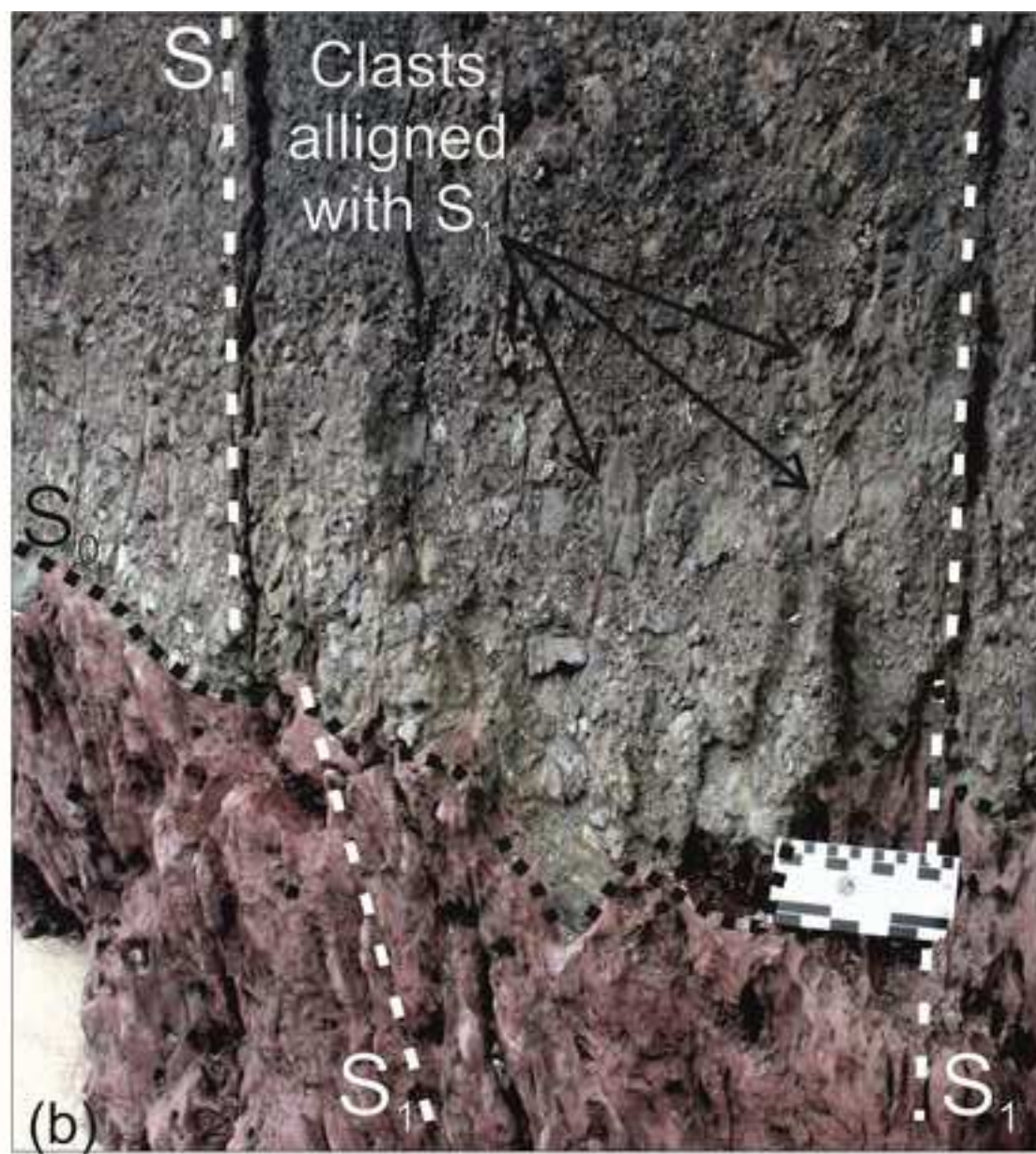
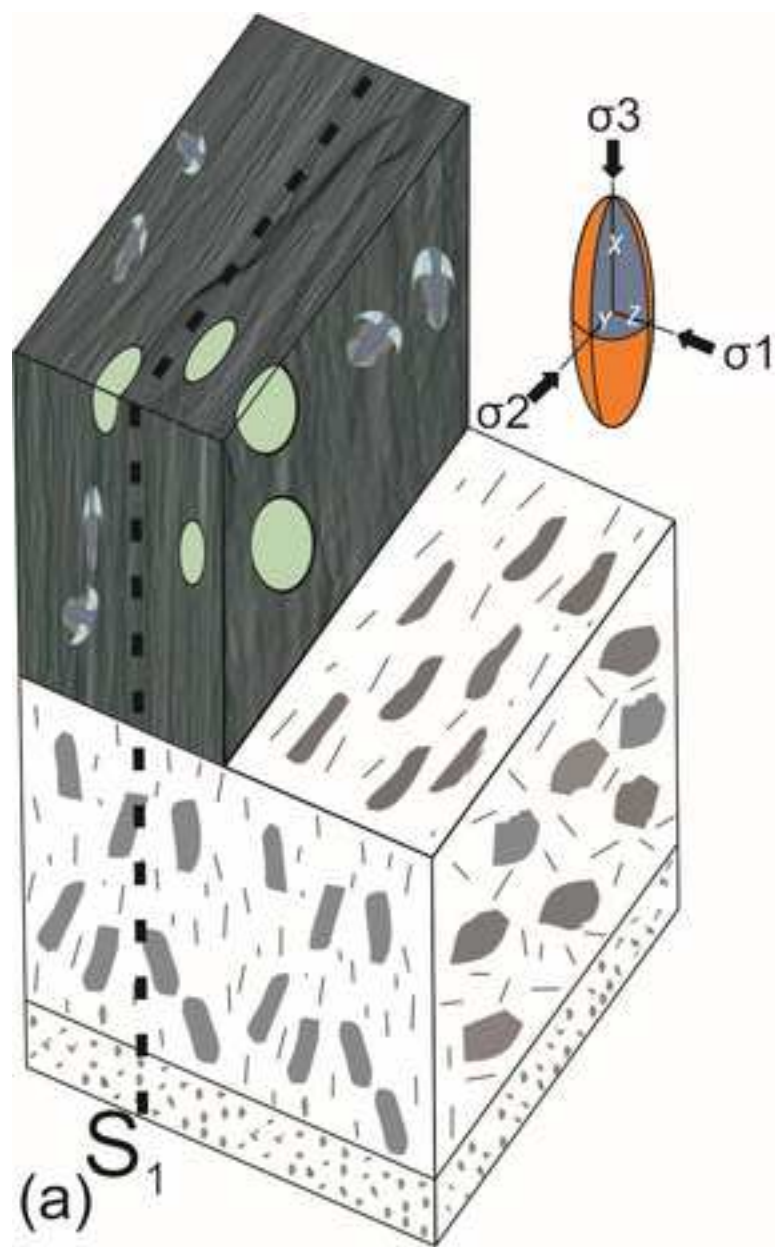
835 Fig. 3 Nearest-neighbour and or centre-to-centre methodology. A. Centre to centre techniques are
836 based on the assumption that the tie-lines between nearest neighbours have a uniformly random
837 distribution in the unstrained state. The lengths, d, and orientations, α , of tie lines joining object
838 centres are marked. The Polar plot of the unstrained state is illustrated below, showing d vs α .
839 Interestingly, this unstrained sample has a weak preferred distribution, in that the clasts are closer
840 together in the vertical direction than the horizontal direction. B. Initial strained state, the distances
841 between clasts become shorter in the tectonic shortening direction. The polar plot indicates higher
842 strain estimates. The apex of the curve shows the orientation of the longest direction and the nadir
843 shows the orientation of the shortest direction. C. The final strain state with pressure solution and a
844 higher strain estimate.

845 Fig. 4 The R_f/ϕ method. A. After fitting ellipses to strain markers, the ratio of the long axis to short
846 axis is calculated and the orientation relative to a reference angle is recorded. B. These ratios are then
847 plotted against the orientation of the long axis. This limited data set suggests that preferred
848 orientation is between 45 degrees and 75 degrees. Clearly more data is required to more accurately
849 estimate strain.

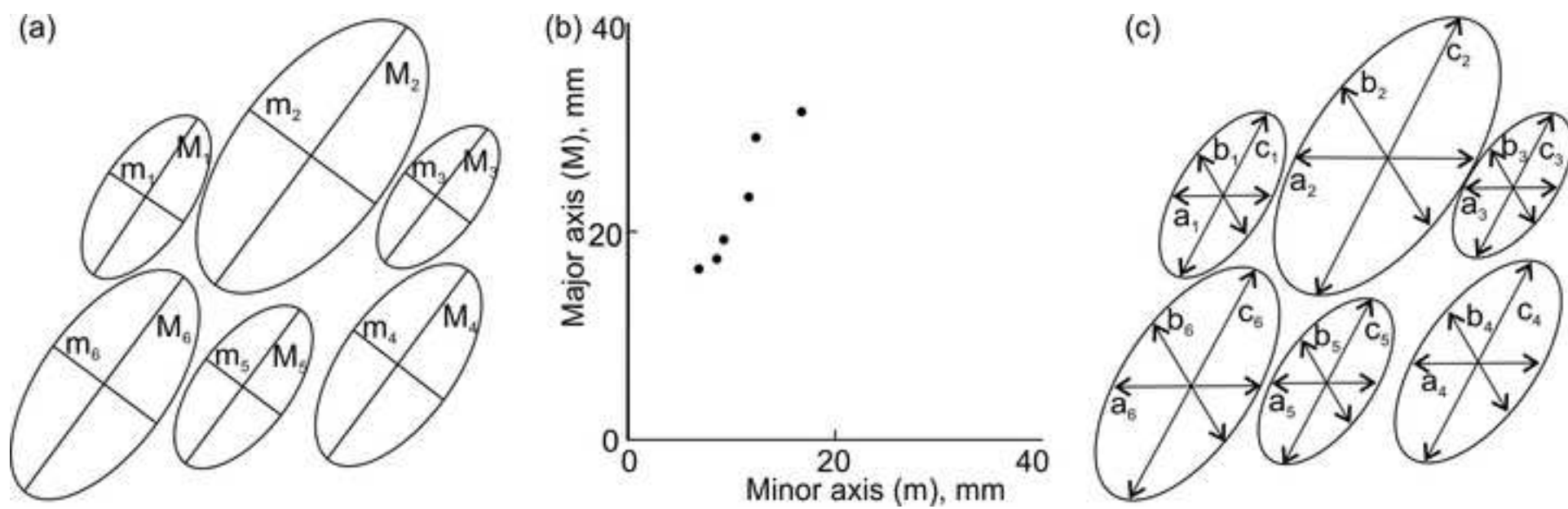
850 Fig. 5. Flinn and Nadai-Hsu plots. A. Flinn plots represent all possible ellipsoid geometries in a 2D space.
851 The standard convention is to use a logarithmic plot, where the ratio of the maximum to intermediate
852 ellipsoid axes ($\ln X/Y$) is plotted as ordinate and the ratio of the minimum to intermediate axes (\ln
853 Y/Z) is plotted as abscissa. Prolate spheroids plot along the vertical axis and oblate spheroids plot along
854 the horizontal. As these ellipsoids become less spherical, they plot further away from the origin. B.
855 Nadai-Hsu plots show similar information to the Flinn Plots, but have an advantage that less deformed
856 ellipsoids plot closer together regardless of shape.

857 Fig. 6. Typical strain analysis methodology. A. Selection of a suitable oriented thin section. B. Fitting
858 ellipses to the clasts shown in A. C. Fitting the central void of the Fry Plot. D. The same data is
859 presented in a polar plot. E. Strain estimate from the DTNNM method represented by the black star.
860 The shaded ellipses represent the Bootstrapped confidence intervals. F. Strain estimate from the MRL
861 method represented by the black star. The shaded ellipses represent the Bootstrapped confidence
862 intervals. Note the underestimate compared to the DTNNM method.

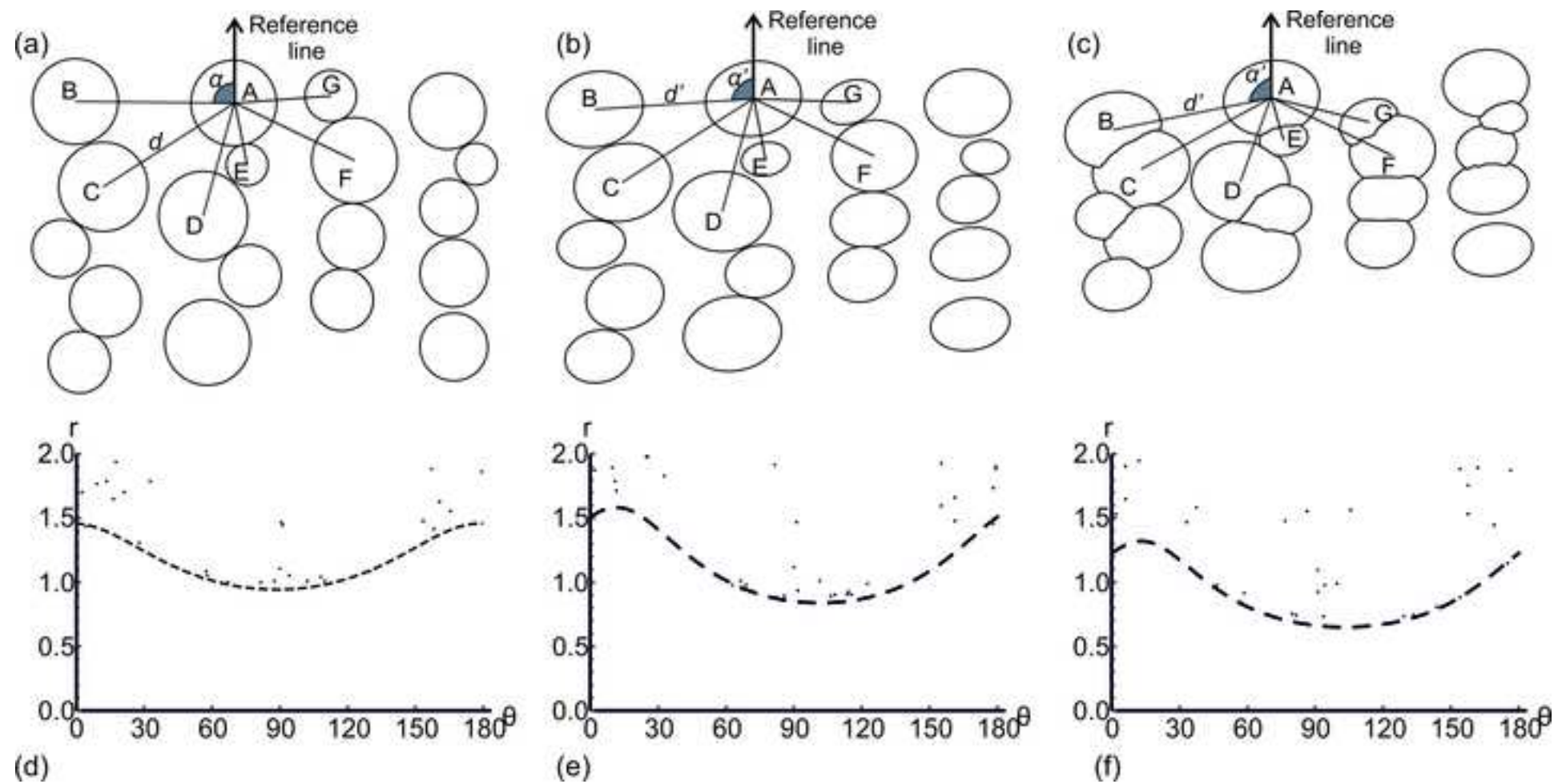
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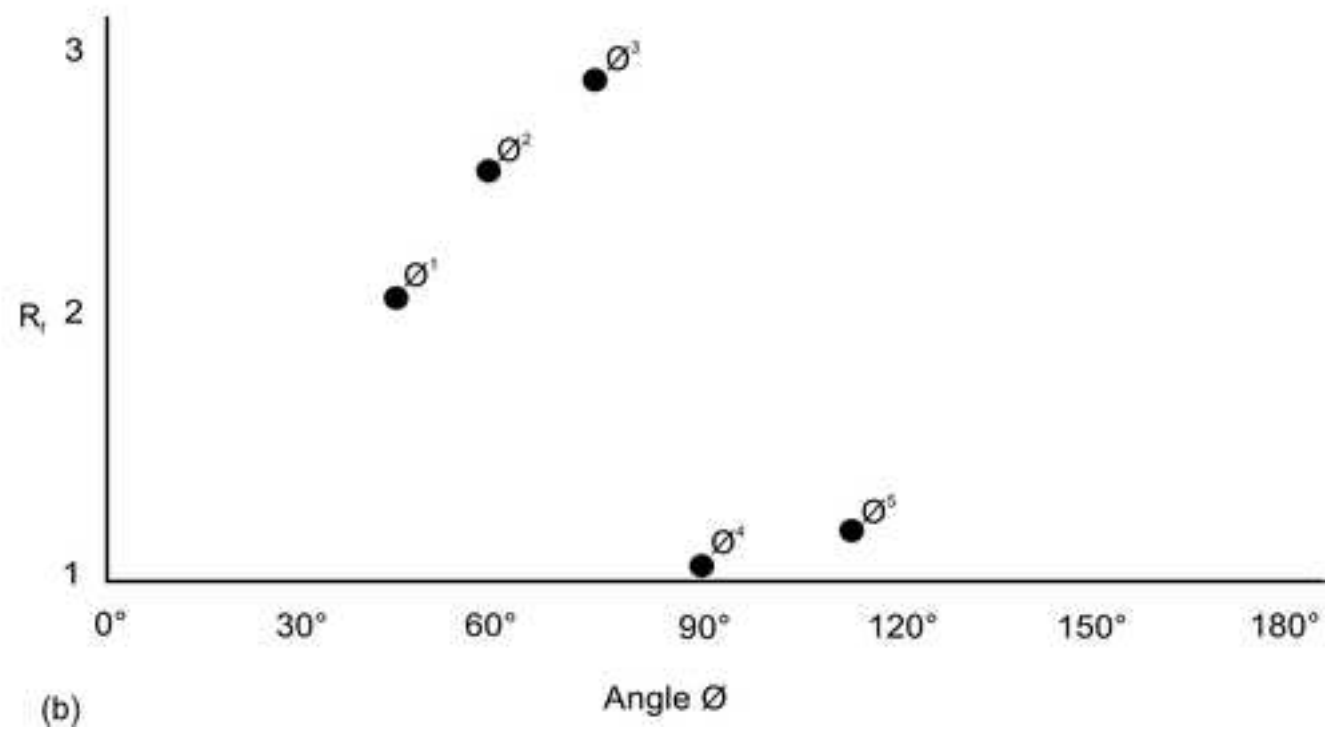
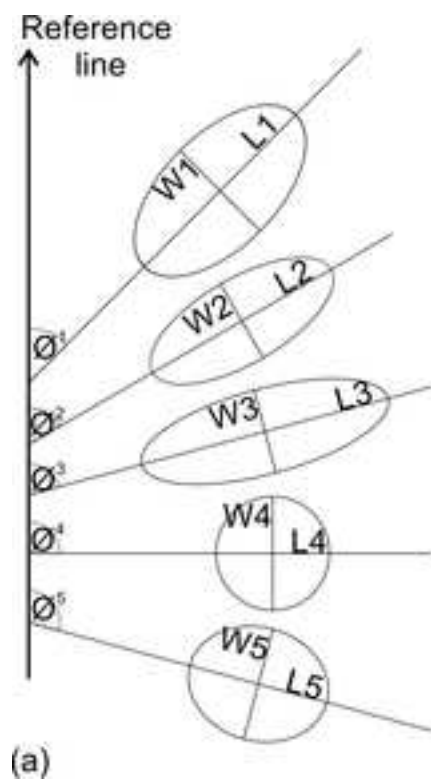
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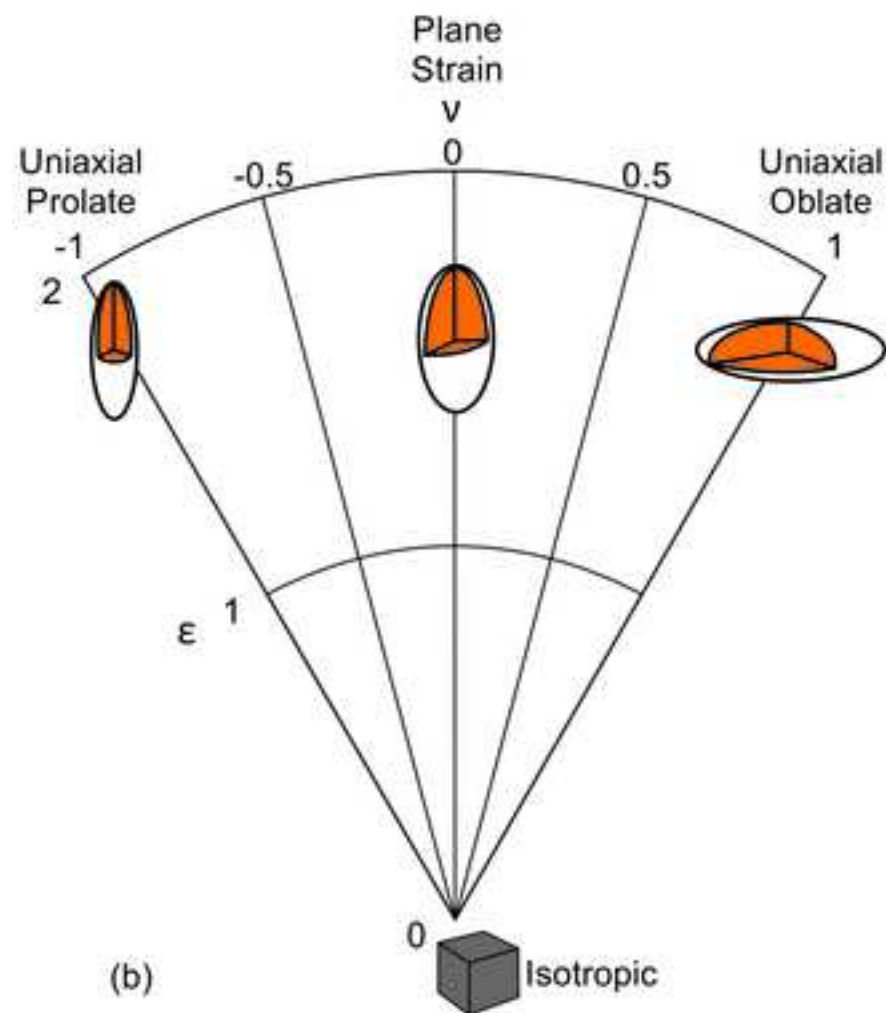
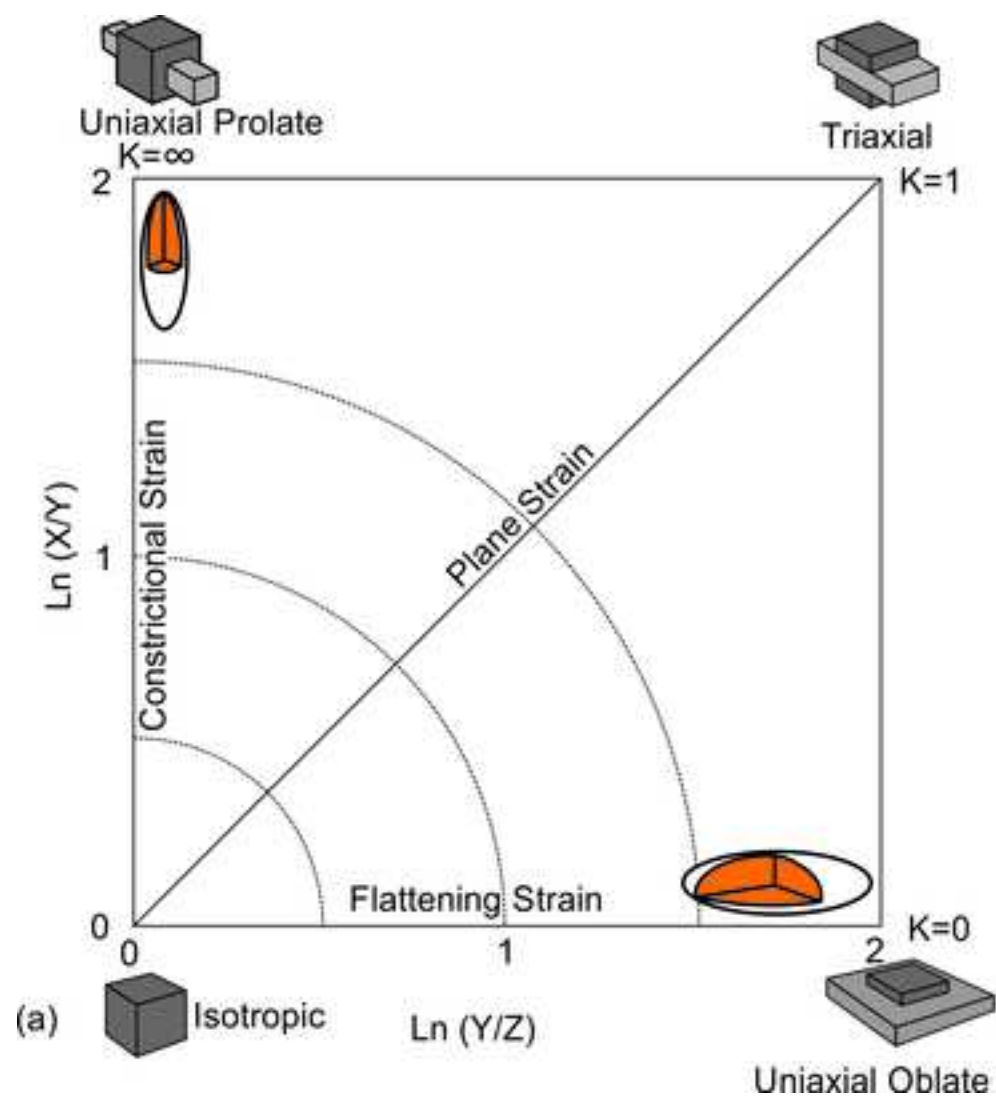
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