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# Surface Quality and Surface Waves on Subwavelength-structured Silver Films

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We analyse the physical-chemical surface properties of single-slit, single-groove subwavelength-structured silver films with high-resolution transmission electron microscopy (TEM) and calculate exact solutions to Maxwell's equations corresponding to recent far-field interferometry experiments using these structures. Contrary to a recent suggestion the surface analysis shows that the silver films are free of detectable contaminants. The finite-difference-time-domain (FDTD) calculations, in excellent agreement with experiment, show a rapid fringe amplitude decrease in the near-zone (slit-groove distance out to 3-4 wavelengths). Extrapolation to slit-groove distances beyond the near-zone shows that the surface wave evolves to the expected bound surface plasmon polariton (SPP). Fourier analysis of these results indicates the presence of a *distribution* of transient, evanescent modes around the SPP that dephase and dissipate as the surface wave evolves from the near to far zone.

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The optical response of subwavelength-structured metallic films has enjoyed a resurgence of interest in the past few years due to the quest for an all-optical solution to the inexorable drive for ever-smaller, denser integrated devices operating at ever-higher band width. Two basic questions motivate research in this field: how to confine micron-sized light waves to subwavelength dimensions [2] and how to transmit this light without unacceptable loss over at least tens of microns [3, 4]. Although surface waves and in particular periodic arrays of surface plasmon polaritons have received a great deal of attention as promising vehicles for subwavelength light confinement and transport, detailed understanding of their generation and early time evolution (within the first few wave periods) in and on real metal films is still not complete [5–8]. Recent measurements [1, 9] of far-field interference fringes arising from surface wave generation in single slit-groove structures on silver films have characterized the amplitude, wavelength and phase of the surface waves. After a rapid amplitude decrease within the first three microns from the generating groove, waves persisting with near-constant amplitude over tens of microns were observed. Such long-range transport is the signature of a "guided mode" SPP, but the measured wavelength

was found to be markedly shorter than the expectation from conventional theory [10]. One possible reason advanced for the disparity between experiment and theory was the presence of an oxide or sulfide dielectric layer on the silver surface, and it has been suggested [11] that an 11 nm layer of silver sulfide would bring experiment and theory into agreement. We report here the results of two investigations: one experimental, into the physical-chemical surface properties of the silver structures and the other theoretical, into the calculated optical response of the silver slit-groove structures using the FDTD technique to numerically solve Maxwell's equations. These studies show no evidence of oxide or sulfide layers on the silver surface and the numerical solutions to Maxwell's equations show not only good agreement with measurements reported in [1] but also point to the important role played by short-range evanescent components in the early time evolution of the surface wave.

Three typical structured samples were chosen for examination with fabrication dates of about 12 months, 6 months, and 1 week from the date of the TEM analysis. The structures dating from 6 months and 12 months were part of the series actually used in the previous reports [1, 9]. They consist of a 400 nm silver film evaporated

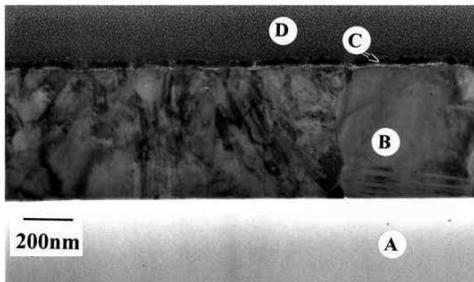


FIG. 1: Cross-sectional bright-field through-focal TEM micrograph of the Ag layer on a fused silica substrate. Labels refer to: fused silica substrate **A**, silver layer **B**, capping gold layer **C**, and capping platinum layer **D**. The darkened features in the Ag layer (**B**) are dislocations and grain boundaries.

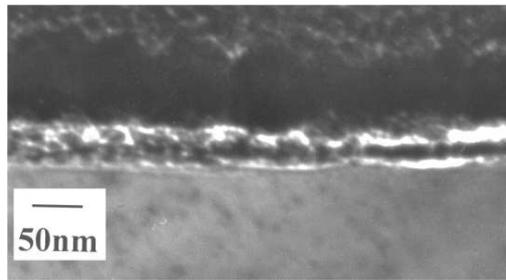


FIG. 2: A higher magnification de-focus image of the upper surface showing the Au-particle-containing protection layer. No Fresnel fringes are observed at the uppermost Ag surface when compared with in-focus images. White spaces indicate voids.

onto a fused silica substrate (Corning 7980 UV grade<sup>©</sup> 25 mm square, 1 mm thick optically polished on both sides to a roughness of no more than 0.7 nm). The structured substrates are stored in Fluoroware<sup>®</sup> sample holders, 25 mm diameter and 1 mm in depth at the center. Electron-transparent sections for cross-sectional transmission electron microscopy (TEM) examination were prepared by sample thinning to electron transparency using standard focused Ga<sup>+</sup>-ion beam (FIB) milling procedures [12] in a FEI 200 FIB workstation and placed on a holey carbon support. The TEM characterization was performed using a Philips CM300 Schottky field emission gun (FEGTEM) microscope operating at 300 kV. The FEGTEM has a point resolution of 0.2 nm and an information limit of 0.12 nm. The minimum focused electron beam probe size is 0.3 nm. In dark field images diffracted flux passes the objective aperture while the direct straight-through beam is blocked. The diffracted beam interacts strongly with the specimen and selection of a particular diffracted beam allows better visual phase differentiation. Typical regions of Ag layer that were thinned to electron transparency are shown at relatively low magnification in the bright field micrograph in Fig. 1. An immediate distinction can be made between the fused silica substrate (**A**) and the Ag deposit (**B**). Protective capping layers of Au and Pt, applied at the time of analysis, are marked at (**C**) and (**D**) respectively. The latter are used to prevent any ‘top down’ ion damage of the cross-section during the ion beam thinning preparation. The white colored line marked by an arrow in Fig. 1 is a band that contains very fine particles of Au formed during the initial stages of the deposition of this metal. The fine particles do not exhibit the same degree of absorption contrast as the bulk of the Au above them because the particle diameters are less than the thickness of the cross-sectional slice and thus do not extend through the full thickness of the TEM sample. It is clearly observed that the Au nanoparticles form a separate layer above the Ag deposit. Local undulations in

the Ag layer are observed to be devoid of any oxide or sulfide layer. Fresnel contrast methods were also used to examine the upper surface regions of the silver at the detail shown in Fig. 2. Imaging of layers in cross-section always results in Fresnel fringes. Because the amplitude and phase changes that occur when an electron is scattered elastically are characteristic of the atomic number, there will be changes in the elastic scattering directly related to the form of the projected scattering potential when there is a composition change at an interface viewed in projection [13], analogous to a phase grating filtering of the scattered electronic wave function. Interface Fresnel effects can thus provide a signature on the form and magnitude of any compositional discontinuity that is present. The visibility of these fringes depends on the thickness of the specimen and on the defocus value of the microscope. From Fig. 2, the critical observation is the *absence* of Fresnel effects at the surface of the metal other than at the localized regions associated with the gold protective coating. The lack of Fresnel fringes at the upper surface indicates a lack of variation in the scattering potentials and hence of the chemical composition at the interface. The silver surface is not covered by a detectable layer of sulfide or oxide since their presence would exhibit differences in scattering potential by comparison with the metal itself [14]. The lower detection limit for such compositional differences is a few tenths nanometer layer thickness. The absence of a dielectric layer is not surprising when account is taken of the small-volume, air-tight sample storage and the trace fractional concentrations of sulfur-containing contaminants in ordinary laboratory air [15].

The optical response of structured metal surfaces is simulated using a finite-difference-time-domain (FDTD) approach [16]. The subwavelength slit-groove structures [1, 9] are modeled in two dimensions and excited by TM polarized light. In metallic regions of space  $\epsilon$  is a complex, frequency-dependent function. Within the

standard Drude model [17] it is given as,

$$\varepsilon(\omega) = \varepsilon_0 \left( \varepsilon_\infty - \frac{\omega_p^2}{\omega^2 + i\Gamma\omega} \right), \quad (1)$$

where  $\varepsilon_0$  is the electric permittivity of free space,  $\varepsilon_\infty = \varepsilon(\omega \rightarrow \infty)$  is the dimensionless infinite frequency limit of the dielectric constant,  $\omega_p$  the bulk plasmon frequency, and  $\Gamma$  the damping rate. We numerically fit the real and imaginary parts of the Drude dielectric constant in the form of Eq. 1 to the experimental data collected in [18]. The Drude parameters obtained in the wavelength regime ranging from 750 nm to 900 nm for silver are  $\varepsilon_\infty = 3.2938$ ,  $\omega_p = 1.3552 \times 10^{16}$  rad s<sup>-1</sup>, and  $\Gamma = 1.9944 \times 10^{14}$  rad s<sup>-1</sup>, which correspond to  $\text{Re}[\varepsilon] = -33.9767$  and  $\text{Im}[\varepsilon] = 3.3621$  at  $\lambda_0 = 852$  nm. These fitted parameters are close to those determined in [1] by ellipsometry,  $\text{Re}[\varepsilon] = -33.27$  and  $\text{Im}[\varepsilon] = 1.31$ . Numerical results were not sensitive to this range of parameter variability. For reference we also implement perfect electric conductor (PEC) boundary conditions, where the metal dielectric constant is set to negative infinity, and all electromagnetic field components are therefore strictly zero in metal regions. The light source is a plane wave  $E_{\text{inc}}$ , incident perpendicular to the metal surface and depending on time as,  $E_{\text{inc}}(t) = E_0 f(t) \cos \omega t$ , where  $E_0$  is the peak amplitude of the pulse,  $f(t) = \sin^2(\pi t/\tau)$  is the pulse envelope, and  $\tau$  is the pulse duration ( $f(t > \tau) = 0$ ). Time propagation is performed by a leapfrogging technique [16]. In order to prevent nonphysical reflection of outgoing waves from the grid boundaries, we employ perfectly matched layer (PML) absorbing boundaries. To avoid accumulation of spurious electric charges at the ends of the excitation line and generate a pure plane wave with a well-defined incident wavelength, we embed the ends in the PML regions. Convergence is achieved with a spatial step size of  $\delta x = \delta y \lesssim 4$  nm and a temporal step size of  $\delta t = \delta x/(2c)$ , where  $c$  denotes the speed of light in vacuum. The parallel computation technique used in our simulations is described in detail in [22]. Calculations of the intensity,  $I \sim (E_x^2 + E_y^2 + H_z^2)$ , are performed and converged along a box contour. The collected data is averaged over time and the spatial coordinates for a range of slit-groove distances. Finally, the space- and time-averaged intensity is normalized to unit maximum. Our results are converged to the CW limit with incident pulse durations  $\tau \gtrsim 200$  fs. A direct comparison of the experimental data with both the PEC and the Drude models is shown in Fig. 3. Clearly, the Drude model agrees very well with the data, whereas the PEC model predicts oscillations of the intensity with a noticeably larger wavelength and smaller amplitude. In order to properly determine the wavelength of oscillations we use a cos function with an exponentially decreasing amplitude plus a constant offset to fit the data shown in Fig. 3. We also extend both the FDTD simulation and the fitting function

to a slit-groove distance of 16  $\mu\text{m}$ , well beyond the range of experimental data and take the Fourier transform of the fitted function over this extended range. We obtain the associated power spectrum expressed as a wavelength distribution. The results are shown in Fig. 5.

$$I_{\text{fit}}(x) = [A_1 + A_2 \exp(A_3 x)] \cos(A_4 x + A_5) + A_6 \quad (2)$$

The FDTD simulation and analytic fit for larger slit-groove distances are shown in Fig. 4 for the case of the Drude model. The fitting function Eq. 2 tracks the FDTD results over the entire slit-groove distance range. Figure 5 shows the normalized power spectrum corresponding to Eq. 2 as a function of the wavelength. The two power spectrum plots of Fig. 5 provide the effective wavelength,  $\lambda_{\text{eff}}$ , at which surface waves propagate as well as the distribution of modes around the peak. Note that the Drude model for silver shows a marked blue shift in peak wavelength and a noticeable broadening of the distribution compared to the perfect metal PEC model. The Drude simulation results in  $\lambda_{\text{eff}} = 837.482$  nm, whereas the PEC gives  $\lambda_{\text{eff}} = 852.066$  nm, very close to the free-space reference wavelength  $\lambda_0 = 852$  nm. The effective surface index of refraction,  $n_{\text{eff}} = \lambda_0/\lambda_{\text{eff}}$ , leads to the following values:  $n_{\text{eff}}(\text{Drude}) = 1.0173$  and  $n_{\text{eff}}(\text{PEC}) = 0.9999$ .

In summary surface analysis by transmission electron microscopy of subwavelength structured silver films used to investigate their optical response [1, 9] showed no detectable evidence of material on the surface other than silver. The suggestion that an 11 nm sulfide layer may be present so as to bring the interference pattern calculated by the authors of Ref. [11] into agreement with experiment is therefore not confirmed. In contrast to the calculations reported by Ref. [11], numerical solution of Maxwell's equations reported here shows excellent agreement with the fringe amplitude and wavelength over the

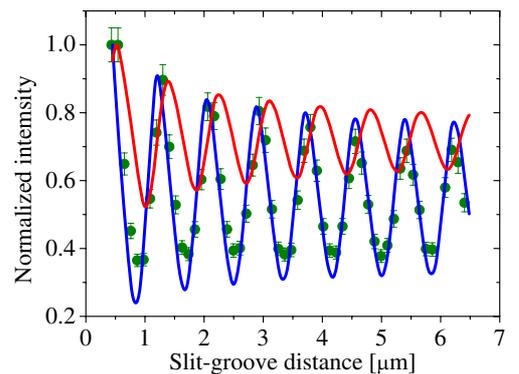


FIG. 3: Color online: Comparison of FDTD simulation and experiment. Green points are experimental data taken from [1]. Blue solid curve that closely fits the points corresponds to Drude model; red solid curve with longer fringe wavelength and smaller amplitude than data corresponds to PEC model.

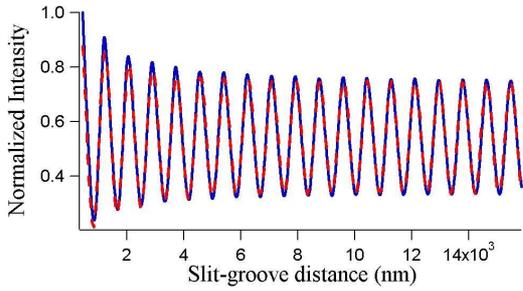


FIG. 4: Color online: Blue solid curve plots the same Drude model FDTD calculation as in Fig. 3 but extended to  $16 \mu\text{m}$  slit-groove distance. Red dashed curve plots the fitting function of Eq. 2.

near-zone slit-groove range measured in [1]. We emphasize that the amplitude decrease in this near-zone reflects evanescent mode dephasing and dissipation. It is much faster than loss rates expected from surface scattering or absorption [1]. Extrapolation of the FDTD simulations beyond the range of the measurements shows that the initially decreasing amplitude of the fringe settles to an oscillation with near-constant amplitude and fringe contrast. These features resemble the calculations of [11], but the results reported here accord with experiment without the need to invoke an 11 nm silver sulfide layer. Fourier analysis of the FDTD simulations reveal that the most probable wavelength in the Fourier distribution is 837 nm, within about 2 nm of the expected long-range SPP wavelength of 839 nm. Similar analysis of the PEC simulations yields a peak wavelength, as expected, at the free-space wavelength of 852 nm. Finally Figs. 4, 5 point to the important contributions to the surface wave of transient modes neighboring the SPP at slit-groove distances within the near-zone. The presence of these modes implies a surface k-mode “wave packet” that evolves to the final SPP as the wave passes beyond the near zone. This near zone, however, extends over several wavelengths; and therefore any theory of subwavelength array transmission must take these ephemeral, evanescent modes into account.

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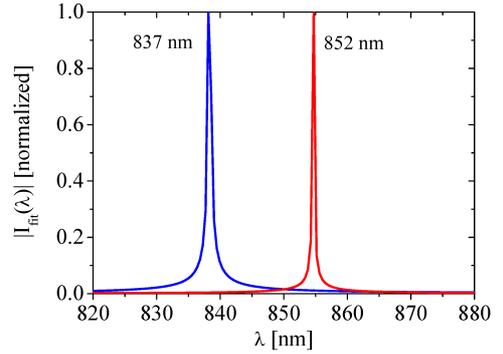


FIG. 5: Color online: Fourier transform spectra of Eq. 2 for Drude peaked at 837 nm (blue) and PEC peaked at 852 nm (red) FDTD simulation fits. Indicated  $\lambda_{\text{peak}}$  correspond to  $n_{\text{eff}}(\text{Drude}) = 1.017$ ,  $n_{\text{eff}}(\text{PEC}) = 1.000$

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