Lead Oxide-Modified TiO₂ Photocatalyst: Tuning Light Absorption and Charge Carrier Separation by Lead Oxidation State

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Modification of TiO₂ with metal oxide nanoclusters such as FeO₄, NiO₃ has been shown to be a promising approach to the design of new photocatalysts with visible light absorption and improved electron/hole separation. To study further the factors that determine the photocatalytic properties of structures of this type, we present in this paper a first principles density functional theory (DFT) investigation of TiO₂ rutile (110) and anatase (001) modified with PbO and PbO₂ nanoclusters, with Pb²⁺ and Pb⁴⁺ oxidation states. This allows us to unravel the effect of the Pb oxidation state on the photocatalytic properties of PbOx-modified TiO₂. The nanoclusters adsorb strongly at all TiO₂ surfaces, creating new Pb-O and Ti-O interfacial bonds. Modification with PbO and PbO₂ nanoclusters introduces new states in the original band gap of rutile and anatase. However the oxidation state of Pb has a dramatic impact on the nature of the modifications of the band edges of TiO₂ and on the electron/hole separation mechanism. PbO nanocluster modification leads to an upwards shift of the valence band which reduces the band gap and upon photoexcitation results in hole localisation on the PbO nanocluster and electron localisation on the surface. By contrast, for PbO₂ nanocluster modification the hole will be localised on the TiO₂ surface and the electron on the nanocluster, thus giving rise to two different band gap reduction and electron-hole separation mechanisms. We find no crystal structure sensitivity, with both rutile and anatase surfaces showing similar properties upon modification with PbOx. In summary the photocatalytic properties of heterostructures of TiO₂ with oxide nanoclusters can be tuned by oxidation state of the modifying metal oxide, with the possibility of a reduced band gap causing visible light activation and a reduction in charge carrier recombination.

1. Introduction

TiO₂ plays an important role in photocatalysis due to its properties, including relatively low cost, availability and non-toxicity. These properties make TiO₂ suitable as a photocatalyst for water-splitting technology using renewable resource in the form of solar light, or for depollution of toxic organic pollutants from the domestic and industry use. However the band gap of TiO₂ which lies in the range of 3.0 to 3.2 eV (depending on the crystal form) can only absorb in the UV region. It is therefore important to find a means to reduce the band gap and make TiO₂ active in the visible region. There are several ways to achieve this target and one of these is so-called “band gap engineering” which is focused on substitution of metal cations and/or non-metal anions at Ti and O sites in rutile or anatase.

Efforts in band gap engineering and while the results are promising, there are still important practical issues like stability, solubility and reproducibility that may limit TiO₂ doping for photocatalyst production. Another important aspect of photocatalyst efficiency is recombination of photoexcited electrons and holes (charge carriers) and we need to understand how modifying TiO₂ impacts this important factor.

Nanoscale heterostructures composed of two different structures interfaced together can be used to improve the photocatalytic properties of TiO₂ or any other oxide. Research in this field shows that the interface between two materials play an important role in tuning photocatalytic properties and inducing activity of material in the visible region. Recent examples of such heterostructures are BiOBr-ZnFe₂O₄, AgI-BiO₂ and BiVO₃-WO₃, where improved activity in the visible region has been reported.

Fabrication of interesting heterostructures of TiO₂ modified with dispersed, molecular scale metal oxide nanoclusters has been presented by Libera et al (using atomic layer deposition (ALD) and Tada et al (using chemisorption-calcination (CCC)) for FeOx-modified TiO₂. In both experiments, similar results in terms of band gap reduction and photocatalytic activity were found and the results are explained by the presence of FeOx cluster derived electronic states lying at the valence band of TiO₂ and pushing the valence band edge up in energy. Moreover the results of photoluminescence spectroscopy revealed a reduction in electron/hole recombination explained by suppression of the PL TiO₂ peak at 540nm. Using first principles density functional theory simulations of models of metal oxide...
nanocluster modified TiO$_2$, we have previously shown that (FeO)$_{29}$, (NiO)$_{30}$ and (SnO)$_{32}$ nanoclusters supported on TiO$_2$ can reduce the band gap and improve the photocatalytic properties of heterostructures. We have also found that oxide nanocluster modifications of TiO$_2$ may also result in no effect in terms of band gap reduction, for example, supported SnO$_2$ nanoclusters on anatase (001) have no impact on the anatase band gap.  

A comparison of SnO and SnO$_2$ modified TiO$_2$ in our DFT simulations$^{31,32}$ shows the dramatic effect of the metal oxidation state – with SnO modification reducing the anatase band gap and SnO$_2$ modification having no effect. An experiment from Boppama and Lobo$^{33}$ examined ZnGa$_2$O$_4$ modified with SnO and SnO$_2$ and these authors also found a dramatic effect arising from Sn oxidation state, with only SnO modified ZnGa$_2$O$_4$ showing visible light activity, but no detailed explanation for this effect was presented. We have suggested that the presence of the Sn(II) stereochemical lone pair in SnO is the origin of the difference between SnO and SnO$_2$ modified TiO$_2$. Thus, it appears that there is great potential in examining how metal oxides with variable oxidation states and a stereochemical lone pair could be used to modify TiO$_2$ for visible light absorption.

Motivated by this idea, in this paper we present results for models of rutile (110) and anatase (001) modified with PbO and PbO$_2$ nanoclusters and investigate further how the oxidation state of the metal (Pb$^{2+}$ vs. Pb$^{4+}$) impacts the energy gap of TiO$_2$ and how this idea may be useful for photocatalyst design based on surface modified metal oxides.

### 2. Computational Methods

To model TiO$_2$ rutile (110) and anatase (001) surfaces, we use a three dimensional periodic slab model within the VASP code.  

The valence electrons are described by a plane wave basis set and the cut-off for the kinetic energy is 396 eV. The core-valence interaction is described by PAW potentials$^{35}$ and the number of valence electrons is 4 for Ti, 4 for Pb and 6 for O. The exchange-correlation functional was approximated by the Perdew-Wang 91$^{36}$ functional. We use a Monkhorst-Pack (2×1×1) k-point sampling grid.

To describe Ti 3d states the DFT+U approach was used where U=4.5 eV. The need to introduce the U parameter in order to describe properly d shells in transition metals is well known.$^{37-41}$

For Pb, the electronic states for Pb$^{2+}$ and Pb$^{4+}$ oxidation states are consistently described by DFT so no U correction is applied.

While the DFT+U approach gives a consistent description of the Ti 3d electronic states, it will still underestimate the band gap. This is of course an important issue, however, we are primarily concerned with qualitative changes in the band gap upon surface modification, that is whether the metal oxide nanocluster reduces the energy gap or not and for this, DFT+U is sufficiently useful.

The rutile (110) and anatase (001) surfaces are used as the initial substrates for modification with PbO$_2$ nanoclusters. The rutile (110) surface is the most widely studied TiO$_2$ surface and the most likely to be used in any experimental work. This surface has two-fold coordinated bridging O atoms, 5-fold coordinated surface Ti atoms and 6-fold coordinated surface Ti atoms. A (2x4) surface supercell expansion is employed to allow isolated nanoclusters to be adsorbed. The anatase (001) surface, while not the most stable anatase surface, has been of great interest for its potential photocatalytic activity and is considered here for this reason. In our work, we study anatase (001) as an unreconstructed surface, which is reasonable to describe this surface. Some preliminary calculations of anatase (101) modified with lead oxide nanoclusters indicate no significant effects as a result of the surface used. The (001) surface is terminated by two-fold coordinated oxygen atoms while the oxygen atoms in the surface are three coordinated. The Ti atoms in the surface are 5-fold coordinated. A (4+2) surface supercell is used. Both surface models are stoichiometric with no defects and no adsorbed hydroxyl species, both of which are well known defects in TiO$_2$ surfaces and a 12 Å vacuum gap is used. The convergence criteria for the electronic and ionic relaxations are 0.0001 eV and 0.02 eV/Å. For the consistency in the calculation, we also applied the same supercell and technical parameters for the bare TiO$_2$ surface and free clusters.

The clusters are positioned on the TiO$_2$ surfaces and the adsorption energy is computed from:

\[
E_{\text{ads}} = E((\text{PbO}_x)-\text{TiO}_2) - \{ E(\text{PbO}_x) + E(\text{TiO}_2) \}
\]

Where \(E((\text{PbO}_x)-\text{TiO}_2)\) is the total energy of the PbO$_x$ (PbO or PbO$_2$) nanocluster supported on the anatase surface and \(E(\text{PbO}_x)\) and \(E(\text{TiO}_2)\) are the total energies of the free PbO cluster and the unmodified anatase surface. A negative adsorption energy indicates that cluster adsorption is stable.

To study a model of the photoexcited electronic state of PbO-modified anatase and examine how the Pb oxidation state determines the electron and hole trapping, we take the (PbO) and PbO$_2$-modified rutile models as examples and generate a triplet electronic state,$^{32,42,44}$ in which we have an excited electron in the conduction band and a hole in the valence band. To describe reduced Ti$^{3+}$ that are formed we continue to use DFT+U (\(U = 4.5\) eV on the Ti 3d states). However, we also have to properly describe the localized hole formed after excitation and the DFT+U approach is also applied to the O 2p states,$^{32,42}$ with a Hubbard \(U\) of 5.5 eV sufficient to give valence band hole localisation.$^{32,44}$ The following calculations are performed:

- a single point energy of the triplet at the singlet geometry, \(E_{\text{unrelaxed}}\)
- a full ionic relaxation in the triplet electronic configuration, \(E_{\text{relaxed}}\)
- a dipole correction perpendicular to the surface plane is added to the total energies. Within this computational set-up, the following energies are calculated:

(1) The singlet-triplet vertical unrelaxed excitation energy: \(E_{\text{unrelaxed}} = E_{\text{singlet}} - E_{\text{triplet}}\), where the singlet (ground state) is fully relaxed and the triplet is fixed at the ground state geometry. This should correspond to the simple VB-CB energy gap from the density of states.

(2) The singlet-triplet vertical excitation energy: \(E_{\text{relaxed}} = E_{\text{singlet}} - E_{\text{triplet}}\), where both the singlet and triplet electronic states are fully relaxed. The change in this energy with respect to the bare surface allows us to determine the effect of the surface modification on the energy gap of TiO$_2$.

(3) The triplet relaxation (or trapping) energy: \(E_{\text{relaxed}} = E_{\text{triplet}} - E_{\text{unrelaxed}}\), where the first energy is the fully
relaxed triplet and the second energy is the triplet state at the singlet geometry (from (1) above), so that $E^{\text{elax}}$ is the energy gained when the electron and hole are trapped at their Ti and O sites upon structural relaxation.

3. Results and Discussion

3.1 PbO and PbO$_2$ Nanoclusters Supported on TiO$_2$ Rutile (110)

Figure 1 presents the relaxed atomic structures together with adsorption energies for representative PbO$_x$ nanoclusters supported on the model rutile (110) surface: PbO, Pb$_2$O$_2$, Pb$_3$O$_6$, and Pb$_4$O$_8$. All clusters adsorb strongly at the surface with adsorption energies in the range from -2.81 eV to -7.16 eV and creating new interfacial metal-oxygen bonds. The magnitude of the adsorption energies indicates that the adsorbed nanoclusters will be stable to aggregation.

Table 1 presents the details of the new metal-oxygen bonds between the clusters and the surface. The smallest cluster, PbO, supported on rutile (110) creates three new bonds: Pb surface metal bonds to O cluster atoms with two bonds (2.25 Å, 2.45 Å) and the third bond between O cluster atom and Ti surface atom is 1.80 Å. In bulk litharge structured PbO, the Pb-O distances are 2.35 Å [6] and in the free PbO clusters, the Pb-O distances are in the range of 1.97 – 2.22 Å, so that the increased Pb coordination in the supported clusters leads to longer Pb-O distances that are reasonable for the Pb$^{2+}$ oxidation state.

The Pb$_2$O$_3$ cluster results in seven new bonds: there are five bonds between Pb atoms and O atoms with the distances from 2.26Å to 2.61Å. The next two bonds between O cluster atoms and Ti surface atoms have the distances 1.78Å and 1.92Å. The adsorption of the biggest Pb$_4$O$_8$ cluster results in five new bonds: three bonds between Pb cluster atoms and O surface atoms with distances 2.31Å, 2.45Å and 2.55Å and the next two bonds from O cluster atoms and Ti surface atoms have distances 1.89Å and 1.89Å.

![Figure 1](image_url)

Table 1. New surface-cluster Pb-O bond distances for PbO and PbO$_2$ nanoclusters absorbed on TiO$_2$ rutile (110).

<table>
<thead>
<tr>
<th>Distances / Å</th>
<th>Pb$_2$-O$_2$</th>
<th>O$<em>2$-Ti$</em>{1}$</th>
<th>Pb$_3$-O$_6$</th>
<th>O$<em>2$-Ti$</em>{1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>PbO</td>
<td>2.25; 2.45</td>
<td>1.80</td>
<td>2.29; 2.52; 2.48; 2.29</td>
<td>1.96; 1.99; 1.96</td>
</tr>
<tr>
<td>Pb$_2$O$_2$</td>
<td>2.52; 2.56; 2.61; 2.26</td>
<td>1.93; 1.78</td>
<td>2.44; 2.30; 2.30</td>
<td>1.91; 1.99; 1.85</td>
</tr>
<tr>
<td>Pb$_3$O$_4$</td>
<td>2.31; 2.45; 2.55</td>
<td>1.89; 1.88</td>
<td>2.15; 2.23; 2.65; 2.39; 2.33</td>
<td>1.91; 2.02; 1.82; 2.06</td>
</tr>
</tbody>
</table>

[a] Pb from the cluster (Pb$_x$) and O from the surface (O$_x$) [b] O from the cluster (O$_x$) and Ti from the surface (Ti$_x$)

In all heterostructures Ti atoms in the (110) surface are pulled out of the surface when bonded to O atoms from the clusters: by 0.74Å for the PbO cluster and by 0.91Å for the biggest Pb$_4$O$_8$
cluster.

Figure 2 presents the electronic density of states projected (PEDOS) onto Pb 6s and O 2p states of the supported PbO and PbO₂ nanoclusters and the Ti 3d and O 2p states of the rutile (110) surface. The PEDOS plot is presented here in order to investigate the changes to the valence and conduction band edges due to adsorption of the lead oxide nanoclusters. In each case the zero of energy is the top of the occupied states. Considering firstly the PbO nanoclusters, the smallest PbO nanocluster does not introduce new states into the band gap of TiO₂ when adsorbed at the rutile (110) surface. The (PbO)₂ nanocluster results in the presence of cluster derived Pb and O states at the top of the VB. The biggest (PbO)₄ nanocluster introduces new PbO derived electronic states above the VB edge of TiO₂, which gives a significant reduction in the energy gap of TiO₂ while at the same time leaving the conduction band unchanged, so that the energy gap between the TiO₂ surface VB and CB is unchanged over unmodified TiO₂.

These new electronic states derived from the nanocluster will result in a narrowing compared to the original energy gap of TiO₂ because the valence band edge now lies higher in energy. The PEDOS plot for PbO₄ supported on TiO₂ gives an indicative VB shift of 1eV compared to original TiO₂ band gap, which would result in visible light absorption. We note however that these energy differences are simply Kohn Sham eigenvalue differences and in a later section will examine this in more detail.

Contrary to this, the results for PbO₂ supported nanoclusters show no change in the region of the valence band of TiO₂ while new electronic states derived from empty Pb 6s states lie in the energy gap, below the conduction band edge of TiO₂. These new states can function as states into which an electron from the (unmodified) TiO₂ valence band can be excited, thus giving an effectively reduced energy gap when compared to unmodified TiO₂ (again the surface VB-CB energy gap is unchanged upon modification). In this case, the energy gap underestimation with DFT is clearly apparent, as in the largest Pb₄O₈ nanocluster, the empty Pb states are found ca. 0.9 eV above the VB edge. However, the important point is that the modification of TiO₂ with PbO₂ does lead to a reduction in the energy gap.

The nature of the VB and CB in the different PbOx modifications of TiO₂ will have important consequences for hole and electron separation after photoexcitation. More details on this are presented in section 3.3. However, from the DOS analysis we can propose that in both cases PbO and PbO₂ modification of rutile will enhance the electron/hole separation. This arises since after excitation of PbO-TiO₂, the electron will be found in the surface and the hole on the nanocluster, while for PbO₂-TiO₂, the electron will be found on the PbO₂ nanocluster and the hole on the rutile surface, giving different mechanisms for electron-hole separation after photoexcitation.
Fig. 2 Electronic density of states projected (PEDOS) onto Pb 6s, O 2p of the PbO and PbO$_2$ clusters and Ti 3d, and O 2p states of the rutile (110) surface. In each set of plots, the energy zero is set to the top of the highest occupied electronic states, which is different for each PbO and PbO$_2$ modified TiO$_2$ system.
The Bader charges on Pb in PbO-TiO<sub>2</sub> nanoclusters are +1.20 electrons and in the PbO<sub>2</sub> nanoclusters, we computed Pb charges around +0.58 electrons. All Ti and O atomic charges are consistent with a Ti<sup>4+</sup> and O<sup>2-</sup> oxidation state.

Tin is another metal with two oxides, one of which has a stereochemically active lone pair. The present results for PbO and PbO<sub>2</sub> modified rutile can be compared to SnO and SnO<sub>2</sub> modified TiO<sub>2</sub> where our calculations show that the adsorption of SnO clusters on TiO<sub>2</sub> surfaces results in the introduction of the states above the valence band of TiO<sub>2</sub> which come from the Sn 5s – O 2p interaction and this shifts the valence band to higher energy, reducing the energy gap. In contrast, the adsorption of SnO nanoclusters slightly affects the conduction band edge, with a small downwards shift of the CB edge observed in this case arising from empty Sn 5s states, in contrast to the position of the empty states in the energy gap from the PbO<sub>2</sub> nanoclusters.

### 3.2 PbO and PbO<sub>2</sub> nanoclusters supported on anatase (001)

Figure 3 presents the atomic structure of representative Pb<sub>2</sub>O<sub>2</sub> and PbO<sub>2</sub> nanoclusters supported on the TiO<sub>2</sub> anatase (001) surface. We investigate briefly if the different crystal structure of anatase compared to rutile can impact the properties after metal oxide cluster deposition. From these representative structures we conclude that the adsorption energies are similar to adsorption at the rutile (110) surface and the number of new bonds between clusters and surface are in the same range as well. The detailed metal-oxygen distances are presented in table 2 and the metal-oxygen distances are in the same range compared to PbO and PbO<sub>2</sub> modified rutile (110).

**Fig. 3** Relaxed adsorption structures with adsorption energies given in eV for (a) Pb<sub>2</sub>O<sub>2</sub> and (b) PbO<sub>2</sub> clusters on TiO<sub>2</sub> anatase (001).

**Table 2.** New surface-cluster Pb-O bond distances for (PbO)n and (PbO<sub>2</sub>)n clusters absorbed on TiO<sub>2</sub> anatase (001).

<table>
<thead>
<tr>
<th>Distances / Å</th>
<th>Pb-O&lt;sub&gt;[1]&lt;/sub&gt;, O&lt;sub&gt;Ti&lt;/sub&gt;&lt;sup&gt;[a]&lt;/sup&gt;</th>
<th>Pb-O&lt;sub&gt;[2]&lt;/sub&gt;</th>
<th>O&lt;sub&gt;Ti&lt;/sub&gt;&lt;sup&gt;[b]&lt;/sup&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pb&lt;sub&gt;2&lt;/sub&gt;O&lt;sub&gt;2&lt;/sub&gt;</td>
<td>2.45; 1.92</td>
<td>2.11</td>
<td>1.90; 1.86</td>
</tr>
<tr>
<td>PbO&lt;sub&gt;2&lt;/sub&gt;</td>
<td>2.45; 1.92</td>
<td>2.44</td>
<td></td>
</tr>
</tbody>
</table>

[a] Pb from the cluster (Pb<sub>c</sub>) and O from the surface (O<sub>s</sub>) [b] O from the cluster (O<sub>c</sub>) and Ti from the surface (Ti<sub>s</sub>)

Figure 4 presents the PEDOS from the Pb 6s and O 2p states of the nanocluster and the surface and Ti 3d and O 2p states of anatase (001) after modification with PbO and PbO<sub>2</sub> nanoclusters. The PbO nanocluster introduces new states at the top of the valence band of anatase (001), while the PbO<sub>2</sub> nanocluster results in new states below the original conduction band of anatase (001). When comparing to the SnO<sub>2</sub> modification to rutile and anatase in refs. 31 and 32, where a notable crystal structure sensitivity was found in experiment and modelling, we can state that in contrast PbO<sub>2</sub> nanocluster modified TiO<sub>2</sub> shows no crystal structure sensitivity, with modifications to both rutile and anatase showing an effect on the energy gap. For SnO<sub>2</sub> nanocluster modified TiO<sub>2</sub>, a positive effect on the visible light photocatalytic activity was only seen for rutile<sup>31</sup>. This difference arises for SnO<sub>2</sub> and PbO<sub>2</sub> modifications since the PbO<sub>2</sub> energy states lie lower in energy than the SnO<sub>2</sub> energy states and will create new electronic states in the original energy gaps of both TiO<sub>2</sub> polymorphs.

**Fig. 4** The electronic density of states projected (PEDOS) onto Pb 6s and O 2p states of the supported Pb<sub>2</sub>O<sub>2</sub> and PbO<sub>2</sub> clusters and the Ti3d and O 2p states of the anatase (001) surface.

### 3.3. The Effect of Pb Oxidation state on the Excitation Energy and the Nature of the Photoexcited State.

The PEDOS plots of PbO and PbO<sub>2</sub> modified rutile (110) presented in figure 2 indicates two different VB and CB alignments, that are shown in the schematic diagram in figure 5.

For PbO supported nanoclusters the top of the valence band is from PbO nanocluster states and the surface Ti 3d states dominate the bottom of the conduction band of TiO<sub>2</sub>. For PbO<sub>2</sub> supported nanoclusters the top of the valence band is from Ti 3d states while the PbO<sub>2</sub> states dominate the conduction band of TiO<sub>2</sub>.

**Fig. 5** Schematic diagram for indication of electron/hole localisation. h<sup>+</sup> and e<sup>-</sup> indicate the electron and hole formed after photoexcitation.
These arrangements of the valence and conduction bands will enhance electron and hole separation upon photoexcitation, although the locations of hole and electrons will be different depending on oxidation state. From the schematic in figure 5, we propose that for PbO-modified TiO₂ photoexcitation will lead to the electron populating the conduction band which derives from rutile (110) surface, while the hole localization will be at the top of the PbO derived valence band. The localization of electron/hole for PbO₂-modified TiO₂ will be different: the electron will be found in conduction band states derived from empty Pb-O electronic states, while the hole should be localised on TiO₂ valence band derived states.

We examine charge separation by using the model of photoexcited state where a triplet electronic state is introduced. By construction this will have an electron in the conduction band and a hole located in the valence band. For rutile and anatase TiO₂, refs. 42, 43 and 45 have shown that this model produces a localised Ti³⁺ electronic state and a localised oxygen hole state (polarons), so long as DFT+U, with appropriate values of U on Ti and O, or hybrid DFT are used. These are necessary to localise the resulting polaronic states after photoexcitation. In the present systems, our intention is to study the location of the electron and hole after photoexcitation and demonstrate how changing the Pb oxidation state, which can be achieved by changing the Pb precursor in a synthesis, can lead to two different mechanisms of electron/hole separation.

Table 3 presents the vertical, relaxation and excitation energies for the bare rutile (110) surface and the PbO₂-modified surface. For the PbO₂-modified surface, we found that due to the close proximity of the empty Pb 6s states to the valence band, the photoexcited model with the strong DFT+U band gap underestimation gives an excitation energy that is close to 0 eV. Thus, we can highlight that while the simple photoexcited model has some merits, the underlying DFT functional plays an important role in its applicability. For PbO-modified TiO₂, we can compute these energies with more confidence.

<table>
<thead>
<tr>
<th>Table 3: Excitation and relaxation energies for the triplet excited state in PbO- modified TiO₂ in eV. Also shown are the same energies for the bare rutile (110) surface.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Structure</td>
</tr>
<tr>
<td>Rutile TiO₂ (110)</td>
</tr>
<tr>
<td>PbO₂ rutile 110</td>
</tr>
</tbody>
</table>

The energies for the bare rutile (110) surface have been discussed in ref. 45 and we point out here that the vertical energy is very similar to the valence-conduction band gap from the DOS and the excitation energy is lower as a result of relaxation following electron and hole formation.\(^{42,45}\) Considering PbO₂-modified rutile (110), the vertical and excitation energies are reduced by the surface modification, confirming the simple DOS analysis that PbO modification of TiO₂ will reduce the energy gap of TiO₂. The relaxation energy is also larger for PbO-modified rutile, which arises from the large gain in energy when the nanocluster strongly relaxes around the valence band hole, compared to relaxations in the (110) surface.

Figure 6 shows the spin density of the relaxed photoexcited state for the \( \text{Pb}_2\text{O}_4 \) and \( \text{Pb}_2\text{O}_4 \) nanoclusters supported on rutile (110).

For \( \text{Pb}_2\text{O}_4 \)-rutile (110) the electron is localised on a Ti site in the subsurface layer of rutile which assigned as a Ti³⁺ site. This can be confirmed by a Bader charge\(^{47}\) of +1.66 electrons and spin magnetisation of +0.9 electrons. In contrast, the Ti⁴⁺ cation has a computed Bader Charge of +1.27 electrons and zero spin magnetisation. This localisation of electron gives an elongation of nearest Ti-O bonds of ca. 0.1 Å, which is typical for Ti-O bonds with a Ti⁴⁺ cation. The hole is localised on O from the PbO nanocluster with a computed Bader charge of +7.11 electrons and a computed spin magnetisation of +0.76 electrons.

In contrast to SnO-modified TiO₂\(^{32}\) where the hole is spread over an Sn-O bond, there is in the present structure little Pb contribution to the valence band hole. This would be consistent with the bulk findings that the lone pair effect diminishes as one goes down the group 14 column from Sn to Pb.\(^{48}\)

Fig. 6 Spin density and geometry of the photoexcited state in PbO and PbO₂-modified rutile (110)

Despite the issues with the very small energy gap and the computed singlet-triplet excitation energy, we briefly consider the nature of the photoexcited state for PbO₂-modified rutile (110). With a Pb⁴⁺ oxidation state giving empty Pb states in the energy gap, the excited electron is distributed over a Pb atom from the cluster and two neighbouring oxygen atoms in the cluster. We characterise this Pb as a Pb⁴⁺ ion, confirmed by a Bader charge of +1.49 electrons (a Pb⁴⁺ cation has a computed Bader Charge of +0.58 electrons). The spin density in figure 6 shows that two oxygen atoms in the nanocluster also carry the electron, with Bader charges of +7.3 and +7.6 electrons for these O atoms and a computed spin magnetisation of +0.57 and +0.23 electrons, suggesting that the electron is spread over an O-Pb-O unit in the nanocluster. This gives an elongation of the cluster Pb-O bonds of ca. 0.3 Å. The valence band hole is localised on a bridging oxygen from the surface, with a computed Bader charge of +6.74 electrons and a spin magnetisation of +0.77 electrons, together
with an elongation of the nearest Ti-O bonds that involve this oxygen of 0.1 Å. The locations of the electron and hole in the PbO$_2$-TiO$_2$ system appear to suggest that a less favourable separation of charge carriers is likely in this case, especially when compared with PbO$_2$-modified TiO$_2$. This would have the consequence of more charge carrier recombination and lower photocatalytic activity.

### 3.3 Discussion

We have examined modifying TiO$_2$ rutile (110) and anatase (001) surfaces with PbO and PbO$_2$ nanoclusters to investigate: (1) the role of the metal oxidation state in the nanocluster in inducing visible light activation and charge recombination reduction, (2) the importance of the lone pair effect and (3) crystal sensitivity.

Modification of rutile (110) and anatase (001) with PbO and PbO$_2$ nanoclusters is predicted to lead to a reduced energy gap compared to unmodified TiO$_2$. We expect that such structures will display visible light activity and, arising from the nature of the valence and conduction bands, a reduction in charge recombination after excitation. It is however, in the mechanism of band gap reduction and charge separation that we see differences between the two Pb oxidation states.

For PbO nanoclusters supported on rutile (110) and anatase (001) the results are consistent with previous theoretical and experimental findings for FeO$_x$, NiO$_x$, and SnO$_{2x-1}$, where the original TiO$_2$ band gap is reduced due to the introduction of electronic states from the nanoclusters above the TiO$_2$ valence band. The experimental studies using valence band X-ray photoelectron spectra confirm the reduction of band gap due to a rise of the valence band edge for FeO$_x$ and NiO$_x$ and are consistent with the modelling results, so that this mechanism of energy gap reduction should hold. A model of the photoexcited state confirms the reduction in the energy gap by modifying TiO$_2$ with SnO nanoclusters and highlights the charge separation upon photoexcitation.

However PbO$_2$ nanoclusters supported on rutile (110) and anatase (001), while leading to a predicted band gap reduction, present a striking difference in terms of the mechanism of band gap reduction and the nature of the valence and conduction band edges, somewhat similar to SnO$_{2x-1}$ nanoclusters on rutile (110). In the latter, there is no rise in the TiO$_2$ valence band edge but the SnO$_2$ nanocluster states are present below the conduction band of TiO$_2$, giving a small reduction in the energy gap. For PbO$_2$-modified rutile, we find that the Pb-derived states lie well below the conduction band edge of TiO$_2$, which will reduce the energy gap. Unfortunately, the position of the states in the energy gap means that the simple photoexcited model does not work for computing excitation energies within the present computational set-up and in addition our results suggest that the spatial separation of electrons and holes will be less favourable in PbO$_2$-modified rutile compared to PbO-modified rutile.

Some support for this oxidation state effect comes from the recent experimental work on ZnGa$_2$O$_4$ which was modified with SnO and SnO$_2$ nanoclusters and the oxidation of Sn state was controlled by different precursors. In that work, only the modification with SnO resulted in a reduction of the band gap of ZnGa$_2$O$_4$. However, no atomic level explanation of this finding was given. However, the present results and those in refs. 31 and 32 along with these experimental hints do strongly indicate that the oxidation state of the metal in the nanocluster plays an important role in tuning the properties of photocatalyst.

In terms of the lone pair effect, for SnO-modified TiO$_2$, we find a strong effect on the energy gap with the valence band edge shifted upwards and derived from the Sn-6s-O2p interaction in the nanocluster. Analysis of the photoexcited state showed localisation of the hole on an Sn-O bond and the electron on a surface Ti atom. For PbO, the shift of the TiO$_2$ band gap is due to the presence of Pb-6s-O-2p derived states from the PbO nanocluster pushing up the valence band edge. However the photoexcited states calculations suggests that the effect of the lone-pair is smaller compared to SnO-modified TiO$_2$, since the hole formed after photoexcitation is now also localised on oxygen in the nanocluster. Comparison with bulk indicates that the weakening of the lone pair effect is similar to bulk SnO and PbO.

Another aspect of our analysis of the photoexcited of modified TiO$_2$ is new insights into the possibility of reducing electron-hole recombination and improving the photocatalytic properties. For PbO nanocluster modified rutile (110) and anatase (001) the hole is found on the nanocluster and the electron on a single Ti$^{3+}$ in subsurface of the TiO$_2$ surface. In contrast, the PbO$_2$-TiO$_2$ photoexcited state shows electron-hole separation enhancement but with different locations of the hole and electron: the hole is localised on a bridging O atom from the surface while the electron is associated with an O-Pb-O structure in the PbO$_2$ nanocluster. Again the oxidation state of the metal in metal oxide supported nanoclusters presents an interesting approach to tuning of the photocatalytic properties of metal oxides.

Finally, comparing the properties of PbO and PbO$_2$-modified rutile (110) and anatase (001) for any crystal structure sensitivity previously found for SnO/SnO$_2$ modified anatase, we have found that there is no sensitivity to crystal structure for lead oxide modified TiO$_2$.

### Conclusions

We present DFT simulations of lead oxide nanoclusters supported on TiO$_2$ rutile (110) and anatase (001) surfaces. We found that the oxidation state of the metal in the supported metal oxide nanocluster plays an important role in defining the energy gap and the nature of the valence and conduction band edges. A reduction in the band gap of rutile and anatase TiO$_2$ can be achieved by modification with PbO or PbO$_2$ nanoclusters. Different Pb oxidation states show different electron/hole localisation upon photoexcitation and hence different mechanisms for charge separation. The enhancement in electron/hole separation will improve photocatalytic properties over pure TiO$_2$. Photoexcited calculations for PbO nanoclusters supported on rutile (110) show the decreasing effect of the lone-pair which is similar to bulk. There is no crystal sensitivity reported for adsorbed PbO and PbO$_2$ nanoclusters on rutile (110) and anatase (001). Finally, the present set-up of VB-CB shows reduction in the band gap comparing to TiO$_2$ origin and The present results give interesting insights into the possibility in tuning the photocatalytic properties by metal oxidation state, lone pair effect and crystal structure for developing new photocatalysts.
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Notes and references

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Graphic Abstract

The photocatalytic properties of lead oxide modified TiO₂ are controlled by the oxidation state of lead.