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A positron annihilation spectroscopic investigation of europium-doped cerium oxide nanoparticles

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Doping in ceria (CeO$_2$) nanoparticles with europium (Eu) of varying concentrations (0, 0.1, 0.5, …, 50 atom%) are studied using complementary experimental techniques and novel observations were made during the investigation. The immediate observable effect was a distinct reduction in particle sizes with increasing Eu concentration attributed to the relaxation of strain introduced due to the replacement of Ce$^{4+}$ ions by Eu$^{3+}$ ions of larger radius. However, this general trend was reversed in the doping concentration range of 0.1 - 1 atom % due to the reduction of Ce$^{4+}$ to Ce$^{3+}$ and the formation of anion vacancies. Quantum confinement effects became evident with the increase of band gap energy when the particle sizes reduced below 7-8 nm. Positron annihilation studies indicated the presence of vacancy type defects in the form of vacancy clusters within the nanoparticles. Some positron annihilation was also seen on the surface of crystallites as a result of diffusion of thermalized positrons before annihilation. Coincidence Doppler broadening measurements indicated the annihilation of positrons with electrons of the different species of atoms and the characteristic $S$ - $W$ plot showed a kink-like feature at the particle sizes where quantum confinement effects began.

1. Introduction

Ceria is an oxide with a wide range of uses including polishing material, catalysis, fuel cells, advanced ceramics and sensors amongst others.\textsuperscript{1-4} Many of its applications rely on the ability of ceria to transport and act as a labile source of oxygen.\textsuperscript{5, 6} To this effect, it is often ‘doped’ with lower valence ions particularly trivalent lanthanide cations.\textsuperscript{7-9} These ions are introduced into the lattice to substitute for Ce$^{4+}$ ions and it is generally believed that anion vacancies are created as a means of charge compensation\textsuperscript{10} although other defect mechanisms have been proposed by Yeriskin et al.\textsuperscript{11} The study of the defect chemistry of cerium oxide nanoparticles doped by europium (Eu) ions has become of significant interest because of the modification of the optical
and luminescent properties of the material on doping.\textsuperscript{12} Numerous studies have recently appeared in the literature emphasizing the roles of vacancy type defects and their evolution during the changes in crystallite sizes\textsuperscript{13} and doping concentrations.\textsuperscript{14} However, a comprehensive study of defect structure and dynamics has yet to be carried out for this system. In this work, we will address this issue with a systematic study of the defects generated by europium doping. We shall also study the interaction of the defects with the dopant ions when Eu is doped in discrete and varying concentrations. Positron annihilation spectroscopy is used as an effective method to study the defects and their evolution on doping. It is thought this is extremely pertinent since, discussed by us earlier, techniques such as x-ray photoelectron spectroscopy (XPS) and x-ray diffraction (XRD) have limitations in the study of these systems because of complex spectral peak shapes and the sensitivity of ceria to x-ray irradiation.\textsuperscript{12} Positron annihilation is a technique that can be used to study defects in material systems very reliably and it can be sensitive to even very low defect concentrations.\textsuperscript{15,16}

2. Experimental

2.1 Positron annihilation studies

Positron annihilation experiments were performed by placing sufficient sample in a glass tube of approximately 10 mm diameter so as to embed a positron emitting $^{22}$Na radioactive isotope at its geometric centre. The source, about 400 kBq in strength, was made in the form of a small deposition of $^{22}$NaHCO$_3$ on part of a thin ($\sim$ 2 mg cm$^{-2}$) Ni foil with remaining foil used to cover and protect the source. The glass tube containing the source-sample assembly was continuously evacuated to maintain a clean and dry atmosphere in it. The gamma rays resulting from positron emission and subsequent annihilation were recorded using nuclear radiation detectors and the signals were processed using the associated electronics. Two types of experiments were carried
out, the first of which recorded the positron lifetime spectrum using a gamma-gamma slow-fast coincidence spectrometer and the other recording the Doppler broadening of the positron annihilation gamma ray spectrum in coincidence mode using two high pure germanium (HPGe) detectors. In the former, about 1-1.5 million counts were collected in each spectrum and the spectra were analyzed using the program PALSfit. In the coincidence Doppler broadening spectra (CDBS), about 8 million events were generated from the counts accumulated. Briefly, gamma ray events at energies $E_1$ and $E_2$ were recorded from two high sensitive HPGe detectors and a two-parameter spectrum was generated from their time corrections with $E_1 + E_2$ and $E_1 - E_2$ as two coplanar axes and counts distributed accordingly. The projected one-dimensional spectrum parallel to the energy-difference axis within the energy-sum segment (1022 – 2.4) keV < $E_1 + E_2$ < (1022 + 2.4) keV of each sample is then divided by an area-normalized identical spectrum obtained for a pair of pure (99.999%) Al single crystalline samples prior annealed at 625 °C for 2 h in vacuum (p < 10-5 mbar).

2.2 Characterization

Powder x-ray diffraction (XRD) patterns were recorded on a PANalytical MPD instrument using an Xcelerator detector and a Cu Kα radiation source at a working power of 45 kV and 40 mA. For optical absorption measurements, the powder samples were dispersed in spectroscopic grade ethanol using an ultrasonicator and the absorption spectra were recorded with a spectro-photometer (Cary 50). Total reflectance x-ray fluorescence spectroscopy (TXRF) was performed to obtain the actual Ce:Eu concentration of the samples using a Bruker S2 Picofox instrument.
3. Results and discussion

A set of undoped and europium doped cerium oxide nanoparticles were synthesized by a simple one step solvothermal process (See supporting information). The doping concentrations were varied from 0.1 atom% to 50 atom% which subsequently represented as CEX, where X = 0, 0.1, 0.5, 1, 5, 10, 20, 30, 40, and 50 atom%. Several complementary experiments had been performed to characterize the samples and estimate the particle sizes, lattice parameters, optical band gaps, luminosity of the emissions etc. These are summarized below.

![X-ray diffraction patterns](image)

**Fig. 1** Typical x-ray diffraction patterns of the undoped and some of the Eu-doped cerium oxide nanocrystalline samples.

Some of the illustrative XRD patterns are shown in Fig. 1. The well-defined peaks corresponding to reflections of the expected fluorite phase are described in the figure. The peak widths indicate that the samples are nanocrystalline in nature. The crystallite sizes ($d_c$) were estimated using Scherrer formulism.\(^{21}\) Fig. 2 shows an expected decrease of crystallite size with increasing concentration of Eu\(^{3+}\), although it increases during the change of concentration from...
0.1 to 1%. The decrease in crystallite size suggests that the dopant introduces significant lattice strain (the ionic radius of Eu$^{3+}$ (1.07 Å) is about 10% larger than that of Ce$^{4+}$ (0.97 Å)) and this reduces ion transport and sintering as noted previously for doped CeO$_2$. The increase in crystallite size seen between 0.1 and 1% doping concentration may be explained by the creation of charge compensating anion vacancies which will tend to increase oxygen ion mobility favoring sintering.

![Graph showing particle size vs. concentration of Eu.](image)

**Fig. 2** The average particle sizes in the undoped (shown against a concentration 0.01 subsequently) and the Eu-doped CeO$_2$ samples.

We have also verified from total reflectance x-ray fluorescence (TXRF) data that the actual concentration of Eu in the sample is significantly less than that might be expected from concentrations in the mother liquor. Similar effects have been previously reported by us and are ascribed due to limited solubility of the trivalent oxides in strongly basic conditions. Fig. 3 illustrates the actual amount of Eu incorporated into the solid against dopant concentration in solution. As the solution concentration of Eu increases, the effectiveness of incorporation decreases. At the highest dopant concentrations, quite large increases in solution concentration
have little effect on the solid concentration. As well as complex solution effects, the data might also suggest high surface concentrations since the TXRF technique is not surface sensitive.

**Fig. 3** The percentage (relative to the target concentration) of Eu incorporated in CeO$_2$ at different solution concentrations of Eu determined by total reflectance x-ray fluorescence studies.

The lattice parameter $\alpha$ of the different samples, undoped and doped, were estimated as

$$\alpha = d\sqrt{h^2 + k^2 + l^2}$$

(1)

where the interplanar separation $d$ is obtained from the Bragg relation $2d \sin \theta = n\lambda$. Fig. 4 shows unexpected trends of the lattice parameter with the dopant concentration. The lattice parameter of the samples with higher concentrations of doped Eu is obviously larger than the ones with lower Eu concentration. However in the region [Eu] = 0.1 to 1% where an increase in particle size had been earlier observed (Fig. 2), there is a complex dependence of lattice parameter and dimension.
Fig. 4 The lattice parameters ($\alpha$) of the undoped and Eu-doped CeO$_2$ samples.

Fig. 5(a) presents a semi-log plot of the two quantities showing that the lattice parameter steadily increases with decrease in nanoparticle sizes. A relationship can be obtained between the change in lattice parameter $\Delta \alpha$ with respect to the lattice parameter of bulk CeO$_2$ (5.410Å) and the particle size $d_c$ in a log-log plot (Fig. 5(b)) as

$$\log (\Delta \alpha) = -1.7437 \log(d_c) - 0.4947$$  \hspace{1cm} (2a)

or

$$\Delta \alpha = 0.32 \ d_c^{-1.7437}$$ \hspace{1cm} (2b)

The relation is however markedly different from a similar relation obtained earlier by Deshpande et al.$^{24}$ The differences could be attributed to the cause of lattice parameter variation, i.e., doping by Eu in the present case versus crystallites of different sizes of undoped CeO$_2$ in the said work.
Fig. 5 (a) A plot of the lattice parameter ($\alpha$) versus size of the nanoparticles in the undoped and the Eu-doped CeO$_2$ samples. (b) The change in lattice parameter ($\Delta\alpha$) versus size of the nanoparticles in the undoped and the Eu-doped CeO$_2$ samples.

Fig. 6 Optical absorption spectra of the undoped and a few of the Eu-doped CeO$_2$ samples.
The optical properties of CeO$_2$ also showed an unusual variation in the bad gap energy ($E_g$) with Eu doping and, consequently, crystallite size. Typical data are given in Fig. 6 as optical absorption spectra. $E_g$ can be calculated using:

$$\alpha h\nu = A(h\nu - E_g)^n$$

(3)

where $A$ is a constant, $h\nu$ is the photon energy and $n$ depends on the nature of transition ($n = 1/2$ for direct transition and 2 for indirect transition).$^{25,26}$ CeO$_2$ is a direct band gap semiconductor and therefore the optical band gap for the samples can be obtained by extrapolating the linear portion of the $(\alpha h\nu)^2$ vs. $h\nu$ curve to zero. The error in the determination of the band gap energy due to the fitting procedure was estimated ~2 meV. The $E_g$ as a function of Eu concentration and crystallite size is shown in Fig. 7(a) and (b) respectively and displays a clear maximum around 6-7 nm. It is suggested that this is due to two opposing effects. Firstly, as the Eu content increases (and size generally decreases as described above), the apparent value of $E_g$ decreases because of the creation of additional energy levels within the band gap of the undoped sample. However, as the size decreases (i.e. Eu content increases) there is a tendency towards higher $E_g$ values because of quantum confinement effects expressed by the relationship$^{27}$

$$E_g(nano) - E_g(bulk) = \frac{\hbar^2 \pi^2}{2er^2} \left( \frac{1}{m_e m_0} + \frac{1}{m_h m_0} \right) - \frac{1.8e}{4\pi\varepsilon_0 r}$$

(4)

Here $r$ represents the radius, $m_0$ is the electron mass and $m_e$ and $m_h$ are the relative effective masses of the electron and hole respectively. Li et al.$^{28}$ reported that the exciton Bohr radius for CeO$_2$ is 7-8 nm and hence quantum confinement effects including increased band gaps would be seen at and below this value. Interestingly, the increase in $E_g$ seen at low dimension occurs around this size as clearly seen in the Fig. 7(b). Similar changes in the band gap $E_g$ have been seen in nanosized CdS particles.$^{29}$ The overall decrease of the band gap energy with decreasing particle
size is to be understood as due to electron–phonon coupling phenomenon\textsuperscript{30} and the effect dominates over quantum confinement when the particle size decreases further below 6.09 nm.

Fig. 7 (a) The calculated band gap energies of the undoped and Eu-doped CeO\textsubscript{2} samples (b) The same versus size of the nanoparticles in the undoped and the Eu-doped CeO\textsubscript{2} samples.

The above data clearly detail the response of the host ceria fluorite lattice to Eu ion inclusion. However, the defect mechanism associated with this process has not been discussed. It is clear that the number of vacancies will increase with Eu doping to charge compensate the 3+ states substituting for 4+ lattice cations. Less clear is an understanding of Ce\textsuperscript{3+}-vacancy combinations that might be formed as a result of lattice and other energy changes resulting from Eu inclusion. Positron annihilation studies might prove useful as defect sites can act as positron trapping sites and authors such as Liu et al have demonstrated the usefulness of this spectroscopic method.\textsuperscript{31} The results of the present investigation are shown in Fig. 8(a) to (e). These results show distinct differences from those of Liu et al on pristine ceria materials. As in earlier work, three different components of positron lifetime were observed in all the samples. The lifetimes are labelled as $\tau_1$, $\tau_2$ and $\tau_3$ in increasing order of their magnitudes and their relative intensities are named as $I_1$, \[ \begin{align*}
\text{Band gap (E}_g\text{) (eV)} & \quad \text{Concentration of Eu (%)} \\
3.35 & \quad 0.01 \\
3.30 & \quad 0.1 \\
3.25 & \quad 1 \\
3.20 & \quad 10 \\
3.15 & \quad 100 \\
\end{align*} \]
$I_2$ and $I_3$ respectively. As can be seen in the data, the variation of each lifetime component with Eu concentration is similar suggesting some interaction between the states.

The longest component, $\tau_3$, can be assigned to the formation of orthopositronium atoms in the free volume separating the nanoparticles since positron in such extended defects will have very long lifetimes due to the temporary bound states formed. Although the intensities ($I_3$) are very small, they were needed to be included in the data analysis to adequately fit the data and since they follow the same pattern of variation as the other positron lifetime parameters, their presence cannot be ignored.

**Fig. 8** The positron lifetimes (a) $\tau_1$, (b) $\tau_2$ and (c) $\tau_3$ and intensities (d) $I_2$ and (e) $I_3$ versus the concentrations of Eu doping in the CeO$_2$ nanocrystalline samples. The values shown against 0.01 stand for the undoped sample.
The intermediate positron lifetime $\tau_2$ is not typical of other single lifetime features seen in bulk materials and it is suggested that this lifetime is assignable to Ce$^{3+}$-vacancy combination sites within the nanocrystallites. The values of $\tau_2$ (> 400 ps) would suggest the presence of large size voids or vacancy clusters, but this is inconsistent with the structure of dense nanocrystallites as described above. Since the size of the nanocrystallites formed here are below the thermal diffusion length of positrons in typical metallic oxides (~ 50-100 nm), it could be suggested that $\tau_2$ is the lifetime based around contribution from surface positron annihilation and a defect specific lifetime. However, since the variation of $\tau_2$ is quite similar to that of the other parameters, $\tau_1$ and $\tau_3$, changes taking place in the crystal structure may also have important bearing on its values and variation.

Notably, significant difference between the shortest positron lifetime $\tau_1$ and those previously reported can be seen.\(^{31}\) Liu et al had attributed $\tau_1 \sim 236$-247 ps to neutral Ce$^{3+}$-oxygen vacancy associates. Here in this work, the magnitudes of $\tau_1$ are smaller ($\tau_1 \sim 172$-179) and their variations are also relatively less. They are also significantly less than those reported in other works that have assigned the same lattice defect where values of $\tau_1 \sim 262$ ps\(^{32}\) and $\tau_1 \sim 187.9$-211.1 ps\(^{33}\) have been reported. Although the mean positron lifetime (defined later) may differ by small amounts due to differing sample conditions, the differences between this work and the previous ones would suggest that $\tau_1$ contribution is not due to those types of defects and instead we suggest that the shortest lifetime $\tau_1$ is related to free positrons, i.e., those which do not get trapped by the vacancy defects within the nanoparticles. Note, that these are not typical of bulk lifetimes ($\tau_b$) since the crystallites are so small that free positrons can diffuse to the surface where they are annihilated. Further $\tau_1$ shows a small qualitative variation (Fig. 8(a)) similar to that of $\tau_2$ and it is posited that a minor contribution to $\tau_1$ may arise from the Bloch-state residence time of trapped positrons, in accordance with the positron trapping model.
According to the two-state positron trapping model,\textsuperscript{34}\ i.e., a situation where there is only one dominant type of positron trapping sites (i.e. a Ce\textsuperscript{3+}-oxygen vacancy associates), the positron trapping rate $\kappa$ for the ‘bulk-like state’ is given by the relationship:

$$
\kappa = \frac{1}{\tau_1} - \frac{1}{\tau_b}
$$

(5)

where the lifetime $\tau_b$ of positrons annihilating in bulk crystals of CeO\textsubscript{2} is taken as 187 ps (Chang et al\textsuperscript{32}). But the positron trapping rate when derived from the measured positron lifetimes should also satisfy the relationship

$$
\kappa_{exp} = I_2 \left( \frac{1}{\tau_1} - \frac{1}{\tau_2} \right)
$$

(6)

For all concentrations of Eu, the data suggest that $\kappa_{exp} > \kappa$. As suggested above, the defect related lifetime $\tau_2$ is larger (394-423 ps) than expected for a cerium-anion vacancy combination (i.e. not all positrons with lifetime $\tau_2$ and intensity $I_2$ are providing Bloch-state residence time) and it can be suggested that the majority of positrons are being annihilated at the nanoparticle surfaces. Note that $\kappa_{exp}$ can be reduced to $\kappa$ either by assuming smaller values of $\tau_2$ or alternatively decreasing $I_2$ by a factor $\kappa/\kappa_{exp}$. The first option is unlikely since $\tau_2$ is determined by the concentration of positron trapping vacancy clusters and this is unlikely to be significant in these small particles. It is more reasonable to assume that a fraction $(\kappa/\kappa_{exp})I_2$ of positrons is annihilated in vacancy clusters within the nanoparticles and reduce $\tau_b$ to $\tau_1$ by admixing the Bloch-state residence time with it.

The experimentally measured $\tau_2$ can be expressed as a linear combination of positron lifetime at the defect vacancy ($\tau_{\text{vacancy}}$) and the positron lifetime at surface ($\tau_{\text{surface}}$) as:

$$
\tau_2 = \frac{\tau_{\text{vacancy}} I_{\text{vacancy}} + \tau_{\text{surface}} I_{\text{surface}}}{I_{\text{vacancy}} + I_{\text{surface}}}
$$

(7)
where $I_{\text{vacancy}} = (\kappa / \kappa_{\text{exp}}) \quad I_2$, $I_{\text{surface}} = I_2 - I_{\text{vacancy}}$ and $\tau_{\text{surface}}$ can be estimated as 450 ps, the typical saturation lifetime of positrons at surfaces of metals and metallic oxides.

**Fig. 9** (a) The derived positron lifetime in vacancy-type defects $\tau_{\text{vacancy}}$ of the undoped (shown against a concentration 0.01) and the Eu-doped CeO$_2$ samples. (b) The same versus size of the nanoparticles in the undoped and the Eu-doped CeO$_2$ samples.

The results of this analysis are summarized in Fig. 9(a) and (b). The magnitudes of the defect related lifetime show two distinct ranges. In the range from $[\text{Eu}] = 0$ to 1%, $\tau_{\text{vacancy}}$ is approximately constant within 277-293 ps and its values are typical of the positron lifetime in Ce$^{3+}$-oxygen vacancy associates and monovacancies as reported by others.$^{31-33}$ Beyond this concentration, it increases monotonously to values 325-330 ps. Significantly, these observations are consistent with the reports available in literature.$^{31-33}$ It is also noteworthy to mention that $\tau_{\text{vacancy}}$ does not exhibit any explicit dependence on the particle size (Fig. 9(b)). For example, the positron lifetime fell considerably from 302 ps to 273 ps when the particle size varied rather little (4.8 to 4.86 nm only) although this change was caused by an increase in the dopant Eu concentration from 5 to 30%. On the other hand, during the increase of particle size from 4.86 to 7.75 nm, the positron lifetime
changed by about 20 ps only and even the final decrease by about 16 ps took place when the particle size varied only from 7.75 to 8.77 nm. This means that the change in positron lifetimes, which signifies a change in the defect characteristics (i.e., size or environment), is dependent on the dopant concentration and is less sensitive to the sizes of the nanoparticles. This observation is in sharp contrast to the results illustrated in Fig. 7(a) and (b) in which the quantum confinement was shown essentially as a finite size effect and less dependent on the dopant concentration.

The variation of the positron lifetimes and their intensities with Eu doping and also with the sizes of the nanoparticles can give further information on the evolution of defects and their interaction with the doped ions. The value of $\tau_{\text{vacancy}} = 277$ ps in the undoped sample is larger than the lifetime $\tau_0 = 187$ ps of positrons annihilating in bulk crystals of CeO$_2$ by about just 90 ps, which is the typical enhancement in positron lifetime due to trapping in monovacancies. Hence, the positron trapping defects in the undoped sample can be reasonably understood to be of the monovacancy-type within the lattice (i.e., an isolated small polaron state associated with anion vacancy production). The polaron states are generally very strong trapping centres for positrons and should therefore have short lifetimes. On addition of Eu, the additional anion vacancies may allow delocalization of the electrons and, hence, increase of the positron lifetimes. At high Eu concentrations, it seems likely that defect clusters are produced and this results in significant increase in the lifetimes. Although there are no reported values of positron lifetimes in vacancy clusters of CeO$_2$, similar enhancement in other materials suggests that the values $\tau_2 = 325$-330 ps when compared to $\tau_2 = 187$ ps correspond to vacancy cluster defects consisting of about 4-5 monovacancies. At lower concentrations of doping, since Ce ions were in the 4+ state, the replacement by Eu$^{3+}$ ions creates charge imbalance and formation of an oxygen vacancy which is positively charged. In the region of concentration [Eu] = 0.1 to 1% it would appear that, these
anion vacancies are associated with Ce\(^{4+}\) ions (effectively reduction to Ce\(^{3+}\)) and Ce\(^{3+}\)-vacancy clusters or associates are formed. With further increase in the doping concentration, these isolated small associates will agglomerate to form the larger vacancy clusters that results into the very sharp rise of \(\tau_2\) to 325-330 ps, as shown here. It might be conjectured that these larger associates are similar in structure to local regions of the M\(_2\)O\(_3\) structure consisting of Ce\(^{3+}\) and Eu\(^{3+}\) metal ions.

As already pointed out, the region of doping [Eu] = 0.1 to 1\% is of particular interest since it is associated with an intermittent increase of particle sizes (Fig. 2) and lattice contraction (Fig. 4). The calculated vacancy-sensitive lifetime \(\tau_{\text{vacancy}}\) showed little change in this region (Fig. 9(a)) whereas the measured positron lifetimes \(\tau_1\), \(\tau_2\) and \(\tau_3\) fall in this region and the intensities \(I_2\) and \(I_3\) increase. It is, therefore, tempting to assign changes in the measured lifetimes as being due to changing surface effects which appear to cause the apparent high value of \(\tau_2\). It is suggested that the first decrease in lifetime seen at low [Eu] = 0.1\% concentration is associated with the lattice contraction mentioned above. There is then an increase in \(\tau_2\) which is probably associated with the increased values of \(\tau_{\text{vacancy}}\). This could be also supported by the nanocrystallite size reduction which allows more rapid movement of positrons to the nanocrystallite surface. The initial decrease of the intensities \(I_2\) and \(I_3\) stems from the lattice expansion effects where the decreasing electron density will reduce the probability of annihilation. Conversely, when the lattice contracts, the intensities would increase. This appears to be true as seen in Figs. 8(d) and (e). Further, when the crystallite sizes decrease, it would enhance the number of positrons diffusing to the surfaces and the widening of the intercrystallite region would cause more orthopositronium atoms to form and then undergo pick-off annihilation with the typical lifetimes as shown in Fig. 8(c).
CDBS experiments can provide clarity on changes to the electron momentum distribution in the samples and how positrons develop affinity to these changes. After recording the gamma ray events $E_1$ and $E_2$ from the two high sensitive HPGe detectors and noting their time correlations, a two-parameter spectra is generated with $E_1 + E_2$ and $E_1 - E_2$ in the two coplanar axes and counts distributed accordingly.\textsuperscript{23,24} The projected one-dimensional spectrum parallel to the energy-difference axis within the energy-sum segment $(1022 - 2.4) \text{ keV} < (E_1 + E_2) < (1022 + 2.4) \text{ keV}$ of each sample is then divided by an area-normalized identical spectrum obtained for a pair of pure (99.999\%) Al single crystalline samples prior annealed at 625 °C for 2 h in vacuum ($p < 10^{-5}$ mbar). The quotient spectra generated for all the samples are shown in Fig. 10. The individual features represent positron annihilation events (via interaction with the core electrons of oxygen ions surrounding the cationic vacancies and their clusters) within the samples. The series of the peaks at different momentum appear at $p_L (10^{-3} \text{m}_0 \text{c}) = 9.4, 23.5, 32.1, 39.2$ and $43.1$. The features at different positions probably reflect different local structural arrangements of vacancies and the cations ranging from simple, isolated point defects to complex 3D structural arrangements within clusters of defects. Similar features and positions are seen in all samples, but the relative amplitudes of each feature change from sample to sample.
Fig. 10 The ratio curves or quotient spectra of the different samples with respect to the spectrum of reference Al.

Fig. 11 The variation of the amplitudes of the different peaks in the CDB spectra of the samples. For the sake of clarity, the amplitudes have been vertically shifted by 0.5 (P23.5), 0.75 (P32.1), 1.0 (P39.2) and 1.25 (P43.1).
The above argument is based on the elemental or ionic sites that are probable in the crystal structure of the Eu-doped CeO$_2$ or Ce$_2$O$_3$. While the peaks appear at the same values of $p_L$ in all the samples, there are differences in the amplitudes of the peaks for the different samples. The variations in these amplitudes are illustrated in Fig. 11 and these can be used to further understand the defect mechanism outlined above. In the initial stage of doping, i.e., from the undoped to the 0.1%-doped sample, the amplitudes increase indicating increased annihilation of positrons. We suggest that this is due to the decreasing particle size at this stage which increases positron annihilation at surface states. The succeeding doping interval 0.1 to 1% is the region where the particle size has increased again (Fig. 2). The opposite effect is, therefore, reflected in the amplitudes. Between 1% and 20% Eu loading, there is a general increase in amplitude for the low momentum states indicating increased anion vacancy addition. This increase (to around 10% loading) is seen only at low momentum whereas at high momentum, continued decreases are seen. This may be because these states are more sensitive to clusters of defects which are only present at higher dopant levels and we suggest that high momentum features are due to anion defect clusters and the low momentum states due to isolated defect states.

Between 20% and 40% loading levels, there is a decrease in positron annihilation for all features. It is posited that this decrease is due to the change in stoichiometry of the oxide which is tending towards M$_2$O$_3$ rather than MO$_{2-x}$ at these loadings and the structure becomes progressively less defective. However, this region is also characterized by the partial reduction of CeO$_2$ to Ce$_2$O$_3$ by the formation of oxygen vacancy and hence the decrease is partly arrested in the case of the peaks at high momentum values (i.e., 32.1, 39.2 and 43.1). In the region from 1% to 40% of Eu doping, the particle sizes reduce again and the lattice expands due to further reduction of Ce$^{4+}$ to Ce$^{3+}$. While Ce$^{4+}$ has eight coordinated O$^{2-}$ ions, it decreases to seven when reduced to Ce$^{3+}$ and
hence oxygen vacancies further enrich the lattice. Since oxygen vacancies are positively charged, positron trapping is reduced at this stage.

The drastic fall in amplitude of the peak at \( p_L (10^{-3} m_0 c) = 43.1 \) testifies to this argument. A rather unusual trend is seen at [Eu] = 50% where all the amplitudes fall down and this may be an indication of segregation of unincorporated Eu\(^{3+}\) ions and additional doping may result into the development of new phases, as had been seen in a similar case earlier.\(^{35}\)

The S-W plot also indicated the quantum confinement effect through a peak-like kink in the curve, indicating the sensitivity of positron annihilation as a technique and the various parameters derived from its data for better understanding of the defects-related aspects in nanocrystalline systems (See supporting information).

**Fig. 12** The S parameter versus W in ascending order of magnitude depicting the peak-like variation around the crystallite sizes where quantum confinement effects are prominent. The inset shows the full figure. The region around the peak is expanded in the main figure for clarity.
The $S$ parameter values when plotted against the corresponding $W$ in ascending order of the latter throws another interesting observation of a distinct kink-like variation in it, as shown in Fig. 12. Incidentally this happens for the same region of variation of the crystallite size where the indication of quantum confinement effects had been observed from optical absorption measurements (Fig. 7(b)). More systematic studies on samples with well-controlled particle sizes are required to comment further on the exact relationship between the fraction of low momentum electrons annihilated by positrons and the changing band gap in the crystallites.

4. Summary and Conclusions

The results of a detailed investigation carried out using several complementary experimental techniques on CeO$_2$ nanocrystalline samples doped with varying concentrations of Eu are presented in this paper. A notable observation is the decreasing particle size with increase in the concentration of doping but the trend is interrupted in medium concentrations of doping due to the reduction of Ce$^{4+}$ to Ce$^{3+}$ when an increasing concentration of oxygen vacancies resulted in an increase in particle size. The change in lattice parameter had the opposite trend and a linear relation was obtained between this and the particle size. Optical absorption measurements showed a decrease in band gap energy with increasing doping. However, quantum confinement effects being size related manifested in particles of dimensions exactly below the exciton Bohr radius, giving a characteristic blue shift in the optical absorption spectra. The vacancy type defects were investigated through positron lifetime and CDBS measurements. The intermediate particle size enhancement came as a result of the generation of additional oxygen vacancies in the samples and is indicated by a distinct change in the intensity of positrons trapped in the defects. The positron lifetime within the vacancies was delineated from that due to annihilation at the crystallite surfaces and it was found to enhance due to vacancy agglomeration at higher concentrations of doping. The
CDBS measurements demonstrated annihilations taking place with the electrons of ions of different charges and momentum distribution and the variation of the lineshape parameters derived from it further supported the findings from positron lifetime measurements.

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