<table>
<thead>
<tr>
<th>Title</th>
<th>Chimera states in networks of type-I Morris-Lecar neurons</th>
</tr>
</thead>
<tbody>
<tr>
<td>Author(s)</td>
<td>Calim, Ali; Hövel, Philipp; Ozer, Mahmut; Uzuntarla, Muhammet</td>
</tr>
<tr>
<td>Publication date</td>
<td>2018-12</td>
</tr>
<tr>
<td>Type of publication</td>
<td>Article (peer-reviewed)</td>
</tr>
<tr>
<td></td>
<td><a href="http://dx.doi.org/10.1103/PhysRevE.98.062217">http://dx.doi.org/10.1103/PhysRevE.98.062217</a></td>
</tr>
<tr>
<td>Access to the full text of the published version may require a subscription.</td>
<td></td>
</tr>
<tr>
<td>Rights</td>
<td>© 2018 American Physical Society</td>
</tr>
<tr>
<td>Item downloaded from</td>
<td><a href="http://hdl.handle.net/10468/7754">http://hdl.handle.net/10468/7754</a></td>
</tr>
</tbody>
</table>

Downloaded on 2019-08-03T23:42:48Z
Chimera states in networks of type-I Morris-Lecar neurons

Ali Calim,1,* Philipp Hövel,2,3 Mahmut Ozer,4 and Muhammet Uzuntarla1,†
1Department of Biomedical Engineering, Bulent Ecevit University, Zonguldak, Turkey
2School of Mathematical Science, University College Cork, Cork T12 XF64, Ireland
3Institut für Theoretische Physik, Technische Universität Berlin, Hardenbergstraße 36, 10623 Berlin, Germany
4Department of Electrical and Electronics Engineering, Bulent Ecevit University, Zonguldak, Turkey

(Received 3 September 2018; revised manuscript received 8 November 2018; published 21 December 2018)

Chimeras are complex spatiotemporal patterns that emerge as coexistence of both coherent and incoherent groups of coupled dynamical systems. Here, we investigate the emergence of chimera states in nonlocal networks of type-I Morris-Lecar neurons coupled via chemical synapses. This constitutes a more realistic neuronal modeling framework than previous studies of chimera states, since the Morris-Lecar model provides biophysically more relevant control parameters to describe the activity in actual neural systems. We explore systematically the transitions of dynamic behavior and find that different types of synchrony appear depending on the excitability level and nonlocal network features. Furthermore, we map the transitions between incoherent states, traveling waves, chimeras, coherent states, and global amplitude death in the parameter space of interest. This work contributes to a better understanding of biological conditions giving rise to the emergence of chimera states in neural medium.

DOI: 10.1103/PhysRevE.98.062217

I. INTRODUCTION

Synchronization is widely assumed to be essential for the proper functioning of a large variety of natural and artificial systems, ranging from physical experiments to chemical reactions and physiological processes. Prime examples include coupled lasers [1], Josephson junctions [2], oxidation and catalytic surface reactions [3,4], genetic oscillator networks [5], and neural systems [6]. For decades, synchronization in neural systems has remained a very popular topic of research, because it is considered as a brain mechanism underlying many behavioral and cognitive functions, e.g., attention selection, information processing, and neural control of movement [7–11]. Furthermore, neural synchronization is proposed to be responsible for formation and dissolution of functional brain networks performing multiple vital tasks, such as visual perception, sleeping, and memory in the brain [12–14]. Considering its relative consequences, it is critical to understand how neural synchronization is organized or conserved and how it affects the neural information coding or propagation.

However, synchronized population activity is not perpetually desirable and pervasive in every region of the brain [15,16]. For instance, the cortex operates in a highly asynchronous state during waking and REM sleep, in which low-frequency oscillations, i.e., delta activity, are adequately inhibited [17]. The subthalamic nucleus, a specific location in the basal ganglia, is another example of this observation. It exhibits desynchronized electrical activity in the beta frequency band as an indicator of movement preparation [18]. In some cases, these two common states, namely, synchronization and desynchronization, could be present within the same neuronal circuitry at the same time [19,20]. Several recent experimental and clinical studies confirm that such a coexistence occurs in the brain, more specifically during unihemispheric sleep [21,22], epileptic seizures [23,24], and bump states [25,26] observed in in vitro preparations. The idea first surfaced in the pioneering work of Kuramoto, in which this surprising collective behavior was studied in identical phase oscillators with nonlocal interactions [27]. Following the first report of such an intriguing hybrid behavior, Abrams and Strogatz named this emergent dynamical phenomenon chimera state [28]. In chimeras, coupled dynamical elements exhibit extraordinary spatiotemporal patterns splitting the system into two subpopulations: one synchronized and phase locked, the other desynchronized and incoherent. This symmetry-breaking behavior has been studied in a variety of complex dynamical systems and has attracted growing attention in neural system studies from both theoretical and experimental perspectives [28–31]. Aside from its experimental evidences in optical [32], chemical [33], mechanical [34,35], electronic [36,37], electrochemical oscillator systems [38–40], extensive theoretical and numerical studies exploring chimera states have only recently been carried out in the field of neuroscience [41–48].

Hizanidis et al. investigated chimera states in modular neural networks based on the connectome of Caenorhabditis elegans [49]. They showed that chimeralike states spontaneously emerge with a suitable tuning of electrical and chemical coupling strengths. Moreover, it was also reported that an important system component, which leads to emergence of chimeras, is the largest community in constructed modular networks. In another work, Majhi et al. analyzed chimera states in a two-layer neural network, considering

*ali.calim@hotmail.com
†muzuntarla@yahoo.com
Hindmarsh-Rose neurons coupled via electrical and chemical synapses [50]. They showed that the emergence of chimera states depends significantly on chemical synapses, not electrical ones. They also emphasized the importance of chemical synaptic transmission delays and illustrated that chimera states appear in a larger region in a two-dimensional parameter space (coupling range versus chemical synaptic strength) due to the increasing values of delay in the synaptic transmission between the layers. Omelchenko et al. studied robustness of chimera state adding heterogeneity into single neuron dynamics and network topology [51]. They demonstrated that chimera state maintains in the system of inhomogeneous FitzHugh-Nagumo neurons with nonlocal coupling topology by introducing small diversities into intrinsic cellular properties. They also showed that random structural irregularities of the network topology do not destroy the chimera state up to a certain limitation of random links.

It is well known from experimental and theoretical studies that one of the most important intrinsic features of neural dynamics is excitability [52–55]. It plays a basic but important role in achieving biological functions of the nervous system by determining firing and resting behaviors. In fact, the excitability is determined by a bifurcation parameter that changes the dynamic behavior of a neuron from a quiescence state to a regularly spiking regime. In this sense, neurons are mainly classified into two types according to frequency response characteristics to a constant bias current: type-I excitability with a continuous frequency versus bias current curve related to a saddle-node infinite-period bifurcation of equilibria and type-II excitability with a discontinuous frequency versus bias current curve connected to a Hopf bifurcation. At the bifurcation point, neurons of type-I excitability begin to exhibit self-sustained oscillation with an almost zero frequency. In contrast, type-II neurons switch from quiescence state to repetitive firing with a finite frequency. Apart from the firing frequency as a response to an external bias current, type-I and type-II neurons differ in several ways, such as their changes the dynamic behavior of a neuron from a quiescence state to a regularly spiking regime. In this sense, neurons of type-I excitability has been considered only with a generic neuron model, the saddle-node infinite period oscillator [59]. To introduce small diversities into intrinsic cellular properties of chimera state adding heterogeneity into single neuron dynamics and network topology [51]. They demonstrated that chimera state maintains in the system of inhomogeneous FitzHugh-Nagumo neurons with nonlocal coupling topology by introducing small diversities into intrinsic cellular properties of the network topology do not destroy the chimera state up to a certain limitation of random links.

The vast majority of chimera studies in the neuroscience literature to date have focused on the emergence of this state in neural systems of type-II excitability. Chimera state has been detected and deeply analyzed in populations of FitzHugh-Nagumo [57] and Hindmarsh-Rose [58] neurons, which are prominent models for this class of neural excitability. However, chimera research on neural systems with type-I excitability has been considered only with a generic neuron model, the saddle-node infinite period oscillator [59]. To ensure biophysical relevance and achieve realistic modeling, taking into account ion current dynamics is crucial for neural systems which would potentially evolve into chimera state since above-mentioned phenomenological neuron models do not involve ion currents and gating features.

In this paper, we address this issue and report for the first time the emergence of chimera state in a nonlocally coupled neural population of Morris-Lecar model exhibiting type-I excitability but not bistability. As for the synaptic communication within the network, excitatory chemical coupling scheme is considered. Using this modeling framework, we show the existence of peculiar chimera state as well as other emergent system regimes (incoherent state, traveling wave, coherent state and global amplitude death) by exclusively scanning the excitability level of individual units and the interaction intensity in nonlocal network associated with coupling range and synaptic strength.

The rest of the paper is organized as follows: In the next section, we introduce the model, that is, a set of $N$ nonlocally coupled Morris-Lecar neurons, and the methods used for the characterization of chimera states in terms of firing frequency and strength of incoherence. Section III includes the main results and frames the conditions for the appearance of chimera states. In Sec. III A, we present a bifurcation analysis of the Morris-Lecar model. In Sec. III B, variation of dynamical behaviors was analyzed depending on the level of excitability. In Sec. III C, the influences of nonlocal network features on the appearance of chimera states were investigated and explained by producing detailed parameter maps that reveal the behavioral transitions between different network states. Furthermore, we went into a minute examination of chimeric behavior to identify its key characteristics. Finally, the main conclusions are summarized in Sec. IV.

II. MODELS AND METHODS

We consider a nonlocal network of Morris-Lecar neurons coupled with excitatory chemical synapses. The membrane potential of a neuron in the network is modeled based on the two-variable Morris-Lecar equations as follows [60–63]:

$$
\frac{dV_i}{dt} = g_C m_i^n (E_C - V_i) + g_K w_i (E_K - V_i) + g_L (E_L - V_i) + I_0 + I_i^\text{syn},
$$

$$
\frac{dw_i}{dt} = \phi (w_i^n - w_i) \cosh \left( \frac{V_i - \beta_w}{2 \gamma_w} \right),
$$

$$
\frac{m_i^n (V_i)}{dt} = 0.5 \left[ 1 + \tanh \left( \frac{V_i - \beta_m}{\gamma_m} \right) \right],
$$

$$
\frac{w_i^n (V_i)}{dt} = 0.5 \left[ 1 + \tanh \left( \frac{V_i - \beta_w}{\gamma_w} \right) \right],
$$

where $i = 1, 2, \ldots, N$ is the neuron index, $V_i$ denotes the membrane potential, and $I_0$ is the externally applied bias current. $w_i$ and $m_i^n$ are the fraction of open $K^+$ and $Ca^{2+}$ channels, respectively. $C, \phi, \beta_m, \gamma_m, \beta_w$ and $\gamma_w$ are constants. $g_C, g_K$ and $g_L$ represent conductances for calcium, potassium and leak channels, respectively. $E_C$, $E_K$ and $E_L$ denote the corresponding equilibrium potentials (see Table I). Last, $I_i^\text{syn}$ denotes the total synaptic current received by neuron $i$ from its nonlocal interactions.

| TABLE I. Morris-Lecar model parameters for type-I excitability. |
|-----------------|-----------------|-----------------|-----------------|
| $g_C$ = 1 mS/cm² | $g_K$ = 2 mS/cm² | $g_L$ = 0.5 mS/cm² |
| $E_C$ = 100 mV | $E_K$ = -70 mV | $E_L$ = -50 mV |
| $\beta_m$ = -1 mV | $\beta_w$ = 10 mV | $C = 1 \mu F/cm²$ |
| $\gamma_m$ = 15 mV | $\gamma_w$ = 14.5 mV | $\phi = 1/3$ |
Transmission of an electrical stimulus from a presynaptic neuron to a postsynaptic cell takes place in either electrical or chemical synapses. Based on their electrophysiology, these can be defined as linear and nonlinear coupling, respectively. In an electrical synapse, ions flow directly from one cell into another and the synaptic activity is bidirectional. In a chemical synapse, however, the signal transmission occurs into another and the synaptic activity is unidirectional. In an electrical synapse, ions flow directly from one cell to another and the synaptic activity is bidirectional. In a chemical synapse, however, the signal transmission occurs into another and the synaptic activity is unidirectional.

The total excitatory synaptic current is calculated by summing the basis of the interaction dynamics in our system setup.

In what follows, we investigate competing dynamical behaviors in chemically coupled nonlocal networks of Morris-Lecar neurons. We begin with a brief review of the bifurcation analysis of the Morris-Lecar model.

A. Bifurcation analysis of a type-I Morris-Lecar neuron

Figure 1 shows the bifurcation diagram and the firing frequency response of Morris-Lecar model as a function of applied constant bias current $I_0$. In Fig. 1(a), stable (unstable) equilibria corresponding to quiescence states are represented by solid (dashed) lines, whereas stable (unstable) limit cycles corresponding to repetitive firing are shown with filled (empty) circles marking the minimal and maximal membrane voltage amplitudes. Using the parameter set given in Table I, repetitive spiking arises through a saddle-node on invariant circle (SNIC) bifurcation at $I_0 = 8.33 \mu A/cm^2$. In this bifurcation point, the periodic oscillations, what is referred to as limit cycle, appear with finite amplitude as the saddle and node annihilate. As a result, there exists only an unstable equilibrium surrounded by a stable limit cycle. In this setup, the neuron cannot exhibit bistability. The limit cycles vanish through a saddle-node (SN) bifurcation of the spiking attractor at $I_0 = 24.18 \mu A/cm^2$, followed by a subcritical Hopf (HB) bifurcation of the equilibrium at $I_0 = 20.37 \mu A/cm^2$ as shown in Fig. 1(a). One can infer the consequences of these bifurcations from Fig. 1(b), which shows the $(I_0, f)$ curve of the model. It can be clearly noticed that the neuron starts firing with an arbitrary low firing frequency, and the firing frequency rapidly and continuously increases with the increase in the applied bias current over a wide range. As one of the distinctive characteristic properties, this indicates that the neuron is of type-I excitability, which resembles the dynamic behavior of excitatory pyramidal neurons in the cortex [71] that can fire at very low frequency for sustained inputs.
B. Influence of excitability level on population behavior

Next, we investigate the emergence of chimera states with the variation of excitability level accessible by the bias current parameter $I_0$. To do so, we consider $N = 1000$ nonlocally coupled identical Morris-Lecar neurons with fixed coupling radius $r = 0.1$ and synaptic strength $g = 0.1 \text{ mS/cm}^2$, and picture population behavior by varying $I_0$. Obtained results are presented in Fig. 2 where each column illustrates the space-time plots (top panels) and typical snapshots of membrane potentials (middle panels) as well as corresponding average firing frequency profiles (bottom panels) of a given population that is subjected to a fixed $I_0$. It is seen that the system under study exhibits characteristically distinct types of dynamical behaviors as $I_0$ varies. More precisely, we observe an incoherent state for $I_0 = 8 \mu \text{A/cm}^2$ at which all the neurons fire asynchronously with the same firing frequency [see Fig. 2(a)]. Population starts to exhibit traveling wave patterns as shown in Fig. 2(b) with a slight increase in $I_0$ which is set to $10 \mu \text{A/cm}^2$. Then, a further increase in bias current to $11 \mu \text{A/cm}^2$, we observe the chimera state in which the population splits into two domains: coherent and incoherent subpopulations. Top and middle panels illustrating different projections of the population activity in Fig. 2(c) confirm the coexistence of synchronization and desynchronization states within the same population. An arc-shaped average firing frequency profile shown in bottom panel is also another indicator for the emergence of chimera state in a population of type-I Morris-Lecar neurons. To check the persistence of such special behavior, we further increased $I_0$ and observed that the chimera state does no longer exist, instead a coherent state [Fig. 2(d)] and a global amplitude death [Fig. 2(e)] emerge for $I_0 = 15 \mu \text{A/cm}^2$ and $I_0 = 22 \mu \text{A/cm}^2$, respectively. It can be seen that the population exhibits fully synchronized firings with increased rates in the case of coherent state whereas the coupled neural system is void of oscillations and exhibits a single stable steady state at the emergence of a global amplitude death.

To clearly distinguish these different types of population behaviors and characterize the effect of excitability on their arisals, we compute the $S$ measure as a function of $I_0$ for fixed network parameters. The obtained results are presented in Fig. 3. As seen in the figure, a sweep from subthreshold values of $I_0$ to suprathreshold levels induces five different dynamic behaviors marked by different colors. Note that their respective dynamics were previously illustrated in Fig. 2. Based on extensive simulations, we determine a transition line between traveling waves and chimera states at $S \approx 0.5$, which splits the parameter region between incoherence state at $S = 1$ and coherence state at $S = 0$ into two distinct divisions. If the applied bias current is chosen in the range of $8 \mu \text{A/cm}^2 < I_0 < 9.25 \mu \text{A/cm}^2$, we observe that it gives rise to incoherent neural activity, even though it includes insufficient forcing. After the first dynamic behavior threshold, we see traveling waves in the range of $9.25 \mu \text{A/cm}^2 < I_0 < 10.5 \mu \text{A/cm}^2$. Subsequently, the neural population exhibits chimera states in the applied bias current range of $10.5 \mu \text{A/cm}^2 < I_0 < 12.75 \mu \text{A/cm}^2$. Eventually, beyond this point, system operates in a coherent state, because the system units are exposed to a sufficiently high bias current. Through the higher excitability levels attained by $I_0 > 20 \mu \text{A/cm}^2$, the system exhibits global amplitude death state due to hypersynchronization in the network. Our findings indicate that a population of type-I Morris-Lecar neurons may exhibit different types of synchrony states, including a peculiar chimera behavior, and there are transition regions between them depending on excitability level of individual neurons.

C. Influence of nonlocal network features on population behavior

We have so far focused on changes in the excitability level to study the emergence of chimera states with fixed network features. In the following, we investigate population dynamics...
respective. Other system parameters are set as described in the caption of Fig. 2.

FIG. 2. Influence of the excitability level $I_0$ on the emergence of chimera states: Increasing the level of excitability gives rise to different system behaviors in nonlocally coupled identical neuron population, i.e., (a) incoherent state, (b) traveling wave, (c) chimera state, (d) coherent state, and (e) global amplitude death for $I_0 = 8 \mu A/cm^2$, $I_0 = 10 \mu A/cm^2$, $I_0 = 11 \mu A/cm^2$, $I_0 = 15 \mu A/cm^2$, and $I_0 = 22 \mu A/cm^2$, respectively. Other system parameters are as described in the caption of Fig. 2. Note that each column pictures the space-time plots (top panels) and typical snapshots of membrane potentials (middle panels) as well as corresponding average firing frequency profiles (bottom panels) for a given population that is subjected to a fixed $I_0$.

as functions of network coupling radius and synaptic coupling strength. As an extension of the findings about the effect of excitability level on the emergence of chimera states, we now consider four different synchrony states that are shown in Fig. 3 and first seek to determine the influence of network coupling radius in type-I Morris-Lecar neuron populations which operate in, namely, incoherent, traveling wave, chimera, and coherent states. For each case, we analyze the transitions of those behavioral states by varying the coupling radius $r$ for a fixed value of synaptic strength $g = 0.1 mS/cm^2$. Obtained results are given in Fig. 4 that shows variation of $S$ as a function of $r$ for different values of $I_0$. It is evident that coupling radius $r$ is a significant system parameter which plays a major role in determining the emergence of above mentioned synchrony states. For instance, in Fig. 4(a), variation of $r$ results in emergence of all synchrony states in the population operating with $I_0 = 8.5 \mu A/cm^2$ that has initially ensured incoherent state for $r = 0.1$ as illustrated in Fig. 3. It is seen that increasing network coupling radius gives rise incoherent, traveling waves, chimera and coherent states to occur when $r$ lies in the ranges of $0 < r < 0.12$, $0.12 < r < 0.28$, $0.28 < r < 0.34$ and $0.34 < r < 0.5$, respectively. However, these ranges are highly sensitive to changes in $I_0$, where the boundary location of each synchrony state tends to shift lower values of $r$ as $I_0$ increases. In addition to this, although the range of $r$ resulting in chimera state does not change very much, the range of $r$ becomes narrower for incoherent state and traveling waves and wider for coherent state. This indicates that chimera state is robust to variations in excitability level and coupling radius. It is also important to note that traveling waves vanish at very high excitability levels on $r$ plane [see Fig. 4(d)].

To present a broader perspective on chimera state and to confirm its robustness, we scan a wider interval for $I_0$ and show population behavior on $(I_0, r)$ plane as depicted in Fig. 5. It is clear that smaller values of coupling radius support rich population behavior emerging as five different dynamical states whereas larger values only favor coherent state and global amplitude death. Similarly, this is also valid for $I_0$, implying that the population exhibits these two later states with increased levels of excitability. Our results reveal that type-I Morris-Lecar neurons are keen on to become synchronized with increased excitability, and however rich population behavior can be observed with relatively low excitability levels and sparse network configuration. The necessity of relative network sparseness for the behavioral variety is due to the role of neighbor numbers in determining total synaptic current introduced into each neuron in the network. More precisely,
neurons in a densely connected and homogeneous network topology receive almost identical and very large synaptic inputs which remove the significance of their initial condition inhomogeneity and force them to act simultaneously. Moreover, since the synaptic currents become so large at relatively large values of $I_0$ and $r$, global amplitude death appears in the whole population.

Next, we investigate the behavioral transitions with the joint variation of coupling radius $r$ and coupling strength $g$ in our system at a fixed excitability level $I_0 = 10 \mu A/cm^2$. To gain an overall view for coupling parameters’ impacts on population dynamics, a behavioral transition map $(r, g)$ plane is obtained as shown in Fig. 6. It is obvious that the coupling strength $g$ has a similar role as coupling radius $r$. For instance, consider the effect of $g$ along on the line of fixed $r = 0.1$ (see the dashed line in Fig. 6). There exists an incoherent population activity for weak synaptic connections. In this case, the coupling strength is so faint that almost all neurons act as isolated units oscillating independently from their neighbors due to superficial network interaction and very low synaptic current regimes for $g \in (0 mS/cm^2, 0.05 mS/cm^2)$. If the coupling strength is sufficiently increased, the nonlocal
interaction intensity becomes strong enough to produce extraordinary dynamic behaviors emerging with traveling waves for $g \in (0.05 \text{ mS/cm}^2, 0.2 \text{ mS/cm}^2)$ and chimera state $g \in (0.2 \text{ mS/cm}^2, 0.34 \text{ mS/cm}^2)$. With a further increase in coupling strength, the complete synchronization emerges and persists in population behavior for $g \in (0.34 \text{ mS/cm}^2, 0.5 \text{ mS/cm}^2)$. In addition, same behavioral transitions occur if one considers the variation of $r$ for a fixed $g$ in the sense that it induces emergence of dynamical behaviors in relatively the same proportion and order. However, it should be also noted that such common effects of these two parameters are valid when neither of them are very small. Now, if we are to evaluate the interaction intensity arising from the combination of two parameters in line with its growth, it is apparent that the system first exhibits incoherent behavior in the population (see the base levels of firing frequencies of the coherent and incoherent domains ($\Delta f$)). Notice that maximal differences for each case are given in bottom panels. The latter finding indicates that all neurons in the population tend to approach each other in phase domain, suggesting that the system will switch to coherent state with further increase of $r$ and $g$.

If we are to bring out explicitly the particular reason behind the occurrence of chimera and multichimera states in type-I Morris-Lecar neurons, our key insight must be that the system under consideration is nonlocally coupled neural population whose dynamic behavior is determined by excitability level of individual cells and essential ingredients of network, i.e., coupling range and coupling strength. Examining the behavior of an isolated neuron and analyzing the network activities, we found that these principal parameters have a relation with the attraction basins of population even though they have diminutive values. As an example of coupling terms' effect, in the case of Parkinson’s disease, illness or death of dopamine cells induces a disturbance of balance between synchrony and asynchrony in the basal ganglia, which results in excessive synchronization to arise due to strong coupling between neurons that actually need to be inhibited \cite{24,72,73}. In fact, this balance can be maintained and restored via integrating coupling terms that leads to an increase in the number of stable attractors in the network \cite{74–76}, and this gives rise to the emergence of chimera and multichimera states by the cause...
of random initial conditions and increasing coupling strength [68,77]. As a supporting statement, it is recently confirmed that some rare chaotic behaviors require specific choice of coupling terms [78]. In line with this reasoning, we deduce that increasing intensity of network interaction are responsible for the occurrence of multihedral chimeric behaviors.

To provide a quantitatively distinguishable view, we illustrate the regions of these different chimeras observed with various number of heads in individual parameter scales of $r$ and $g$. Figure 8 shows that there exists certain ranges of $r$ ($g$) for a fixed value of $g$ ($r$) giving rise to different multimichimera characterized by number of heads. In Fig. 8(a), one can see that the density of the nonlocal network may give rise to multimichimeras up to 6 chimera heads as the coupling radius $r$ increases, but note that we do not observe a 2-headed chimera state with this parameter scan. In a similar fashion, it is possible to see all multimichimera states including a 2-headed chimera with increasing the coupling strength $g$ [Fig. 8(b)]. Consequently, an intense nonlocal network interaction brings the neural population closer to coherent state (red regions in both figures) since all units begin to oscillate faster and dynamic variables of the system approach to each other. It is important to note here that the nature of fine-structured multimichimeras we observed is different from those reported in previous works on nonlocally coupled oscillators of type-I excitability [59]. They rather resemble chimera states reported in lattice limit cycle models [79] and networks of FitzHugh-Nagumo models with a fractal structure [51]. Moreover, the proximity of parameters $r$ and $g$ in determining interaction intensity leads us to conclude that attracting basins may be adjusted with the preferable choice.

**IV. DISCUSSION**

In this work, we have verified the occurrence of chimera and multimichimera states in a realistic neuron model of Morris-Lecar with type-I neural excitability. Exploring in which parameter range chimera states can be observed, we have based our investigation of chimera states on excitability level of individual cells and basic ingredients of nonlocal neural network topology, i.e., the coupling radius and the coupling strength. To characterize the observed levels of spatial synchrony, regularity in neuron ensembles has been monitored by the measurements of average firing frequency and the strength of incoherence. Furthermore, since identification of result areas where chimera states and other synchrony types occur is of major importance, the parameter spaces of interest have been systematically scanned. It is found that dynamical population behaviors described above can be reached by changing not only the excitability level $I_0$ but also coupling strength $g$ and coupling radius $r$. An extensive parameter scan on $(r, I_0)$ plane has demonstrated that a rich composition of possible dynamic behaviors can obtained by only low excitability levels and sparse network configuration. Moreover, behavioral map on $(r, g)$ plane has shown that coupling strength and coupling radius have a close similarity for the occurrence of any dynamic system state. Finally, different chimera and multimichimera state patterns have demonstrated the effect of nonlocal network features. To achieve this, changes in chimera behavior have been tracked in the networked system close to the border of synchronization as the interaction intensity grows. We have detected that apart from increase in firing frequency and reduction in maximal difference, stable chimera states first happen to be forked chimera heads, and then continue to split into even finer substructures.

To date, there has been general agreement that ensembles of neural oscillators exhibit great diversity in characteristic dynamic behaviors. Many chimera studies that consider different types of oscillators have also showed that miscellaneous dynamic behaviors appear with different levels of order under variations in parameters of interest. For instance, all behavioral parameter maps presented in Refs. [50,58,80–82] imply that resulting behaviors of each system are diverse under same parameter variations although all dynamical units exhibit type-II excitability of different notation. As for different models of type-I excitability, it is surely predictable that they can also give rise to different behavioral picture on the concerning parameter map. For example, in Ref. [59], coexistence of different multimichimera states has been present in a population of type-I saddle-node infinite period oscillators. However, the population of type-I Morris-Lecar neurons here does not exhibit such a coexistence. Moreover, there are incoherent states between different multimichimera regions in Ref. [59]. But, our results do not include such an intermittent state. In regards with the appearance of self-oscillations, we find that a moderate interaction intensity is a necessity to observe chimera states in type-I neurons just after the SNIC bifurcation point due to very low firing frequency of individual units. However the case may not be the same in populations of type-II neurons just after the Hopf bifurcation (cf. Refs. [81–84]).

Finally, an important limitation needs to be emphasized. Since we focused on chimera states with the same character as in Kuramoto phase oscillators which is identified by stable manifolds of limit cycles, we used spiking neurons ($I_0 > 8.33 \mu A/cm^2$) to investigate the emergence of chimera states under the effect of nonlocal interaction intensity. Therefore,
we did not include the results on chimeric behaviors of excitable neurons ($I_0 < 8.33 \mu A/cm^2$). This actually unravels a peculiarity of our study, that is, chimeric behavior in type-I Morris-Lecar neuron population can be observed not only in the excitable regime of isolated units but also in the oscillatory regime depending on the nonlocal interaction intensity (associated with $r$ and $g$). It is also important to note that initial conditions have a great significance for the emergence of chimera states in the excitable regime. Another unanticipated finding is the level of order in the emergent population of chimera states in the excitable regime. We observe desynchronization, traveling wave, chimera state, synchronization and amplitude death. In this context, our findings shed new light on chimera states in neural populations and may also be inclusively promising for future research on the behavior of many different physical and biological systems.

**ACKNOWLEDGMENTS**

M.U. acknowledges support from Erasmus+ programme of the European Union. P.H. acknowledges support by Deutsche Forschungsgemeinschaft within the framework of Collaborative Research Center 910 and under Grant No. HO4695/3-1.


