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<td>Le, Hoa Thanh; Nour, Yasser; Pavlovic, Zoran; Ó Mathúna, S. Cian; Knott, Arnold; Jensen, Flemming; Han, Anpan; Kulkarni, Santosh; Ouyang, Ziwei</td>
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High-Q 3D Microfabricated Magnetic-core Toroidal Inductors for Power Supplies in Package

Hoa Thanh Le, Student Member, IEEE, Yasser Nour, Member, IEEE, Zoran Pavlovic, Member, IEEE, Cian O Mathuna, Fellow, IEEE, Arnold Knott, Member, IEEE, Flemming Jensen, Anpan Han, Member, IEEE, Santosh Kulkarni, Member, IEEE, Ziwei Ouyang, Senior Member, IEEE*

Abstract—Integration of power inductors is a roadblock in realizing highly miniaturized power supply in package (PSiP) and power supply on chip (PwrSoC). Inductors in such power system are used for energy storage and filtering, but they dominate in size and loss. This paper presents a novel 3D integrated silicon/three-dimensional (3D) (TSV) magnetic-core toroidal inductor for PSiP. The magnetic powder based core is embedded into TSV air-core inductor using a casting method. The unique air-core inductor design with a hollow core and suspended windings enable a complete core filling with microscale magnetic powders. The proposed casting method is simple, scalable, and generic for a wide range of magnetic powders. TSV magnetic-core inductors are fabricated in a compact size of 2.4 x 2.4 x 0.28 mm with the core content varying from 63 to 88 weight percent of soft ferrite NiZn powders. The TSV magnetic-core toroidal inductors are fabricated and electrically characterized. Small-signal measurements show a three-fold higher inductance of 112 nH and a 30% higher quality factor of 14.3 at 12.5 MHz for magnetic core inductors compared to similar TSV air-core inductors. The small-signal measurement results are verified by the modelled results. The total core loss is characterized by large-signal measurements. A suitable inductor is implemented in a 12-MHz buck converter that operates in a zero-voltage-switching mode. The converter achieves a peak efficiency of 71.6% and the output power of 2.4 W converting 12 to 5 V dc.

Index Terms—Microfabrication, inductor, through-silicon vias (TSV), magnetic materials, PSiP

I. INTRODUCTION

MINIATURIZATION of power supplies are essential for the development of smart electronics systems e.g. internet of things (IoTs), light emitting diode (LED) lightings, and consumer electronic products [1]–[3]. As more functions are packed in a limited space in such electronic systems, power supplies are required to be more compact and efficient with a lower manufacture cost [4]–[6]. Monolithic integration of power supply has been widely investigated as an ideal solution for miniaturization. The ultimate integrated power supply is power supply on chip (PwrSoC) [5]–[10], in which all active and passive components are integrated on the same die. A shorter-term integration solution is the power supply in package (PSiP) [5], [6] in which the discrete inductors and capacitors are packaged together with the power management integrated circuits. In such power supplies, passive inductors often dominate in size and loss [4]–[6], therefore, reducing inductor’s size is essential for PwrSoC development. Because switching at higher frequency enables the use of smaller inductors, the evolution of integrated power supply is highly correlated to the increase in the switching frequency i.e. 10 – 20 MHz for co-packaged or stacked PSiP and to the very high frequency range (30 – 300 MHz) for PwrSoC [9].

Microelectromechanical system (MEMS) technologies have shown a great potential for making compact, high-performance integrated inductors for a wide range of operation frequencies from a few MHz to the VHF range [8], [9]. The important advantage of MEMS inductors over the traditional discrete inductors is the possibility for IC integration and miniaturization. Previous studies investigated on winding structure optimization, magnetic material technology, and fabrication technology to achieve high inductance density, high quality factor (Q), high operation frequency, and low electromagnetic interference (EMI).

Three-dimensional (3D) toroidal inductors [11]–[14] are known for low EMI due to the high flux confinement, high Q, and high operation frequency [15]. Other 2D inductor geometries, for example spiral inductors [16], [17], racetrack inductors [18], [19], and 3D solenoid inductors [20]–[22], have strong out-of-plane stray fields. 3D toroidal inductors are classified into on-silicon (on-Si) toroidal inductors [11], [23]...
and in-silicon (in-Si) toroidal inductors [14], [24]–[26] according to the fabrication technology. Because fabricating in-Si inductors requires bulk micromachining as the windings are constructed in the substrate, in-Si inductor technology is more challenging and often more complex compared to on-Si inductor technology. However, in-Si inductors have some key advantages over on-Si inductors, such as a higher inductance density due to a lower inductor profile and the potential for advanced packaging of PSiP and PwrSoC. With the in-Si winding structures, inductor profile is substantially lower compared to similar on-Si structures. This is an important advantage for IC implementation in some applications where a low power supply profile is crucial, such as mobile phone or wearable applications [27]. Furthermore, in-Si inductors are often involved through-silicon vias (TSV) as part of the windings, therefore, inductor substrate can be used as a passive interposer for co-packaged or stacked PSiP packaging. This approach has been demonstrated by Li et al. [28] with a DC-DC buck PSiP using 2D TSV spiral inductor sandwiched between two magnetic sheets. This approach is a promising packaging technology for PSiP and PwrSoC as power supply footprint can be significantly reduced using TSV-based interposer.

Developing integrated inductors for PSiP often involves magnetic materials to achieve a useful inductance to operate at high-frequency range (10 - 20 MHz) [29]. Integration of the magnetic-core for the toroidal inductors is very challenging [26], [30]. Previous studies have reported on several deposition methods including electrodeposition, sputtering, and screen-printing, each of which has its own advantages and disadvantages as reviewed in [9]. Screen printing is a well-established and comparatively cheap technology that has been adopted for magnetic-core microinductors in the 1990s [31], [32]. The screen printing technique has the advantages of being a rather simple process with a wide range of printable materials, for example NiFe, NiFeCo for the KHz range, MnZn for frequencies below 5 MHz, and NiZn for an operating frequency as high as 10 MHz and above [28], [33]. NiZn is a preference due to its high resistivity and suitable relative permeability.

In this paper, we report a high-Q 3D TSV in-Si magnetic-core MEMS toroidal inductors for high frequency (10 - 20 MHz) power conversions. The specific contributions of this paper include: (i) A simple casting fabrication process for 3D TSV in-Si magnetic-core toroidal inductor integration. The process is demonstrated with, but not limited to, a composite material consisting of a non-conducting polydimethylsiloxane (PDMS) and 17-µm-diameter NiZn powders. The magnetic composite material is embedded into the pre-fabricated MEMS Through Silicon Vias (TSV) air-core toroidal inductors reported in our previous work [34]. The process is also demonstrated with 50-µm-diameter soft magnetic composite (SMC) particles. Furthermore, the reported process is fully compatible with the screen-printing technique for production scaling. (ii) An improved inductor performance in terms of inductance density and quality factor, i.e. 3 times higher inductance and 30% higher quality factor, compared to the prior microfabricated toroidal inductors. (iii) The fabricated inductors are modelled and fully characterized by small-signal measurement, large-signal measurement, and testing in power converter.

This paper is organized as follows: Section II presents the fabrication of the TSV magnetic-core toroidal inductor using a casting process based on a molding approach for a controlled core thickness and void-free magnetic core. Section III presents the magnetic characterization of the magnetic-core material and electrical characterization of the fabricated TSV inductors. The measurement results are compared to the modelled results. Section IV describes the implementation of a 12-MHz buck converter using a TSV magnetic-core toroidal inductor and GaN FETs. The last section concludes the paper.

II. TSV MAGNETIC-CORE TOROIDAL INDUCTOR

For the operational frequencies from 10 to 20 MHz, an inductance of 100s of nH is needed to achieve higher power converter efficiency and density. Magnetic core based inductors achieve significantly higher inductance densities in comparison to their air core equivalents, resulting in lower ripple current in the converter and lower losses. Fig. 1 shows the proposed TSV magnetic-core toroidal inductor fabricated based-on a pre-made TSV air-core inductor using a simple casting and curing process for the subsequent filling of the magnetic composite. The dimensions of the 3D TSV air-core toroidal inductor are illustrated in Fig. 1a and presented in Table I.
The TSV air-core toroidal inductor is fabricated by a novel MEMS fabrication process reported in [34]. The developed process is based on MEMS fabrication technologies with the focus on CMOS compatibility, scalability, and flexibility. The process consists of three stages: (i) creating TSVs by deep reactive ion etching (DRIE), (ii) electroplating of copper (Cu) and wet-etching of Cu, (iii) Si-core isotropic etching using an inductively coupled plasma (ICP) silicon etching tool to create hollow TSV air-core toroidal inductor. The process has been developed to have low processing temperature of below 200°C, thus enabling heterogeneous integration of inductors on CMOS wafers.

Further, a composite magnetic core is filled into the hollow core of the TSV air-core toroidal inductor for making an isotropic toroidal core. The composite core consists of a polymer matrix material and soft-ferrite magnetic powders. The polymer must be a non-conducting material with a low dielectric constant and a high resistivity to minimize parasitic capacitance and eddy-current losses. The soft ferrite powders must have low coercivity ($H_c$) for high-frequency operations, high resistivity ($\rho$) for low eddy-current losses, and the powder diameter has to be smaller than the inductor winding gap of 90 µm. A PDMS elastomer (Sylgard Re 184, Dow Corning, USA) and FP350 (PPtechnology, USA) - fully-sintered soft ferrite NiZn powders are selected as the matrix polymer and the magnetic powders, respectively.

The fabrication process is described in Fig. 2 and animated in the Supplementary Video V1. A mixture of PDMS and FP350 NiZn ferrite powders are prepared and casted into a stainless-steel mold with a 0.3 mm- deep, 6 x 6 mm cavity. Two parts are attached together to create the mold in which the FP350-PDMS composite is printed (step 2, Fig. 2b). A planarization step is done to get the desired composite thickness of 300µm (step 3, Fig. 2c). An air-core toroidal inductor is immerged slowly into the mold until the top thickness of 300µm (step 3, Fig. 2c). An air-core toroidal inductor is obtained after curing at 75 °C for 3 hours. (f) Step 6: the inductor is released from the mold. (g) A cross-sectional micrograph of a fabricated TSV magnetic-core toroidal inductor scanned by an X-ray inspection system XD7600NT (Nordson DAGE Corp., UK).

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The fabrication process is described in Fig. 2 and animated in the Supplementary Video V1. A mixture of PDMS and FP350 NiZn ferrite powders are prepared and casted into a stainless-steel mold. The stainless-steel mold has two parts: a flat bottom plate and a top plate with a 6 x 6 mm, 300-µm-deep cavity. Two parts are attached together to create the mold in which the FP350-PDMS composite is printed (step 2, Fig. 2b). A planarization step is done to get the desired composite thickness of 300µm (step 3, Fig. 2c). An air-core toroidal inductor is immerged slowly into the mold until the top windings are covered. The sample is cured at 75 °C for 3 hours on a hot plate. The magnetic-core inductor is obtained after releasing from the mold (step 6, Fig. 2f). Fig. 2g shows a cross-sectional micrograph of the fabricated TSV magnetic-core inductors scanned by an X-ray inspection system XD7600NT (Nordson DAGE Corp., UK). It is clearly shown that the magnetic core is fully filled without air-voids. In addition, it is noticed that the magnetic material covers the top and bottom windings thus confining the out-of-plan one-turn flux to further minimize the EMI issue.

The important parameters in the casting process are (i) a high-concentration core for a high inductance density, (ii) a homogeneous core with uniformly distributed magnetic powders for a good isolation between the powders, and (iii) a void-free filling without air gaps. In case of distributed air gaps, these will reduce the effective core volume thus reducing the effective permeability ($\mu_{eff}$). In addition, they can create thermal instability due to the thermal expansion generated by the cycled temperature during operation. The casting process is optimized towards these objectives by varying the powder content ($C_{FP350}$). A high $C_{FP350}$ increases the possibility of forming air gaps. Six inductors were fabricated with the $C_{FP350}$ varies from 63 to 88 weight percent.

### Table 1: Dimensions of 3D TSV Toroidal Inductors

<table>
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<th>Parameter</th>
<th>Description</th>
<th>Value</th>
<th>Unit</th>
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<tr>
<td>N</td>
<td>Number of turns</td>
<td>25</td>
<td>turns</td>
</tr>
<tr>
<td>$R_i$</td>
<td>Toroidal inner radius</td>
<td>300</td>
<td>µm</td>
</tr>
<tr>
<td>$R_o$</td>
<td>Toroidal outer radius</td>
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<tr>
<td>h</td>
<td>Inductor height</td>
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<tr>
<td>$t_{copper}$</td>
<td>Copper slab thickness</td>
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<td>µm</td>
</tr>
<tr>
<td>$d_{TSV}$</td>
<td>TSV diameter</td>
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<td>µm</td>
</tr>
<tr>
<td>$G_w$</td>
<td>Winding gap</td>
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<td>µm</td>
</tr>
<tr>
<td>$G_a$</td>
<td>Air gap between windings</td>
<td>400</td>
<td>µm</td>
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Fig. 2. A manual casting process for magnetic core fabrication. (a) Step 1: a stainless-steel mold with a 0.3-mm-deep, 6 x 6 mm cavity, (b) Step 2: casting of the composite material into the mold, (c) Step 3: a planarization step is done to get a uniform composite layer with a thickness of 0.3 mm, which is designed to be slightly thicker than the inductor thickness of 280 µm to avoid overfilling of the core material over the copper windings. (d) Step 4: immersing of the air-core inductor into the composite layer, (e) Step 5: the core is cured at 75 °C for 3 hours, (f) Step 6: the inductor is released from the mold. (g) A cross-sectional micrograph of a fabricated TSV magnetic-core toroidal inductor scanned by an X-ray inspection system XD7600NT (Nordson DAGE Corp., UK).
(wt%). The results are described in Table II and Fig. 3. At $C_{FP350} = 88$ wt%, big air avoids were observed as shown in Fig. 3b. The maximum $C_{FP350}$ is 84 wt% for a void-free core as shown in Fig. 3c. Other factors are the curing temperature and curing pressure. A curing temperature was optimized at 75°C.

The uniformity of the core depends on the size of the magnetic powders which must be smaller than the winding gap of 90 µm. Due to the limiting winding gap, it is required to perform a grinding step [35] for bigger powders or to use finer powders e.g. sub-micron or nanoscale powders [36]–[38]. The inductors made of finer powders will have higher packaging factors thus achieving higher inductance. The proposed process has an advantage in the flexibility to implement different magnetic materials and matrix polymers for other applications e.g. thermal conductive polymers for better thermal dissipation. The proposed fabrication process was made on individual inductor dies but it can be scaled to the wafer-level processing by using a well-established screen-printing technique.

### III. ELECTRICAL CHARACTERIZATION

#### A. Small Signal Measurement

The TSV air-core and magnetic-core toroidal inductors were electrically characterized using a precision impedance analyzer and vector network analyzer (VNA). The two-port scattering-parameters were measured on a E5071C VNA (0.3 MHz – 20 GHz, Agilent, USA) with 500-µm-pitch ground-signal (GS) probes connected to two terminals of the inductors as shown in Fig. 4c. The measured S-matrix was then converted to the Z-matrix which is used to extract the inductor’s equivalent elements i.e. resistance and inductance. The bias measurements were done by using a HP4285 LCR meter and a current source HP42841.

Fig. 4 presents the small-signal measurement results of the air-core and magnetic-core TSV toroidal inductors. The
inductances measured at 1 MHz of the air-core and magnetic-core inductor are 38.2 nH and 86.0 nH, respectively. The calculated inductances using equation (1), are 37.5 nH (air core) and 85.2 nH (magnetic core). Several models for the TSV air-core toroidal inductor are presented in [15, 39–41]. A parasitic capacitance model is presented in [40]. The air-core inductance is calculated by eq (1) [40]–[41] with two terms created by an N-turn poloidal current and a single-turn toroidal current, respectively. From 1 to 50 MHz, this model has less than 6.7% error compared to the measured air-core inductance. The inductance of the TSV magnetic-core toroidal inductor \( L_{\text{mag}} \) is calculated using a relative permeability \( \mu_r \approx 2.4 \) which is measured by a high-frequency permeameter (PMM-9G1; Ryowa Electronics Co., Ltd., Japan). It is assumed in the frequency range below 50 MHz, the permeability is frequency-independent.

In Fig. 4a, \( L \) decreases slightly with frequency resulting in a slight inductance drop of 4% at frequencies above 40 MHz. On the other hand, the modelled inductance, which is calculated as the imaginary part of the inductor impedance, increases slightly at the frequency above 40 MHz due to a resonant effect with the measured resonant frequency of 142 MHz. The inductance model for \( L_{\text{mag}} \) has less than 5.5% error for the TSV magnetic-core toroidal inductor:

\[
L = \mu_r \left[ \frac{N^2 h \mu_0}{2 \pi} \ln \left( \frac{R_o}{R_i} \right) + \frac{R_o + R_i}{2} \right] \ln \left( 8 \frac{R_o + R_i}{R_o - R_i} - 2 \right) \tag{1}
\]

where \( N \) is the number of turns, \( h \) is the inductor height, \( \mu_r \) is the relative permeability of the core material, \( R_i \) and \( R_o \) is the inner and outer radius of the TSV toroidal inductor.

Fig. 4a shows that the TSV magnetic-core inductor has a peak \( Q \) of 14.3 measured at 12.5 MHz as compared to a peak \( Q \) of 10.3 at 47 MHz of the air-core inductor. The increased \( Q \) for the magnetic core device is due to the higher inductance and lower eddy current losses in the core material at lower frequencies. On increasing frequencies, the eddy current losses in core increase, reducing the inductance and hence the \( Q \)-factor. The inductances measured at 1 MHz of the air-core and magnetic-core inductor are 38.2 nH and 86.0 nH, respectively. Fig. 4b shows the measured and calculated AC resistance \( R_{\text{via}} \) of the TSV air-core and magnetic-core inductors. In this model, it is assumed that the current in the TSVs, top and bottom conductors flows in a skin depth facing the high-field inner region of the toroidal core. The TSV air-core inductor has a resistance of 0.26 \( \Omega \) at 1 MHz and 0.40 \( \Omega \) at 12.5 MHz. The calculated resistances are 0.25 \( \Omega \) and 0.38 \( \Omega \) at 1 MHz and 12.5 MHz, respectively. For the air-core, the model has an error less than 10% for frequencies up to 25 MHz. The magnetic-core inductor has a higher resistance with 0.27 \( \Omega \) at 1 MHz and 0.49 \( \Omega \) at 13 MHz. The small-signal resistance \( R_{\text{mag}} \) is modelled with a winding resistance and an equivalent eddy-current-loss resistance. The winding resistance includes TSVs resistance \( R_{\text{via}} \) and slab resistance \( R_{\text{slab}} \) which are calculated by eq (2) [40] and (3), respectively. The trapezoidal wet-etched profile of the top and bottom windings is accounted in eq (3).

\[
R_{\text{via}} = \frac{N \rho}{2 \delta (d_{\text{via}} - \delta)} \left( \frac{1}{n_i} + \frac{1}{n_o} \right) \tag{2}
\]

\[
R_{\text{slab}} = \frac{N \rho}{\int \delta(f) [2 \pi (R_i + x)/N - G_w - 2 \delta(f) d_e/t_{\text{cu}}] dx} \tag{3}
\]

where \( n_i \) and \( n_o \) are the number of the inner and outer TSVs, \( \rho \) is the conductivity of the winding material and \( \delta = \sqrt{1/\pi f \mu \sigma} \) is the skin depth where \( f \) is frequency, \( \mu \) is copper permeability \( (4 \pi \times 10^{-7} \text{ H/m}) \), and \( \sigma \) is copper conductivity. \( h \) is the wafer thickness and \( d_{\text{w}} = 50 \mu \text{m} \) is the diameter of the TSVs. \( d_e \) is the undercut due to Cu wet etch. The top and bottom slab resistances are calculated using the same eq (3) by replacing the slab length \( l \) by the top slab length \( l_{\text{top}} \) and the bottom slab length \( l_{\text{bot}} \). \( l_{\text{top}} \) and \( l_{\text{bot}} \) are calculated by the eqs. (4) and (5), respectively.

\[
l_{\text{top}} = R_o - R_i \tag{4}
\]

\[
l_{\text{bot}} = \sqrt{(R_o - d)^2 + (R_i + d)^2 - 2(R_o - d)(R_i + d) \cos \left( \frac{2 \pi}{N} \right) + 2d} \tag{5}
\]

It is noted that the \( Q \) model is less accurate at frequencies above 20 MHz with more than 11% error. This is because the modelled resistance is lower than the measured resistance. The resistance model does not account for the proximity effect between the winding slabs and TSVs. An additional contribution to the resistance is a high current density at the connections between TSVs and the perpendicular winding slabs. This effect is not considered in the resistance model.

Fig. 5a shows the measured \( L_{\text{mag}}, R_{\text{mag}}, \) and \( Q_{\text{mag}} \) of the TSV magnetic-core inductors fabricated with a core concentration \( \text{C}_{\text{FP350}} \) from 63 wt% to 84 wt%. The measurements were operated at 12.5 MHz. As expected, \( L_{\text{mag}} \) increases from 86 nH to 112 nH for \( \text{C}_{\text{FP350}} \) from 63 wt% to 84 wt%. \( R_{\text{mag}} \) increases with higher \( \text{C}_{\text{FP350}} \) due to an increased eddy-current loss in larger soft-ferrite volumes. This results in a decrease of \( Q_{\text{mag}} \) from 14.3 to 11.5. Even though adding the magnetic core improves the \( Q \) factor by 30% compared to that of the air-core inductor, the peak \( Q \) still decreases with an increasing \( \text{C}_{\text{FP350}} \). Adding more core material introduces more core eddy-current losses in the device which has a higher frequency dependency than copper eddy current losses. In addition, because the winding resistance is altered by the strong magnetic field generated in the magnetic core, adding more core material will affect the current density and hence the winding resistance.

Furthermore, the fabricated TSV magnetic-core inductors were characterized under a DC bias current \( I_{\text{DC}} \) from 0 to 1.2 A as shown in Fig. 5b. All tested inductors showed a similar inductance drop of 14.1% (at \( I_{\text{DC}} = 1.2 \text{ A} \)) from its initial inductance (at \( I_{\text{DC}} = 0 \text{ A} \)). This drop is due to the saturation response of the soft magnetic materials to the applied field, hence the effective core volume reduces gradually. This reduction results in a lower effective permeability of the core thus reducing the inductance. As the bias current increases, the
MEMS power inductors. The demonstrated TSV inductors fabricated TSV magnetic-core inductors to the prior art of the saturation current ($I_{sat}$) is gradually saturated and thus the inductance decreases. A saturation current of 1.6 A is estimated with a 20% drop of inductance.

The performance of the TSV inductors can be improved further by optimizing the winding design, for example smaller winding gaps for higher winding density and larger and denser parallel TSVs for lower winding resistance. Alternative advanced magnetic materials e.g. iron-based nanocrystalline materials [36]–[38] with high saturation and high permeability can be used to enhance the inductance and power density. The magnetic materials have to be pre-sintered to avoid a high-temperature sintering process which is incompatible with CMOS fabrication technologies.

However, small-signal measurements are not sufficient to evaluate the magnetic-core inductor due to the different loss mechanisms in the core, including hysteresis loss and anomalous loss which only appear at large ac currents. Characterization and testing of the magnetic-core inductors in large-signal condition (i.e. large amplitude AC signal or in power converter) is discussed in the next section.

Table III compares the small-signal performance of the fabricated TSV magnetic-core inductors to the prior art of MEMS power inductors. The demonstrated TSV inductors (this study) have a higher Q factor than most of the integrated inductors reported in [9] and in Table III while the inductance and DC resistance are in the same range. The TSV toroidal inductors occupy a footprint of 2.4 x 2.4 mm and a height of 0.28 mm. The proposed inductors are evaluated and compared using a figure of merit (FOM) which is calculated by $FOM = \sqrt{Q_{DC} / Q_{AC} / V}$, where $Q_{DC}$ = $L_{DC}/R_{DC}$, $Q_{AC}$ is the peak small-signal Q, and V is the volume of the fabricated inductor including the substrate thickness for our inductors. The fabricated TSV magnetic-core toroidal inductors have a higher FOM than most of the reported inductors. The FOM employed here includes both the dc and ac performance of the device, which in most cases are inversely dependent. For example devices, which achieve higher inductance densities (solenoid) with increased windings, typically have higher $Q_{AC}$, but suffer from higher DC resistance. Similarly, devices achieving higher inductance densities with increase magnetic core contribution (stripline) have improved dc losses in comparison to their ac performance. Hence, a FOM where both these factors are considered presents a more realistic comparison between the different devices. One factor still not included in the FOM is the current handling capability of the device, as this data is not widely reported; the authors have chosen to use the FOM metric described above in this study. It is noted that the proposed FOM is useful to evaluate inductor’s performance when the contributions between DC and AC performances are equally important, for example zero voltage switching DC-DC buck converter in which inductor carries both DC and AC current.

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**Table III**

<table>
<thead>
<tr>
<th>Study</th>
<th>Inductor</th>
<th>Core</th>
<th>L (nH)</th>
<th>$Q_{max}$ @ f (MHz)</th>
<th>$R_{DC}$ (Ω)</th>
<th>$I_{sat}$ (A)</th>
<th>Footprint (mm²)</th>
<th>Height (mm)</th>
<th>$\sqrt{Q_{DC} / Q_{AC} / V}$</th>
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<tr>
<td>This study</td>
<td>In-Si 3D toroid</td>
<td>NiZn + PDMS</td>
<td>85</td>
<td>14.3 @ 12.5</td>
<td>0.23</td>
<td>1.6</td>
<td>5.6</td>
<td>0.28</td>
<td>46.36</td>
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<tr>
<td>UF [35]</td>
<td>In-Si 2D spiral</td>
<td>NiZn + PDMS</td>
<td>112</td>
<td>11.5 @ 12.5</td>
<td>0.265</td>
<td>1.6</td>
<td>5.6</td>
<td>0.28</td>
<td>44.46</td>
</tr>
<tr>
<td>UF [24]</td>
<td>In-Si 3D toroid</td>
<td>NiZn + PDMS</td>
<td>390</td>
<td>10 @ 6</td>
<td>0.140</td>
<td>-</td>
<td>9</td>
<td>0.83</td>
<td>22.34</td>
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<tr>
<td>HKUST [25]</td>
<td>In-Si 3D toroid</td>
<td>MxZn + PDMS</td>
<td>160</td>
<td>10.5 @ 14</td>
<td>0.265</td>
<td>-</td>
<td>169</td>
<td>0.32</td>
<td>1.47</td>
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<tr>
<td>Gatech [14]</td>
<td>In-Si 3D toroid</td>
<td>Air</td>
<td>43.6</td>
<td>16.2 @ 65</td>
<td>0.28</td>
<td>-</td>
<td>2.9</td>
<td>-</td>
<td>-</td>
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<tr>
<td>Gatech [26]</td>
<td>In-Si 3D toroid</td>
<td>CoNiFe</td>
<td>60</td>
<td>17.5 @ 70</td>
<td>0.191</td>
<td>-</td>
<td>36</td>
<td>0.6</td>
<td>3.43</td>
</tr>
</tbody>
</table>

UF: University of Florida, USA; HKUST: Hong Kong University of Science and Technology, Hong Kong; Gatech: Georgia Institute of Technology, USA.
B. Large Signal Measurement

The large-signal losses of the TSV magnetic-core inductor were measured in the frequency range from 10 to 15 MHz. The measurement setup consists of two blocks: the signal generation system and the measurement system. The signal generation system generates a sinusoidal excitation current with a high-amplitude, high-frequency AC current along with a DC bias current. The AC current is generated by a signal generator E8257D (250 KHz – 20 GHz, Agilent, USA) and then amplified by an RF-amplifier model 25A250A (10 kHz - 250 MHz, Amplifier Research, USA). A DC bias current is generated by a bench top power supply 72-10480 (3A, 250 MHz, Amplifier Research, USA). The details of the measurement technique including current sensing and compensation are reported in [42], [43].

Fig. 6 shows the large-signal testing results of a 63-wt% TSV magnetic-core toroidal inductor. The inductance and total resistance ($R_{\text{total}}$) were measured with a DC bias current from 0 to 1.6 A and a 12.5 MHz, 0.2 A AC current. The inductance drops 17 % at bias current of 1.6 A giving an estimated saturation current of 1.7 A. $R_{\text{total}}$ increases from 1 to 2 Ω as the frequency increase from 10 to 15 MHz. $R_{\text{total}}$ includes all core losses including the hysteresis loss and the anomalous loss which are neglected in small-signal measurement due to smaller excitation AC currents. The measured $R_{\text{total}}$ is shown in Fig. 6. It is noted that $R_{\text{total}}$ drops from 1.48 Ω to 1.35 Ω with an increased bias current from 0 to 1.6 A. This can be explained by the fact that when some portion of the core enters saturation, the effective core volume reduces. The saturated core volume does not contribute to the inductance but also does not add to the losses. Hence, increasing the DC current leads to a lower inductance and a lower AC core resistance.

Fig. 7 show the core loss separation from the large-signal testing of 63-wt% TSV magnetic-core inductor. The total loss ($P_{\text{total}}$) consists of four losses including eddy-current core loss and winding loss ($P_{e} + P_{w}$), hysteresis loss ($P_{h}$), and anomalous loss ($P_{a}$). $P_{\text{total}}$ is calculated from the large-signal resistance by $P_{\text{total}} = R_{\text{total}}I_{\text{rms}}^{2}$. It is interesting to note, as the test frequency is increased from 10 MHz to 15 MHz, the contribution of $P_{e} + P_{w}$ decreases from 49% to 35 % of the total loss. Assuming that the magnetic core does not significantly alter the current density in the copper windings, the winding resistance is the same for the TSV air-core and magnetic-core toroidal inductors. Hence, by subtracting the air-core resistance, the increased resistance is due to the added magnetic core. This increased resistance results in an additional core loss which is considered as the eddy-current loss ($P_{e}$). $P_{e}$ contributes an average proportion of 13.6 ± 0.15 % to $P_{\text{total}}$ at the frequency from 10 to 15 MHz. This is because the magnetic powders have high resistivity and they are isolated with high-resistivity PDMS.

The core loss is analyzed as follows: The eddy-current loss in powder-core inductor is empirically modelled by the model developed by Skarrie [44]. The measured small-signal resistance as the experimental data to determine the eddy-current loss coefficient. A similar method was reported in [45]. Specifically, the small-signal core loss is determined by subtracting the total small-signal resistance ($R_{\text{mag}}$) to the winding resistance ($R_{w}$) assuming that the added magnetic-core material does not alter the current distribution in the copper windings. This assumption has been verified by Han et al. [46] for a low-permeability magnetic-core inductor ($\mu_{c} < 4$), therefore, for our inductors which have a $\mu_{c}$ from 2.2 to 3.0 the reported approach of subtracting winding resistance is applicable. The hysteresis loss is modelled using (6) [47], and the anomalous loss, which is the subtraction of the total loss to the other losses, is calculated by $P_{a} = P_{\text{total}} - P_{e} - P_{w} - P_{h}$.

\[
P_{h} = 4fB_{ac}^{2}\frac{H_{c}}{B_{sat}}
\]

where $f$ is the excitation frequency, $B_{sat}$ is the saturation magnetic flux density, $B_{ac}$ is the applied AC flux density, and $H_{c}$ is the coercivity.
The proportion of the hysteresis loss is therefore corresponding to 41% and 29% of the total core loss at 10 and 15 MHz. The anomalous loss, which is the subtraction of the total loss to the other losses, is calculated by \( P_a = P_{total} - P_c - P_e - P_h \). It is noted that the anomalous loss contributes 9% and 37% of the total loss at 10 MHz and 15 MHz, respectively. The loss mechanism of the anomalous loss is often explained as excess eddy-currents which appear along the ferrite grain boundaries when subjected to fast switching, large ac fields. This is different to traditional eddy currents which are a macroscopic loss, primarily frequency-dependent phenomena and appear within the material to oppose flow of flux. The anomalous losses are dependent both on frequency and amplitude of applied ac fields.

From the calculated losses, equivalent resistances for the core loss can be calculated to build an equivalent model of the TSV magnetic-core toroidal inductor (Fig. 8) which can be used for inductor design.

**IV. 12 MHz Buck Converter**

A high frequency soft-switching buck converter was designed and implemented using an 85-nH TSV magnetic-core toroidal inductor and gallium nitride (GaN) field effect transistors (FETs). A schematic of the converter’s power stage is shown in Fig. 9a. The converter consists of two EPC8004 40 V GaN FETs (Q_{HS} and Q_{LS}) driven by a LM5113 high speed gate driver, a TSV magnetic-core toroidal inductor (L), input capacitors (C_{IN}) and output capacitors (C_{OUT}). An assembled converter is shown in Fig. 9b in which the TSV magnetic-core toroidal inductor under test is connected to the converter board via a test board using low-resistance copper wires. The contribution from the connection wires is included in the converter simulation with an additional inductance of 20 nH. The test board is used to measure the inductor’s small signal performance and to estimate the power loss in the inductor under test. The power stage is driven by a tunable pulse width modulator with an adjustable dead time capability. A summary of the designed voltage regulator components is shown in Table IV.

The detailed operation of such zero-voltage switching (ZVS) converter using an air-core spiral inductor is reported in [48]. The converter along with the TSV inductor is simulated using LT-spice. The simulation model for the inductor was built based on the small-signal and large-signal measurements to account for the winding loss and the core losses. Fig. 10 presents the simulated and measured waveforms. Fig. 10a shows the simulated waveforms of the high-side gate voltage which confirms that the converter operates in ZVS mode. Fig. 10b shows the simulated inductor current waveforms verify that the converter is operating in ZVS mode. Fig. 10c which indicates that the converter operates in ZVS when the FETs are turning ON. It is also noted from the measured waveform that the converter is partially soft switching due to the probe capacitance loading effect. When a probe is used to measure the switching node voltage \( V_{SW} \), an additional capacitance from the probe \( C_{probe} \) is added to the circuit in parallel to the \( C_{oss} \), as the result, it takes more time to

**TABLE IV**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( V_{IN} )</td>
<td>12 V</td>
<td>Input Voltage</td>
</tr>
<tr>
<td>( V_{OUT} )</td>
<td>3.3–5 V</td>
<td>Output Voltage</td>
</tr>
<tr>
<td>( I_{OUT} )</td>
<td>0–0.5 A</td>
<td>Output Current</td>
</tr>
<tr>
<td>( f_{SW} )</td>
<td>12 MHz</td>
<td>Switching Frequency</td>
</tr>
<tr>
<td>( L )</td>
<td>85 nH</td>
<td>Inductance</td>
</tr>
</tbody>
</table>
discharge the capacitance ($C_{oss} + C_{probe}$) by the negative inductor current ($I_L$) before the FETs turn on. Fig. 11 presents the efficiency ($\eta$) as a function of the output current ($I_{out}$) from 0 to 0.5 A for two output voltages of 3.3 V and 5 V. The converter achieves a peak efficiency of 71.6 % at $V_{out} = 5$ V.

The power loss of the TSV magnetic-core toroidal inductor is determined by the thermal measurement method [49] via DC power loss. The power loss is 0.52 W and 0.79 W for $V_{out}$ of 3.3 V and 5V, respectively. Fig. 12 shows the thermal images of the inductor under the AC power loss in the converter (Fig. 12 a, b) and the DC power loss (Fig. 12 c, d). It is noted that in the magnetic-core inductor, the heat is dissipated more uniformly through the magnetic core confirming the advantage of the magnetic core for better heat transfer. The thermal performance could be further improved by replacing PDMS by a thermal epoxy e.g. EPO-TEK® 921-FL (Epotek, USA has thermal conductivity = 1.1 W/mK, and high resistivity > 6. $10^{11}$ Ωm).

V. CONCLUSION

A high-Q TSV magnetic-core toroidal inductor for high frequency (10 – 20 MHz) power conversions has been reported. The TSV magnetic-core toroidal inductors were modelled, fabricated, characterized and tested in a high-frequency converter. The fabricated TSV NiZn-core toroidal inductors have a peak Q factor of 14.3 and an inductance of 85 – 112 nH. A selected inductor was used to implement a 12-MHz ZVS buck converter which achieved a peak efficiency of 71.6 % and successfully delivered 2.4 W to the output at the input voltage of 12 V and the output voltage of 3.3 V and 5 V. The magnetic core was integrated using a simple casting process with the potential of printing a wide range of microscale magnetic powders for other applications. Furthermore, using TSVs to build the in-Si inductor could enable the fabrication of passive interposers with integrated 3D inductors for PSiP and potentially for PwrSoC integration.

APPENDIX

The calculation of slab resistance is presented as follows: Slab width at position $x$ ($W(x)$):

$$W(x) = \frac{2\pi(R_i + x)}{N} - G_w$$

(7)
Cross-sectional area $A(x)$:

$$A(x) = \delta(f)W(x) - \delta(f)^2 \frac{d_e}{t_{Cu}}$$  \hspace{1cm} (8)

Resistivity of Cu slab $R_{slab}$:

$$R_{slab} = N \int \frac{\rho}{A(x)} \, dx = N \int \frac{\rho}{\delta(f)W(x) - \delta(f)^2} \frac{d_e}{t_{Cu}}$$  \hspace{1cm} (9)

Resistance of Cu slab $R_{slab}$:

$$R_{slab} = N\rho\int_{0}^{l} \frac{1}{\delta(f)[2\pi(R_i + x)/N - \alpha - 2\delta(f)d_e/t_{Cu}]}$$  \hspace{1cm} (10)

Top slab length $l_{top}$:

$$l_{top} = R_o - R_i$$  \hspace{1cm} (11)

Bottom slab length $l_{bot}$:

$$l_{bot} = l + 2d$$

$$= \sqrt{(R_o - d)^2 + (R_i + d)^2 - 2(R_o - d)(R_i + d)\cos(2\pi/N)} + 2d$$  \hspace{1cm} (12)

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