Title | Using feedforward digital control to improve the power quality of a three-channel BCM boost converter for PFC applications
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Publication date | 2019-03
Type of publication | Conference item
| [http://dx.doi.org/10.1109/APEC.2019.8722087](http://dx.doi.org/10.1109/APEC.2019.8722087)
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Using Feedforward Digital Control to Improve the Power Quality of a Three-Channel BCM Boost Converter for PFC Applications

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Abstract—This paper proposes a simple and effective digital feedforward algorithm to improve the power quality of a boundary-conduction-mode (BCM) boost converter for power-factor-correction (PFC) applications. BCM boost converters suffer from a zero-crossing distortion of the line current caused by the valley switching of the converter. The feedforward algorithm works by increasing the switch on-time around the zero crossing of the line voltage, which in turn increases the line current at this point. The feedforward algorithm has a very simple design procedure and implementation requiring only a single look-up table (LUT) in microcontroller software. The algorithm is implemented on a 1 kW interleaved 3-channel BCM boost converter which operates with an input rms line voltage of 85 V to 265 V, and an output voltage of 400 V. Experimental results are given for the prototype converter demonstrating a significantly improved power quality, when the feedforward algorithm is used.

I. INTRODUCTION

For power levels of 300 W and below, the combination of a full-bridge rectifier and BCM boost converter is a popular topology [1]–[3]. Operating the boost converter in BCM creates advantages such as soft-switching, small magnetic volume and a simple control structure that only requires a slow single voltage compensator to regulate the output voltage [4]. At higher power levels the single-channel BCM boost converter suffers from high rms currents which increase conduction losses, and also a high level of differential-mode (DM) electromagnetic-interference (EMI) [5], [6], thus requiring a large DM EMI input filter. A common technique used to extend the power level of the BCM boost converter is to interleave two or three boost converter channels together [7], [8].

The BCM boost converter suffers from a zero-crossing distortion of the line current. This distortion is predominately caused by the valley-switching operation of the converter. Valley switching is when the boost-converter MOSFET turns on after the energy stored in the MOSFET drain-source capacitor has discharged as much as possible back into the input capacitor of the boost converter. The valley switching results in a slightly negative inductor current at the instant before switch turn on, which distorts the line current causing it to become near zero at the zero crossings of the line voltage. This reduces the converters power quality.

A. Previous Solutions

The most popular solution is to increase the on-time around the zero-crossings using feedforward control based on the sensed input voltage. Increasing the on-time at the zero-crossing of the line current allows the converter to pull a larger input current at this point, therefore cancelling the effects of the line-current distortion attributed to the valley switching. An analog solution is proposed in [9], where the slope of the pwm-ramp signal is varied with input voltage to increase the on-time at the zero-crossing points. Although this allows for a simple and cost-effective implementation the method must be tuned experimentally for best results.

This leads to a difficult design procedure for optimal results. Similarly, in [10] an additional on-time is calculated based on the instantaneous input voltage but must also be tuned experimentally. Another method is to theoretically derive the additional on-time required to cancel the valley switching effects as a function of input voltage only. This is implemented in [11] showing significant improvement in power quality, but requires a complex numerical calculation to calculate the additional on-time needed. Other solutions use more than just the input voltage to estimate the additional on-time required, as in [12] where the optimal additional on-time is calculated as a function of input voltage, switching period and voltage-compensator output. The function is then implemented in microcontroller software but is complex, therefore requiring a high-cost microcontroller. The theoretical waveforms of the inductor current when valley switching occurs are derived in [13]. Based on this analysis the level of distortion in the line current is predicted, and from this an iterative algorithm is used to calculate the additional on-time needed to remove the valley-switching distortion. However, this implementation requires pre-loading different look-up
tables into a microcontroller, and selecting the required on-time as a function of input voltage and input current, resulting in an expensive implementation. Therefore, in [14] the same analysis to derive the optimal on-time is performed, but curve fitting is used to find a simple function based on input voltage only to calculate the additional on-time, allowing for a cheap and simple analog implementation, but also resulting in a complicated design procedure.

B. Proposed Solution

In this paper, a digital feedforward control algorithm is proposed to improve the line current distortion of a 3-channel BCM boost converter. The method is derived based on a theoretical analysis of the valley-switching operation. A feedforward algorithm is derived to calculate the additional on-time required to cancel the valley-switching distortion using only the sensed input voltage. This method allows for a very simple design procedure, does not require any experimental tuning and also has a very cheap implementation as only a single look-up table is needed. The proposed feedforward algorithm provides a good improvement in power quality under all operating conditions.

This paper is structured as follows, Section II gives a brief introduction to the basic operation of the three-channel BCM boost converter and how it is controlled. Section III gives a detailed analysis of the valley-switching operation of the converter. Section IV introduces the simple feedforward algorithm used to reduce the zero-crossing line-current distortion, which is derived from the analysis given in Section III. Finally, in section V experimental results are demonstrated on a 1 kW interleaved 3-channel BCM boost converter to show a significant improvement in the power quality of the converter when the feedforward algorithm is enabled.

II. THREE-CHANNEL BCM BOOST CONVERTER

The power stage circuit diagram of the 3-channel BCM boost converter is depicted in Fig. 1. It consists of a full-bridge rectifier, a small input capacitor $C_{in}$, three interleaved boost converter channels and a large electrolytic output capacitor $C_o$. Each boost converter channel has a switch denoted $Q_1$, $Q_2$ and $Q_3$, which are low-cost silicon (Si) MOSFETs, a diode denoted $D_1$, $D_2$ and $D_3$, which are low-cost ultra-fast Si diodes, and a ferrite inductor. Each inductor has an auxiliary winding that is connected to a zero-current detection (ZCD) circuit and is used to trigger the turn-on instant of the switch. The switch turns off after a certain on-time has elapsed.

Fig. 2 demonstrates the typical waveshapes of the input current $i_{in}$ and the inductor currents of each channel $i_{L1}$, $i_{L2}$ and $i_{L3}$ over a full-line cycle of the line voltage $v_{line}$. If effects of the valley switching are assumed to be negligible, the average inductor current of each channel can be calculated as

$$i_{L(avg)} = \frac{1}{2} i_{L(pk)} = \frac{1}{2} \frac{v_{in}}{L} t_{on}$$

where $i_{L(pk)}$ is the peak inductor current, $v_{in}$ is the rectified input voltage, $L$ is the boost inductance value and $t_{on}$ is the boost switch on-time.

![Fig. 1. Three-channel boost converter power stage.](image)

![Fig. 2. Typical waveshapes of the input current $i_{in}$ and the inductor currents $i_{L1}$, $i_{L2}$ and $i_{L3}$ over a full-line cycle of the line voltage $v_{line}$.](image)

The average input current $i_{in(avg)}$ is the sum of the average inductor currents of all channels

$$i_{in(avg)} = \frac{3}{2} \frac{v_{in}}{L} t_{on}$$

(2)

If the on-time remains near constant over a full-line cycle, the average input voltage equals a constant times the rectified input voltage. Therefore $i_{in(avg)}$ and $v_{in}$ have the same shape, and a near-unity power factor is achieved. This is the basis of constant-on-time control [4], which is normally used to regulate the output voltage of BCM boost converters. However, this simplified analysis ignores the effects of the resonance between the MOSFET drain-source capacitance $C_d$, and the boost inductor, which creates a negative inductor current just before MOSFET turn-on. A discussion of how this resonance creates the zero-crossing distortion in the input line current is explained in the next section.
III. LINE-CURRENT DISTORTION

BCM boost converters typically suffer from a line-current zero-crossing distortion. The typical waveshape of the line voltage and line current are shown below in 3. A region exists around the zero-crossing of the line voltage where the line current is zero.

![Fig. 3. Typical waveform of the line voltage $v_{line}$ and line current $i_{line}$ for a BCM boost converter with significant zero-crossing distortion.](image)

In order to understand how to reduce the line-current distortion, it is important to understand how it is created. The distortion is predominately caused by the effects of the resonance between the MOSFET drain-source capacitance $C_{ds}$ and the boost inductance $L$. The resonance has a dramatic effect on the shape of the inductor current waveform.

Fig. 4 shows the circuit diagram of a single channel of the interleaved boost converter, including the MOSFET drain-source capacitance and body diode $D_Q$.

![Fig. 4. A single channel of the interleaved boost converter including the MOSFET drain-source capacitance $C_{ds}$ and body diode $D_Q$.](image)

During a single switching cycle, the boost inductor current charges linearly when the switch is turned on. Once a certain on-time has elapsed, the switch turns off and the energy stored in the boost inductor forces the boost diode to be forward biased and charges the output capacitor. When the inductor current has discharged to zero amps, the capacitor $C_{ds}$ is still charged to the output voltage $v_o$. If the switch remains off, the energy stored in $C_{ds}$ resonates with the boost inductor $L$. Each boost-converter channel has a zero-current-detection (ZCD) timing circuit that detects when the energy stored in $C_{ds}$ has discharged as much as possible into the boost converter’s input capacitor $C_{in}$. This transfer of energy from $C_{ds}$ to $C_{in}$ during each switching cycle reduces the converter’s switching losses. However, this operation also results in the inductor current becoming slightly negative before every MOSFET turn-on instant as is shown in Fig. 5. Fig. 5(a) shows the typical shape of the inductor current over several switching cycles at high instantaneous input voltage, and Fig. 5(b) shows the same waveforms, but at a low instantaneous input voltage.

It can be seen from Fig. 5(b) that the shape of the inductor current has a near-zero average value. As a result, there is a region around the zero-crossing of the line voltage $v_{line}$ where the line current $i_{line}$ is near zero.

![Fig. 5. Inductor current shape at (a) high and (b) low instantaneous input voltages over several switching cycles.](image)

By carrying out a more detailed analysis of the inductor current waveshape over a single switching cycle, it is possible to come up with an additional on-time $t_{add}$, that must be added to the the on-time $t_{on}$ to cancel the effects of the resonance. There are two possible waveshapes for $i_L$ depending on whether $v_{in}$ is greater than or less than half of the voltage $v_o$. First we will look at the case when the input voltage is greater then half of the output voltage, this scenario is displayed in Fig. 6.

![Fig. 6. Waveshape of $i_L$ and $v_{ds}$ over a single switching cycle when $v_{in} > \frac{1}{2} v_0$.](image)

In the time interval $0 \leq t \leq t_{on}$ the MOSFET is switched on, and the inductor is charged linearly by the input voltage. In the interval $t_{on} < t \leq t_2$ the MOSFET is switched off, and the inductor current charges the capacitance $C_{ds}$ until the voltage $v_{ds}$ reaches the same value as $v_o$ and the boost diode $D$ becomes forward biased. In the region $t_2 < t \leq t_3$ the diode $D$ remains forward biased while the energy in the boost inductor discharges into the output capacitor $C_{in}$. This continues until $i_L = 0$, and the diode $D$ becomes reversed biased once more. At the instant $t = t_3$, the energy stored in the $C_{ds}$ begins to flow back into the input capacitor $C_{in}$. This causes the inductor current to become negative in the region $t_3 < t \leq t_4$. 

In summary, the line-current distortion can be reduced by adding an additional on-time $t_{add}$ to the on-time $t_{on}$, which cancels the effects of the resonance.

In conclusion, the line-current distortion in BCM boost converters can be reduced by carefully considering the timing of the switching cycle and the relationship between the input and output voltages. Future work could focus on developing more sophisticated control strategies to further minimize the distortion and improve the overall efficiency of these converters.
As the capacitance \( C_{ds} \) is much smaller than the input capacitance \( C_{in} \), the input voltage can be assumed to be constant over a single switching cycle. Similarly, as the diode’s capacitance is much smaller than \( C_{ds} \) it is assumed to be negligible. By Kirchoff’s voltage law, the following characteristic equation can be written to describe the inductor current and MOSFET drain-source voltage.

\[
-v_{in} + L \frac{d i_L}{dt} + v_{ds} = 0 \\
-v_{in} + LC_{ds} \frac{d^2 v_{ds}}{dt^2} + v_{ds} = 0
\]  

(3)

Solving (3), using the initial conditions of \( i_L(t_3) = 0 \) and \( v_{ds}(t_3) = v_{in} \), and assuming the capacitance \( C_{ds} \) is a constant, the following expressions can be written for \( i_L \) and \( v_{ds} \), as functions of time.

\[
i_L(t) = -C_{ds} \omega_r (v_o - v_{in}) \sin(\omega_r (t - t_3))
\]

(4)

\[
v_{ds}(t) = v_{in} + (v_{in} - v_o) \cos(\omega_r (t - t_3))
\]

(5)

where \( \omega_r = \frac{1}{\sqrt{LC_{ds}}} \) is the resonant angular frequency between \( C_{ds} \) and \( L \). It is clear from (5) that the voltage \( v_{ds} \) reaches a minimum value of \( v_{ds} = 2v_{in} - v_o \) this occurs when \( t = t_4 \). The time instant \( t_4 \) occurs at half the resonant period after \( t_3 \), so that;

\[
t_4 = t_3 + \frac{\pi}{\omega_r}
\]

(6)

At the instant \( t = t_4 \) the ZCD circuit triggers the MOSFET to turn back on and the next switching cycle begins. By assuming the additional on-time required to cancel the line-current distortion is equal to the resonant period \( t_4 - t_3 \), a simple expression is obtained for \( t_{add} \) when \( v_{in} > \frac{1}{2} v_o \).

In the case where \( v_{in} \leq \frac{1}{2} v_o \) the energy stored in \( C_{ds} \) can discharge fully until the voltage \( v_{ds} \) reaches zero. This condition is shown in Fig. 7. In this case the time instant \( t_4 \) is found by setting \( v_{ds} = 0 \) in (5). Therefore,

\[
t_4 = t_3 + \frac{1}{\omega_r} \cos^{-1}\left(\frac{v_{in}}{v_{in} - v_o}\right)
\]

(7)

During the interval \( t_4 < t \leq t_5 \), the inductor current is charged linearly by the input voltage so that \( L \frac{d i_L}{dt} = v_{in} \), and the inductor current can be described by

\[
i_L = \frac{1}{L} \int_{t_4}^{t} v_{in} dt + i_L(t_4)
\]

(8)

When \( t = t_5 \), the inductor current reaches zero. Therefore, (8) can be used to find an expression for \( t_5 \) by setting \( i_L(t_5) = 0 \).

\[
t_5 = t_4 + \frac{L i_L(t_4)}{v_{in}}
\]

(9)

An expression can be obtained for \( i_L(t_4) \) by substituting the value of \( t_4 \) obtained in (7) into the expression for \( i_L \) obtained in (4).

\[
i_L(t = t_4) = -C_{ds} \omega_r (v_o - v_{in}) \sin(\omega_r (t_4 - t_3))
\]

\[
= -C_{ds} \omega_r (v_o - v_{in}) \sin(\cos^{-1}\left(\frac{v_{in}}{v_{in} - v_o}\right))
\]

\[
= -C_{ds} \omega_r (v_o - v_{in}) \sqrt{1 - \left(\frac{v_{in}}{v_{in} - v_o}\right)^2}
\]

\[
= C_{ds} \omega_r \sqrt{v_o^2 - 2v_{in} v_o}
\]

(10)

Combining (9) and (10) the following final expression can be obtained to define the time instant \( t_5 \)

\[
t_5 = t_4 + \frac{1}{\omega_r} \sqrt{v_o^2 - 2v_{in} v_o}
\]

(11)

By assuming the additional on-time required to cancel the line-current distortion is equal to the resonant period \( t_5 - t_3 \), a simple expression is obtained for \( t_{add} \) when \( v_{in} \leq \frac{1}{2} v_o \).

### IV. Simple Feedforward Algorithm

From the earlier analysis in Section III, we can derive the additional on-time \( t_{add} \), which must be added to the on-time calculated by the voltage compensator to cancel the effects of the valley switching. This is done by assuming the additional on-time needed to remove the valley switching distortion is given by \((t_4-t_3)\) when \( v_{in} > \frac{1}{2} v_o \), and \((t_5-t_3)\) when \( v_{in} \leq \frac{1}{2} v_o \). Therefore, the additional on-time can be obtained from (6), (7) and (11) as follows,

\[
t_{add} = \frac{\pi}{\omega_r} \quad \forall \quad v_{in} > \frac{1}{2} V_o
\]

\[
t_{add} = \frac{1}{\omega_r} \cos^{-1}\left(\frac{v_{in}}{v_{in} - V_o}\right) + \ldots
\]

\[
\frac{1}{\omega_r} \sqrt{V_o^2 - 2v_{in} V_o} \quad \forall \quad v_{in} \leq \frac{1}{2} V_o
\]

(12)

The term \( v_o \) describes the output voltage which varies with time. To simplify the equations, \( v_o \) is replaced by the
term $V_o$ in (12). The term $V_o$ is the reference voltage for the voltage compensator and is a constant 400 V. As a result, the feedforward algorithm defined by (12) only has a single variable $v_{in}$. This allows for a very simple implementation in a digital system as the curve of $t_{add}$ versus $v_{in}$ can be calculated once off, as is done in Fig. 8, over the entire range of $v_{in}$ from 0 to 375 V, and then a single look-up table can be used to calculate $t_{add}$ in the microcontroller software. As the MOSFET used has a non-linear drain-source capacitance that varies with the drain-source voltage, the term $\omega_r$ is calculated assuming a constant capacitance given by the time-effective output capacitance from the device datasheet.

![Graph showing additional on-time added by the feedforward algorithm versus input voltage.](image)

Fig. 8. Additional on-time added by the feedforward algorithm versus input voltage.

Fig. 9 depicts how the feedforward algorithm was implemented as part of the digital control scheme for the 3-channel BCM boost converter. A voltage compensator with a bandwidth of 20 Hz was designed to regulate the output voltage to a constant 400 V. The on-time equals the voltage compensator output $v_c$ plus the additional on-time calculated by the feedforward algorithm per (12), so that $t_{on} = v_c + t_{add}$. The voltage compensator was executed in an interrupt every 5 kHz. The feedforward algorithm was executed at a rate of 33 kHz. A closed-loop control strategy was implemented to maintain the correct interleaving of the converter [8]. The closed-loop control strategy works by adjusting the individual on-time of each channel $t_{on1}$, $t_{on2}$ and $t_{on3}$, to maintain the correct phase-shift.

![Diagram of three-channel boost converter control circuit with parameters and values listed in Table I.](image)

**TABLE I**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Microcontroller</td>
<td>XMC1402-Q040X0032</td>
</tr>
<tr>
<td>Boost inductance, $L$</td>
<td>130 $\mu$H</td>
</tr>
<tr>
<td>Output capacitance, $C$</td>
<td>880 pF</td>
</tr>
<tr>
<td>Input rms voltage</td>
<td>85 V to 265 V</td>
</tr>
<tr>
<td>Output voltage, $V_o$</td>
<td>400 V</td>
</tr>
<tr>
<td>Output Power, $P_o$</td>
<td>0 W to 1000 W</td>
</tr>
<tr>
<td>MOSFET</td>
<td>IPA60R090C6</td>
</tr>
<tr>
<td>Drain-source capacitance, $C_{ds}$</td>
<td>550 pF</td>
</tr>
</tbody>
</table>

one $i_{L1}$, of the converter under steady-state operation at rms line voltages of 115 V and 230 V, respectively.

![Graph showing $v_o$, $i_{line}$, $i_{in}$ and $i_{L1}$ at $P_o = 800$ W and a 115 V rms line voltage under normal steady-state operation ($v_{in}$: 500 V/div, $i_{line}$: 200 V/div, $i_{in}$: 2 A/div, $i_{L1}$: 2 A/div, timebase: 5 ms/div).](image)

Fig. 10.
current waveshape with and without the feedforward control enabled for a rms line voltage of 230 V. It is clear from comparing the waveshapes of the line current that there is again significant reduction in the line current zero-crossing distortion when the feedforward control algorithm is implemented.

To compare the effectiveness of the feedforward control algorithm, the converter was ran with and without the feedforward control algorithm enabled under different conditions. Fig. 12 shows a comparison of the shape of the line voltage and line current $i_{line}$ at 700 W output power and a rms line voltage of 115 V, with and without the feedforward control algorithm implemented. It is clear that when the feedforward algorithm is used the zero-crossing distortion of the line current is significantly reduced.

Fig. 13 shows a comparison the line voltage and line current zero-crossing distortion by drastically increasing the on-time around this point. This increases the average input current drawn by the converter at the line current zero-crossing points. When no feedforward algorithm is used the on-time calculated by the voltage compensator is near constant in steady-state operation. But when the feedforward control algorithm is enabled, there are large variations in on-time as the line voltage changes. This variation of on-time is demonstrated in Fig. 14 and Fig. 15 with and without the feedforward control algorithm enabled at a rms line voltage of 115 V and 230 V respectively.

The feedforward control algorithm reduces the line current zero-crossing distortion by drastically increasing the on-time around this point. This increases the average input current drawn by the converter at the line current zero-crossing points. When no feedforward algorithm is used the on-time calculated by the voltage compensator is near constant in steady-state operation. But when the feedforward control algorithm is enabled, there are large variations in on-time as the line voltage changes. This variation of on-time is demonstrated in Fig. 14 and Fig. 15 with and without the feedforward control algorithm enabled at a rms line voltage of 115 V and 230 V respectively.

The power factor of the converter was measured against output power with and without the feedforward control algorithm enabled. This is done in Fig. 16 for a rms line voltage of 115 V, and demonstrates a significant improvement in power factor under all load conditions when the feedforward control is enabled. Similarly, Fig. 17 shows the power factor comparison at 230 V rms line voltage, again with a significant improvement in the converter’s power factor under all load conditions.
A comparison of the input current harmonics of the converter at rated power and rms line voltage of 230 V with and without the feedforward control enabled is given in Fig. 18, demonstrates a substantial reduction in low-order harmonic components. Both sets of input current harmonic measurements are well-below the class A EN61000-3-2 limits.

VI. CONCLUSION

A easy-to-implement and effective digital feedforward control algorithm has been presented to improve the power quality of a BCM boost converter for PFC applications. A theoretical analysis of how the valley switching operation creates a zero-crossing distortion of the input line current was performed. This analysis was then used to derive an equation for the additional on-time needed to remove the zero-crossing distortion.

The simple feedforward algorithm was experimentally validated on a 1 kW interleaved 3-channel BCM boost prototype, requiring a very simple implementation where only a single LUT is needed. Experimental results are given comparing the power quality of the converter with and without the feedforward control enabled. The results show the feedforward algorithm provides a significant improvement in power quality under all load and input voltage conditions.
Fig. 18. Power factor comparison without feedforward (FF) control (continuous line) and with feedforward control (dashed line) at $P_o = 1$ kW and a 230 V line voltage against output power.

VII. ACKNOWLEDGEMENT

The authors would like to thank Advanced Energy for invaluable support, co-funding and use of equipment during this work. The authors wish to acknowledge the Irish Research Council for co-funding to make this project possible.

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